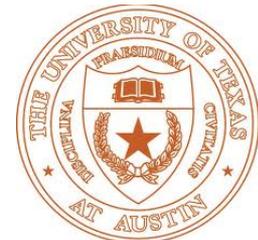


# Practical Anonymous Subscriptions

---

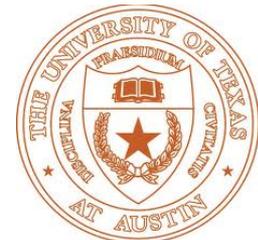
**Alan Dunn, Jonathan Katz, Sangman Kim,  
Michael Lee, Lara Schmidt, Brent Waters,  
Emmett Witchel**

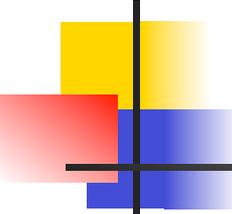


# Practical Anonymous Subscriptions

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**Alan Dunn, Jonathan Katz, Sangman Kim,  
Michael Lee, Lara Schmidt, Brent Waters,  
Emmett Witchel**





# Anonymous subscriptions

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Provide registered/paid users with the ability to *log in* and *access* services such as:

- Music/video streaming
- reading news articles
- transit pass

...while remaining **anonymous**...

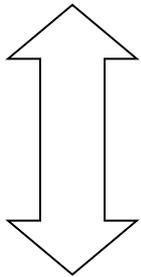
...yet still allowing the server to enforce **admission control**

I.e., users cannot share their login with friends

# System model

Time broken into a series of well-defined *epochs*

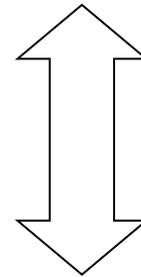
Google™

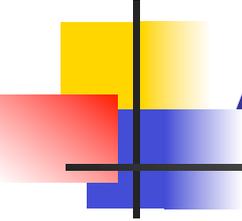


Google™



Google™



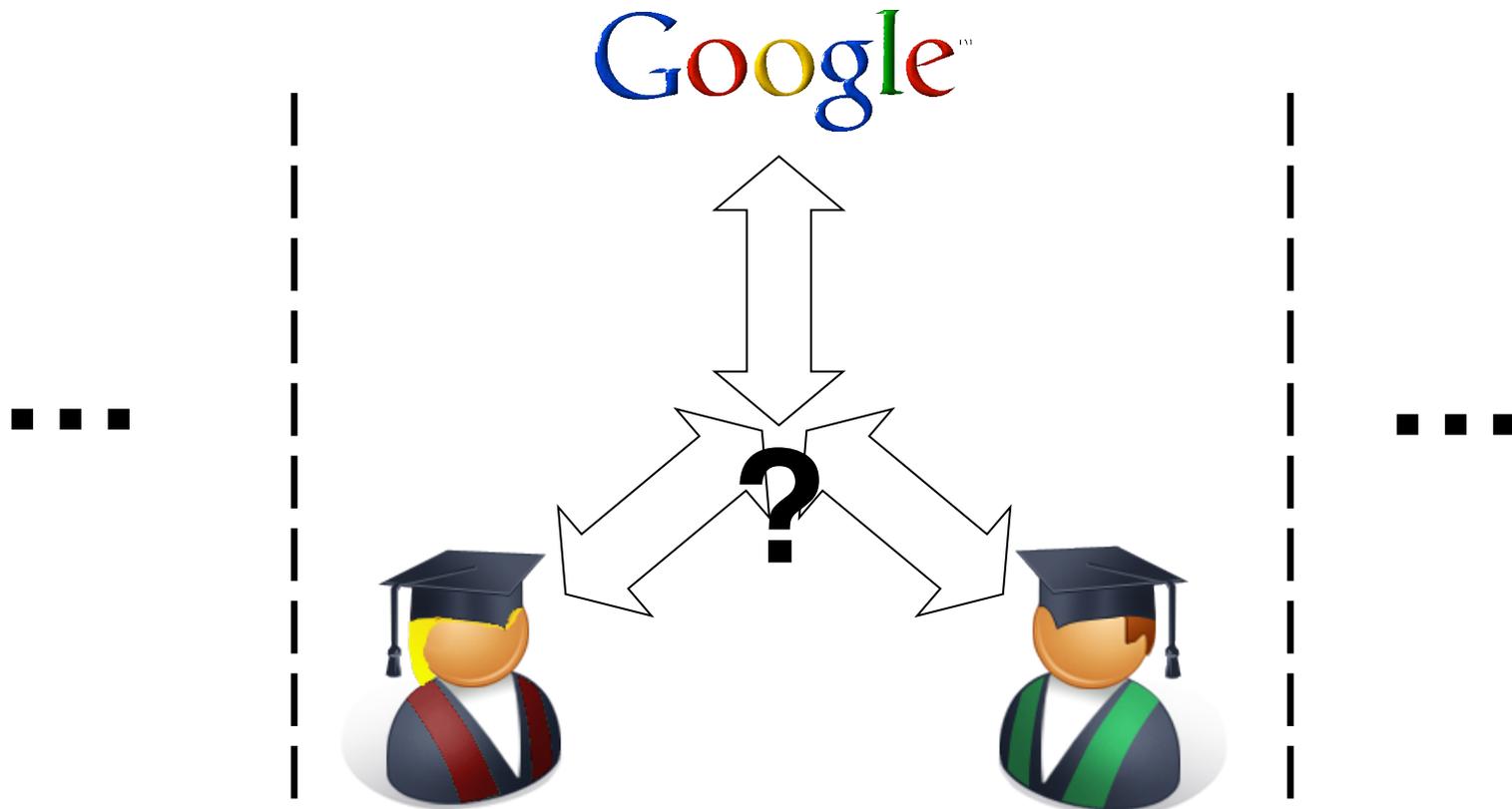


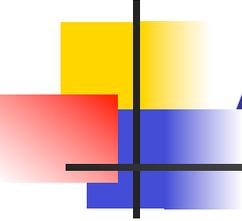
# Anonymity/unlinkability

---

- Cannot link a **user login** to a **user registration**
- Cannot link **logins by the same user** (in different epochs) to each other

# Anonymity/unlinkability





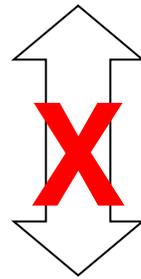
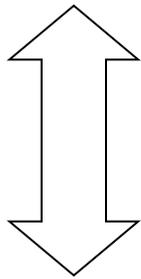
# Admission ctr' I (“soundness”)

---

- Each registered user can only have **one** active login per epoch
  - I.e., a user cannot freely share their login information with their friends
  - (Formal definition later)

# Soundness

Google™

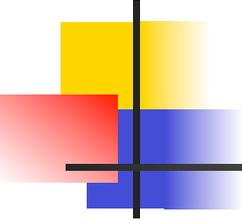


$sk_1$

$sk_1$

...

...

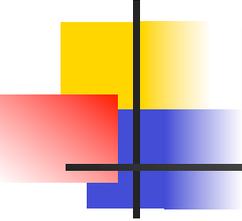


# How long is an epoch?

---

Shorter epochs  $\Rightarrow$  better anonymity

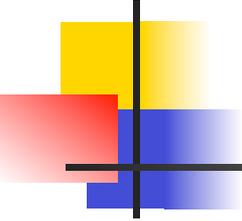
Longer epochs  $\Rightarrow$  less computation



# How long is an epoch?

---

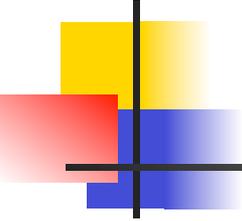
- Here: **conditional linkability**
  - Logged in user can choose to “re-up” his login for the next epoch
    - Re-up is cheaper than a login
  - Allows server to link user across epochs
    - User decides when this is acceptable
    - User can do a full login if unlinkability is desired



# Related (but different)

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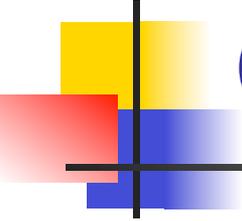
- Anonymous credentials, DAA, group signatures
  - Anonymity, but no admission control
- Anonymous blacklisting systems
  - Anonymity, revocation, but no notion of per-epoch admission control
- E-cash
  - Anonymity, double spending detected, but no notion of unlimited re-use



# Related work

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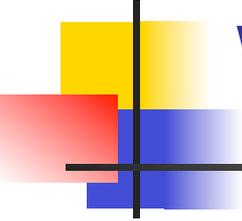
- Unclonable authentication  
[Damgård, Dupont, Østergaard]
- n-time anonymous authentication  
[Camenisch et al.]
  - Uses prior ideas from e-cash [Camenisch, Hohenberger, Lysyanskaya]
  - Different model – multiple verifiers, traceability after the fact



# Our contributions

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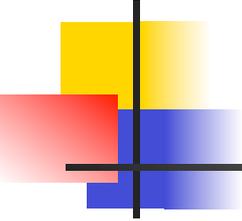
- **More efficient, simpler** construction
  - “Weaker” cryptographic assumptions
  - Cleaner definitions
- **Conditional linkability** for improved efficiency
- **Implementation** and system evaluation



# What we do *not* prevent

---

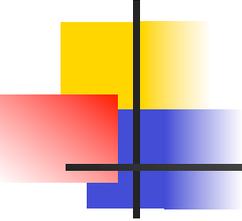
- Users sharing login information to use at **different** times
- **Other ways** of breaking anonymity
  - Traffic analysis, IP addresses
  - User behavior
  - History of accessed content
- Address using complementary techniques



# Functional definition I

---

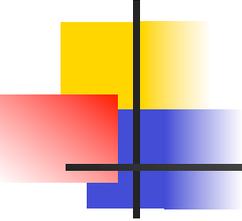
- **Setup** – server generates public/private keys; initializes state including **cur/next**
- **Registration** – user/server interact; user obtains secret key  $sk$  (or error)



# Functional definition II

---

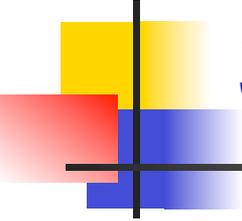
- **Login** – Using  $sk$  and the current epoch number, user logs in to server
  - Server increments **cur**
- **Link** (“re-up”) – User currently logged in during epoch  $t$  can log in for epoch  $t + 1$ 
  - Server increments **next**



# Functional definition III

---

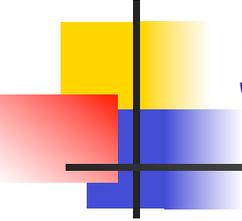
- **EndEpoch** – server refreshes state; updates **cur/next**
  - **cur = next; next = 0**



# Security definitions

---

- (Honest) user is **logged in** at some point in time if (1) that user previously ran Login in that epoch, or (2) at some point in previous epoch, user was logged in and ran Link
- (Honest) user  $i$  is **linked** at some point in time if at some previous point during that epoch, user was logged and ran Link

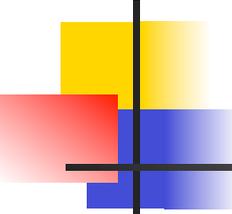


# Soundness (informal)

---

- Attacker registers any number  $N$  of users; honest users also register
- Attacker interacts with server arbitrarily
- Honest users login/link (so affect server state), but attacker cannot observe
- Attacker controls when epochs end

Attacker **succeeds** if, at any point in time,  
 $\mathbf{cur} > N + \# \text{honest users logged in}$

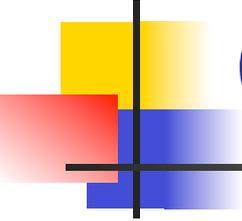


# Anonymity (informal)

---

- Phase 0
  - Attacker outputs arbitrary public key
  - Two honest users register (and get secret keys)
- Phase I
  - Attacker induces honest users to Login/Link
- Phase II – neither user logged in
  - Users either permuted or not
  - Attacker induces honest users to Login/Link

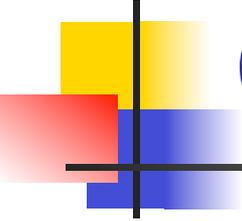
Attacker **succeeds** if it can guess whether users were permuted in Phase II (with significantly better than  $\frac{1}{2}$  probability)



# Construction (intuition)

---

- **Registration**: user gets “anonymous credential”  $C$  (i.e., a re-randomizable blind signature) on PRF key  $k$
- **Login** in epoch  $t$ : user sends  $C' + F_k(t) +$  ZK proof of correctness
  - Server verifies signature and proof; checks that  $F_k(t)$  not in table; stores  $F_k(t)$  in table
- **Link** in epoch  $t$ : user sends  $F_k(t) + F_k(t+1) +$  ZK proof of correctness
  - Look up  $F_k(t)$  in table; verify proof; add  $F_k(t+1)$



# Construction (further detail)

---

- Anonymous credential is based on variant of **Camenisch-Lysyanskaya signatures**
  - Public key =  $(g^x, g^y, g^z)$
  - Signature on  $(d, r)$  is  $(g^a, g^{ay}, g^{ayz}, g^{ax}(g^d Z^r)^{axy})$
  - Re-randomizable, blindable, efficient ZK proofs
- **Dodis-Yampolskiy PRF**
  - $F_k(t) = g^{1/(k+t)}$
  - Compatible with various efficient ZK proofs

# Construction (further detail)

## ■ Registration

User

$$d, r \leftarrow Z_q$$

$$M = g^d Z^r$$

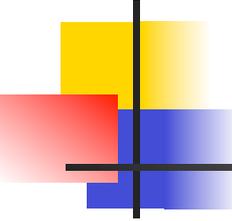
PoK (d, r)

Server

$$a \leftarrow Z_q$$

$$g^a, g^{ay}, g^{ayz}, g^{ax} M^{axy}$$

Verify...



# Construction (further detail)

---

## ■ Login (epoch t)

User

$sk = (A, B, Z_B, C, d, r)$

$r, s \leftarrow Z_q$

$A^r, B^r, Z_B^r, C^{rs}$

Server

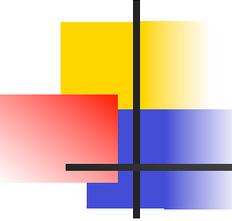
$Y = g^{1/(d+t)}$

Verify...

Y not in table

PoK

(d in signature matches d in Y)



# Construction (further detail)

---

- **Link** (epoch  $t$ )

User

$sk = (A, B, Z_B, C, d, r)$

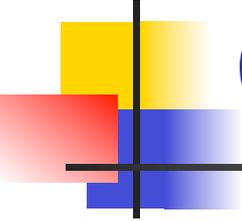
Server

$$Y = g^{1/(d+t)}, Y' = g^{1/(d+t+1)}$$

Y in table?

PoK

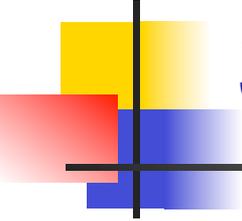
(Y and Y' have correct form,  
and d in Y matches d in Y' )



# Construction (further detail)

---

- ZK proofs (of knowledge) fairly standard
  - Made non-interactive using Fiat-Shamir

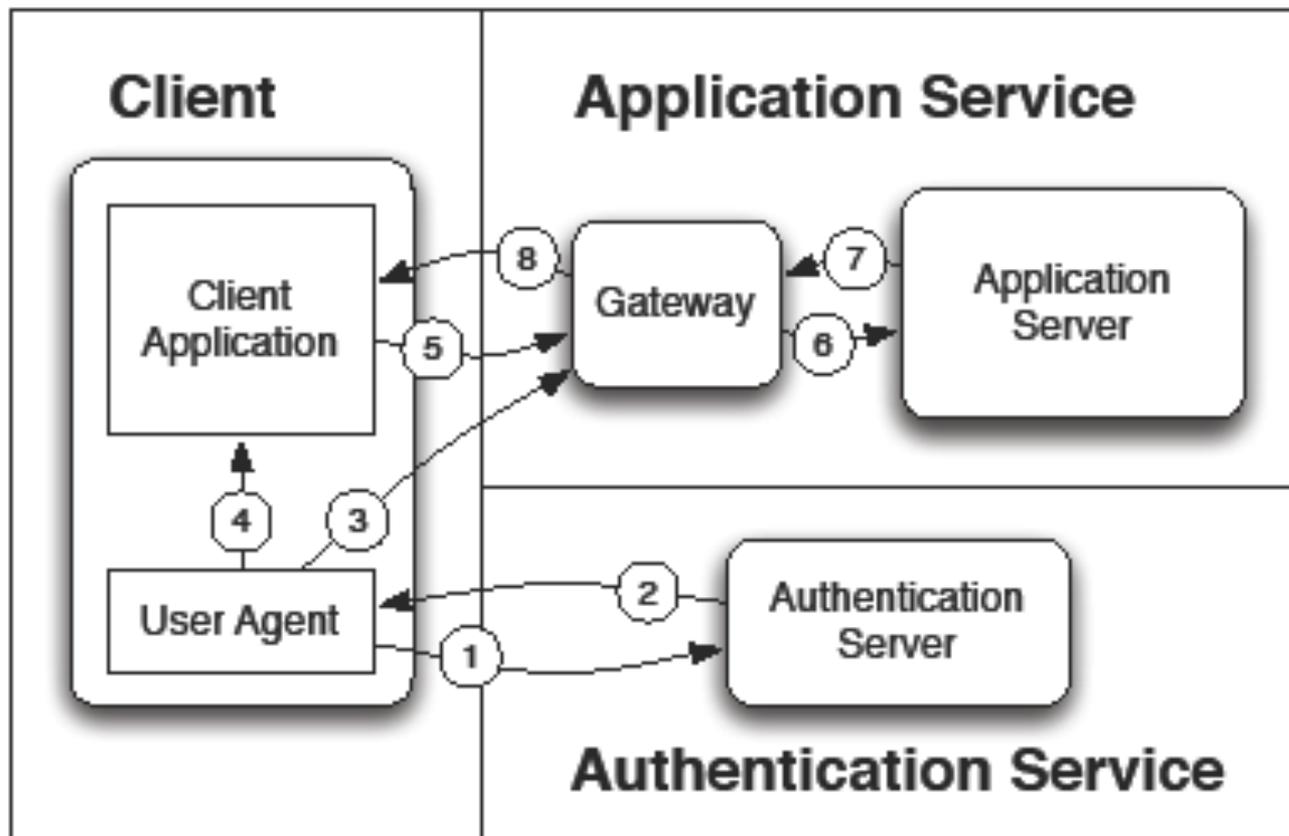


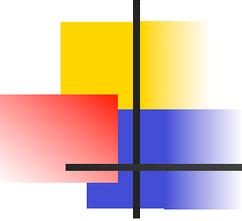
# Security guarantees

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- Soundness holds under **LRSW assumption** (essentially, unforgeability of CL signatures)
- Anonymity holds under **DDHI assumption**
  - $g^{1/x}$  “looks random” even given  $g^x, \dots, g^{x^n}$
- Note: in our security proofs, we assume extraction from all ZKPoKs is possible
  - Can be enforced if interactive proofs are used and sequentiality is enforced
  - Heuristic security if Fiat-Shamir proofs are used

# System architecture

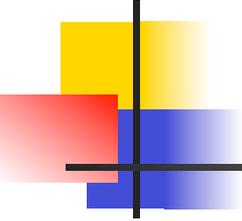




# Notes

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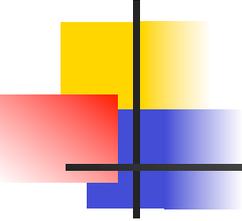
- Only loose synchronization needed
  - Server sends timestamp when connection is established
  - User caches previous timestamp to prevent rollback attacks on anonymity
- Login + (multiple) link(s) are done more efficiently than running Login, Link, ...



# Implementation

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- Using PBC library [Lynn] and PolarSSL
  - Symmetric pairing; 160-bit elliptic-curve group over 512-bit field
- 1400 loc
- Pre-processing used when possible

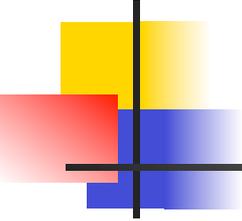


# Raw performance

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	<b>User</b>	<b>Server</b>
<b>Login</b>	13.5 ms	7.9 ms
<b>Link</b>	1.3 ms	0.72 ms

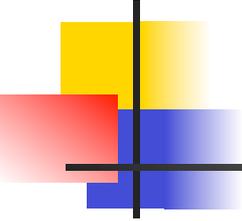
(quad-core 2.66 GHz Intel Core 2 CPU, 8GB RAM)



# Evaluation I

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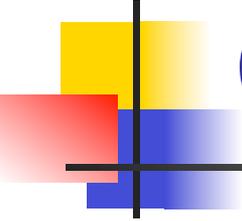
- Integrated our system into a streaming-music service
  - 7500 users
  - Epoch length = 15 seconds
  - Acceptable performance in terms of playback delay/latency; details in paper



# Evaluation II

---

- Anonymous public-transit passes
  - Epoch length = 5 minutes
  - Estimate <10 servers could handle BART peak-traffic volumes
- Implemented user agent as Android app
  - Login message displayed as QR code for physical scanner to read
  - No network connectivity required
  - Login time: 220 ms (HTC Evo 3D)



# Conclusions

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- Design, implementation, and evaluation of a system providing **anonymous subscriptions**
- Formal definitions, cryptographic proofs
- Performance acceptable for practical applications