



Algebraic Pseudorandom Functions with Improved Efficiency from Augmented Cascade

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Hart Montgomery

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Stanford University

Pseudorandom Functions

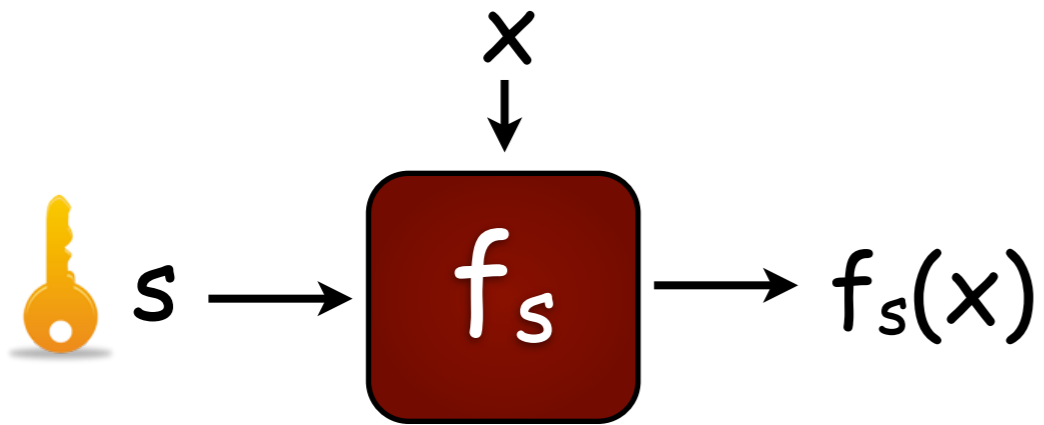


- Definition

Pseudorandom Functions



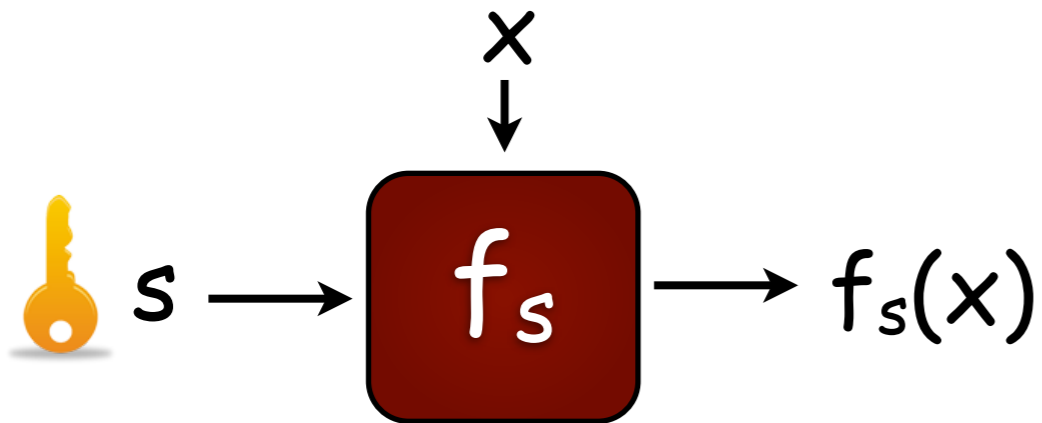
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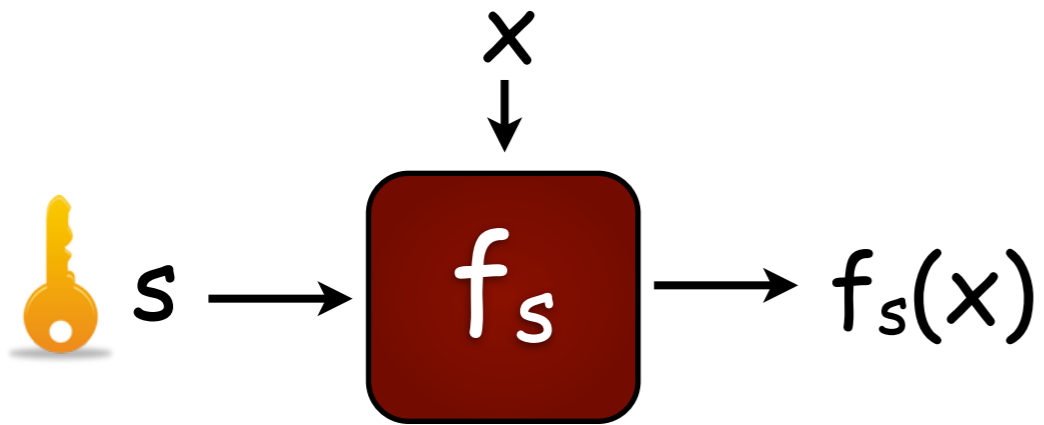


The function f
looks like a
random function

Pseudorandom Functions



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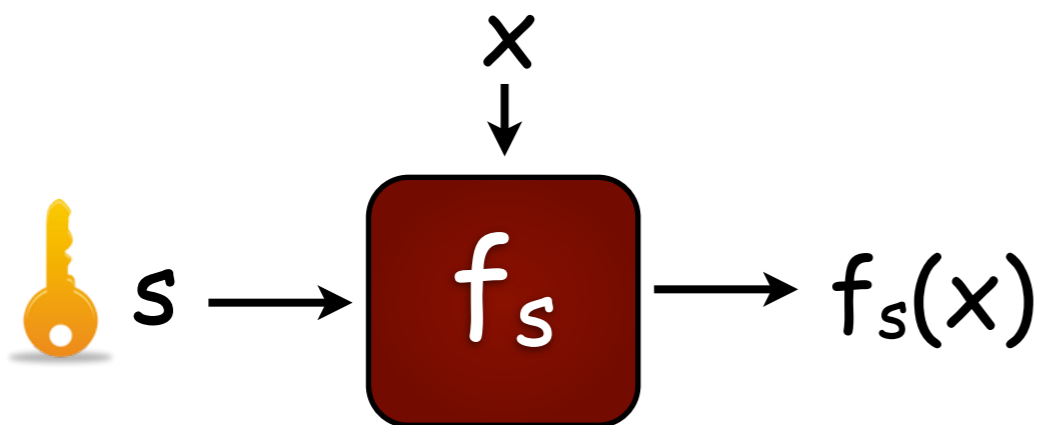
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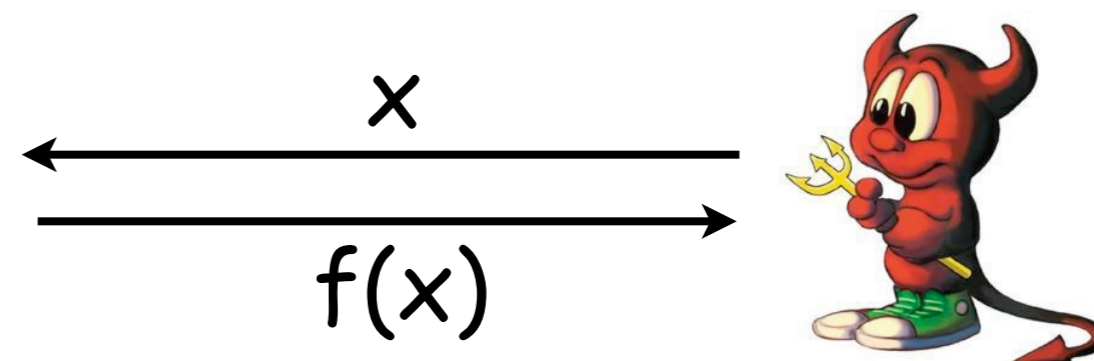


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Exp-PRF: choose a random key k and set $f(x) = f_k(x)$

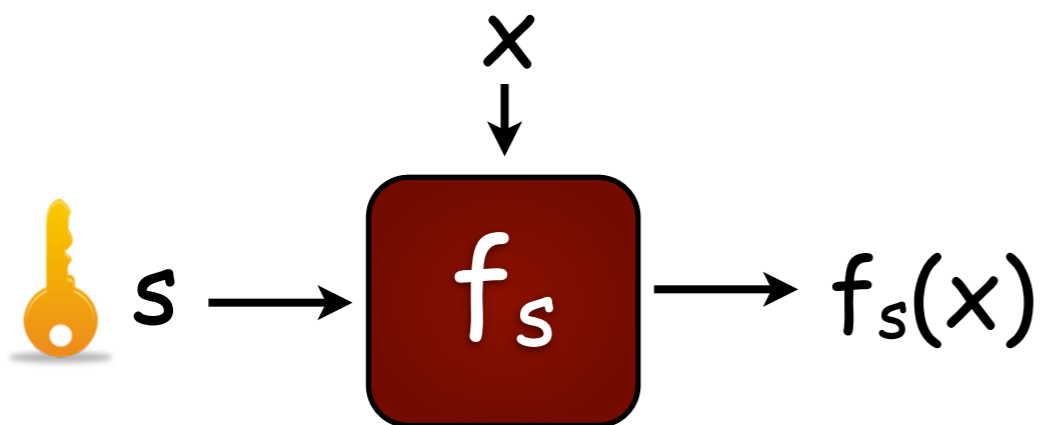
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Pseudorandom Functions



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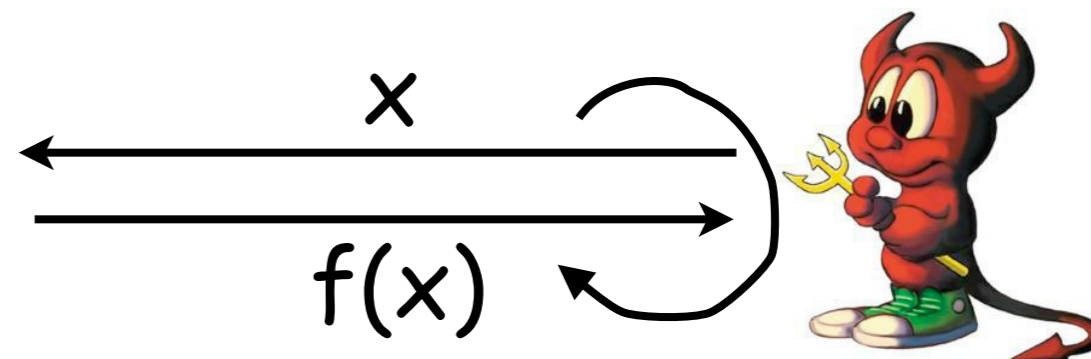


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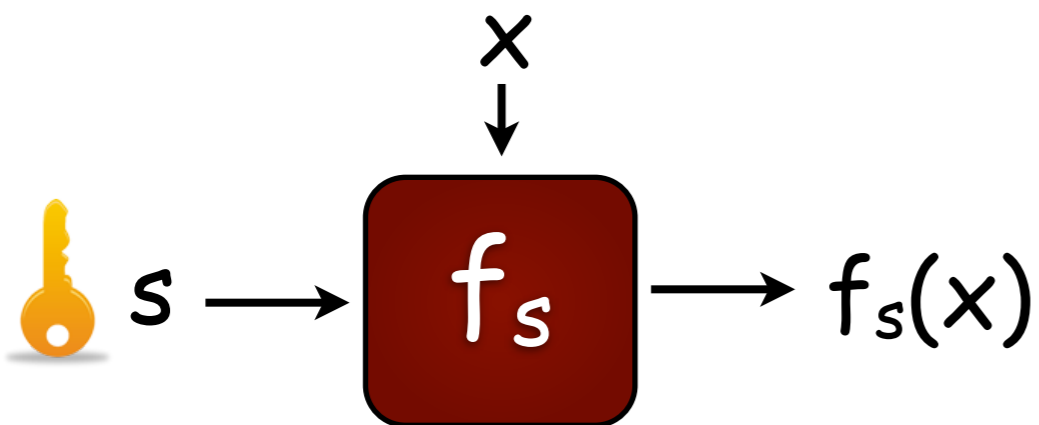
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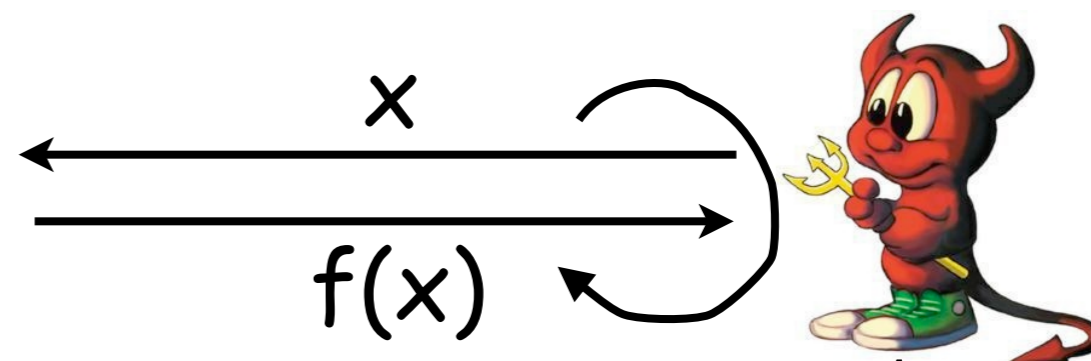


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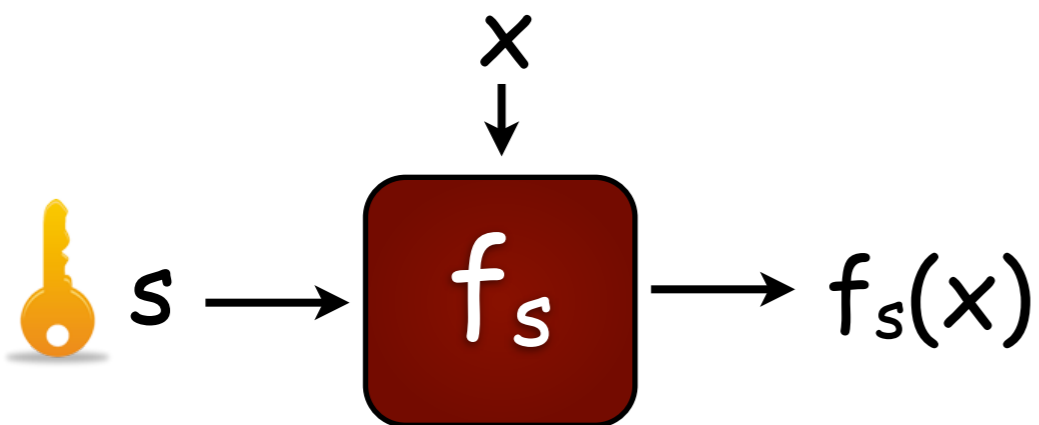


PRF? or rand?

Pseudorandom Functions



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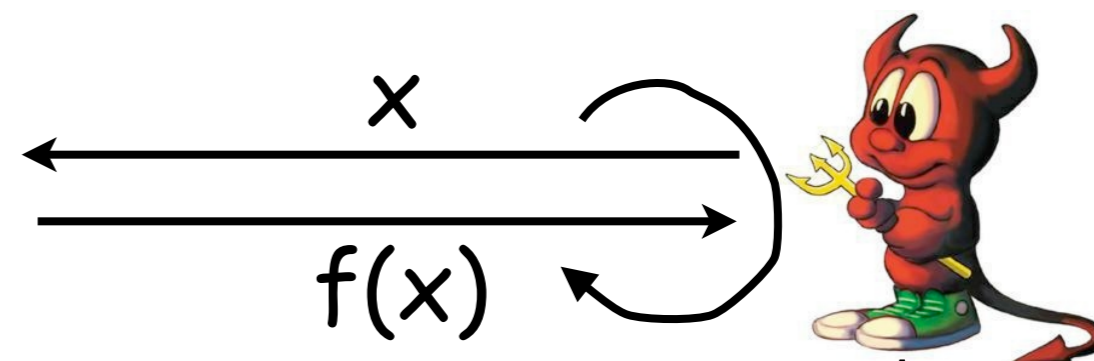
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- Security Game

Exp-PRF: choose a random key k and set $f(x) = f_k(x)$

Exp-rand: choose a random function $f(x)$

Secure if  cannot guess “PRF” or “rand” with probability better than $1/2$



PRF? or rand?



- Workhorse of cryptography. Lots of applications!
 - Private Key Crypto; parties share PRF secret
 - Message Integrity and User Authentication
 - Key Derivation schemes
 - Stateless Signature Schemes
 - Defend against denial-of-service attacks [Ber '96, CW03]
 - Prove lower bounds in learning theory; impossibility results in complexity theory

Heuristic PRFs



Heuristic PRFs



DES

Triple-DES

IDEA

Serpent

AES

Heuristic PRFs



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Very fast but unfortunately **rely on interactive assumptions**

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Algebraic Constructions



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Non-interactive assumptions: Challenges posted. Require no interaction.



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Algebraic Constructions

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Eg., DDH, Discrete Log, etc.

Cascade Construction



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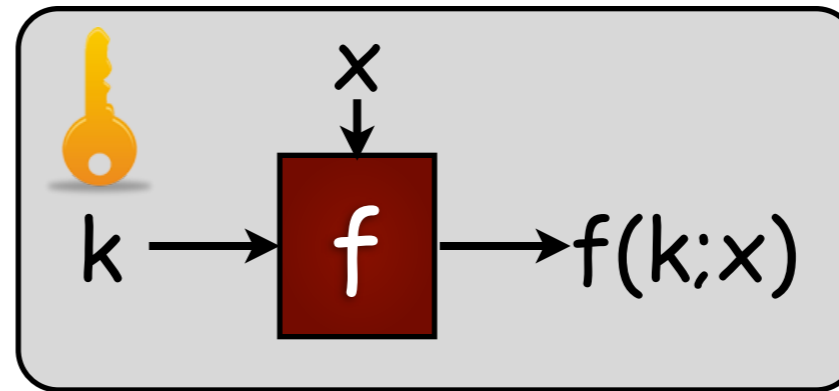
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Cascade Construction



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$$f : K \times X \rightarrow K$$

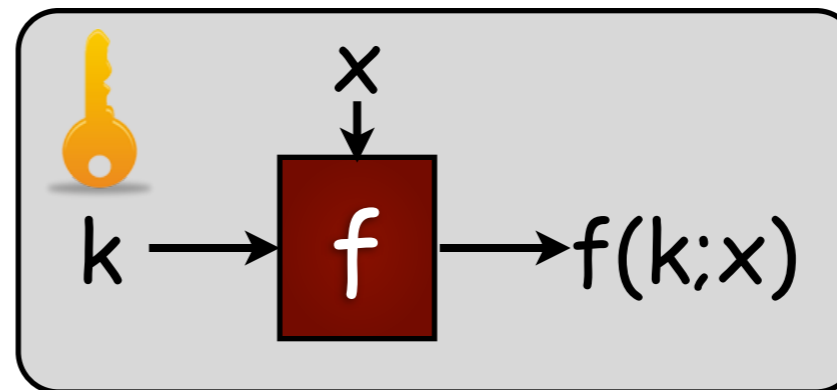


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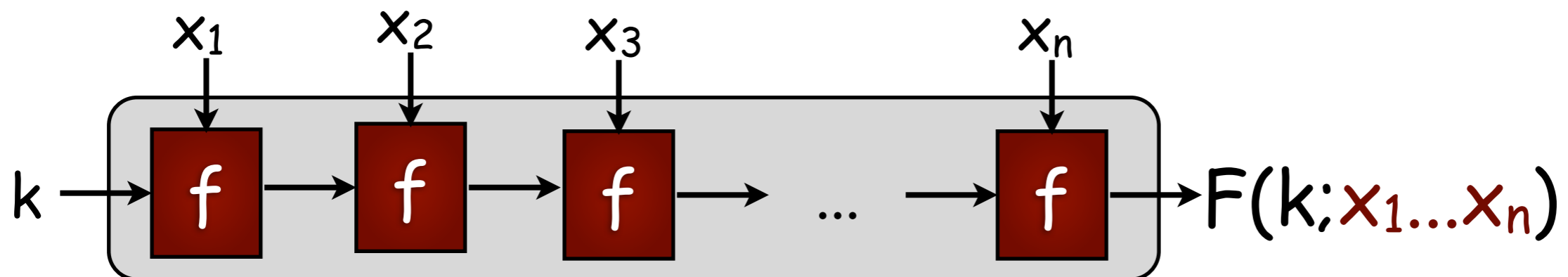


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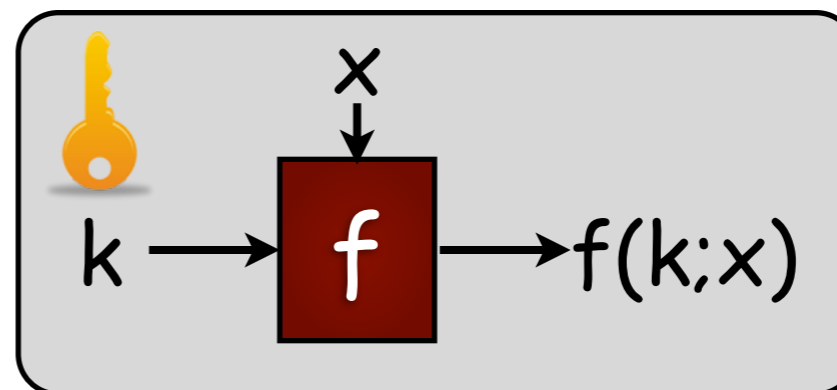


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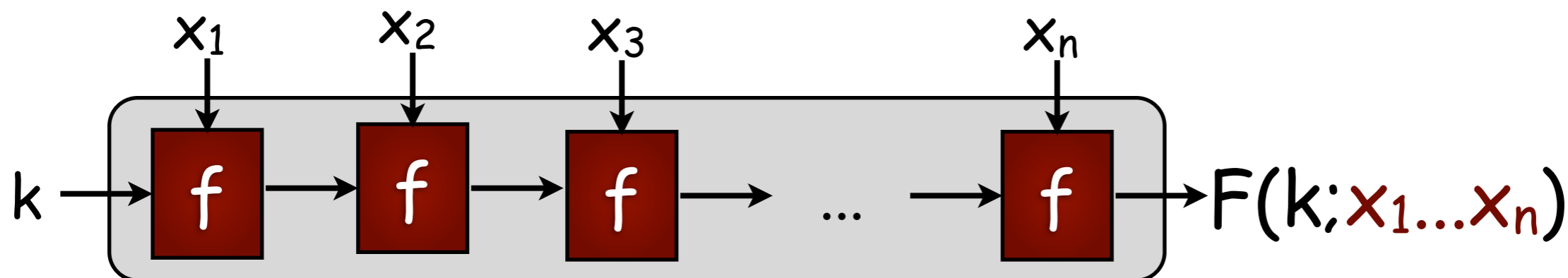


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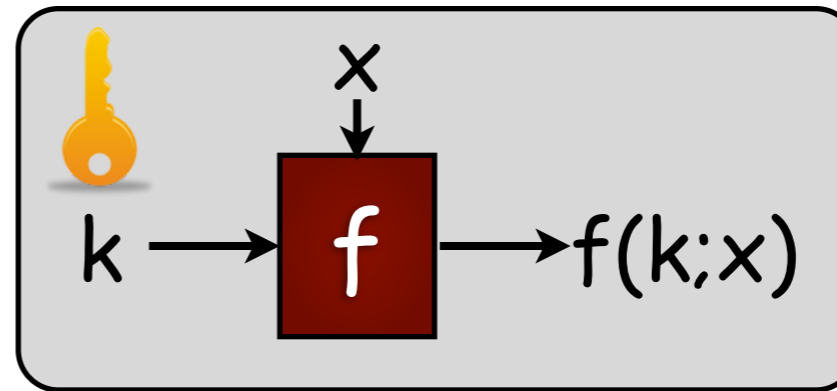
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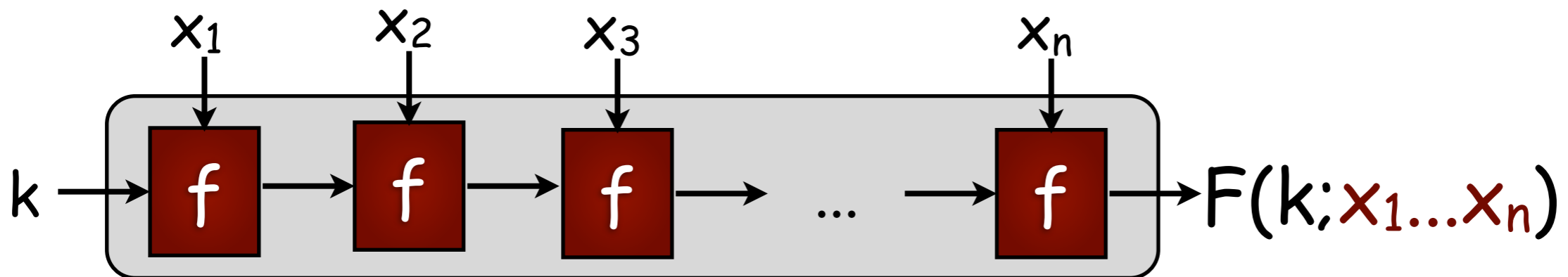


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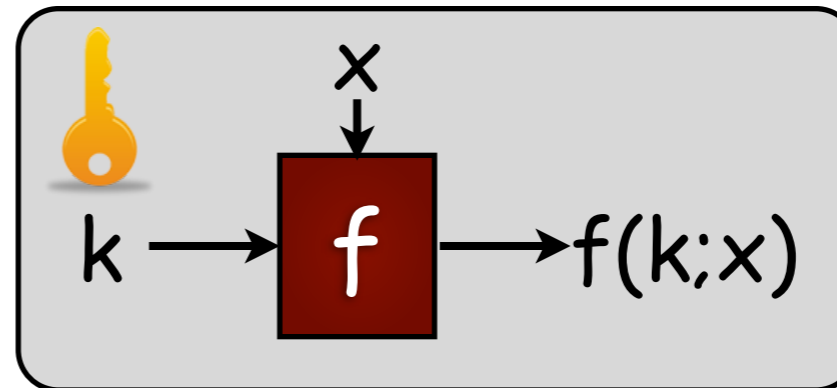
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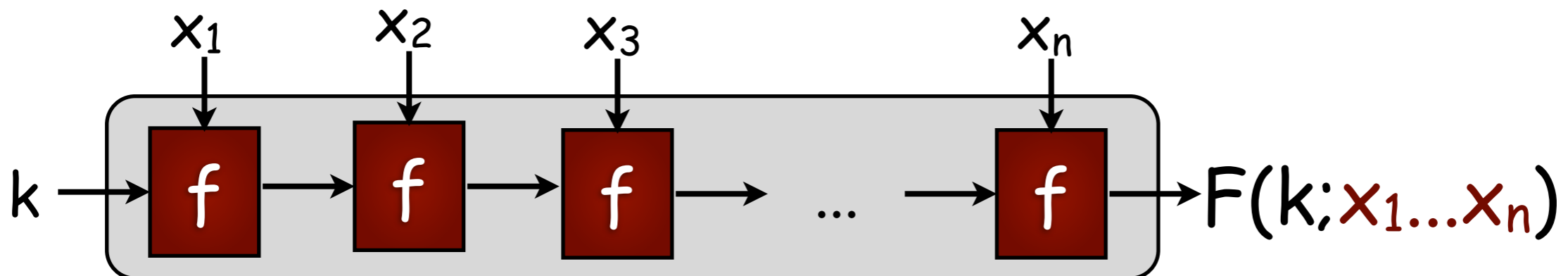


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Generalizes first algebraic construction of PRF by Goldreich-Goldwasser-Micali [GGM '86] from Pseudorandom Generators

Augmented Cascade



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Range of the function smaller than key domain.

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Can extend output using pseudorandom generators; but breaks the *algebraic structure*

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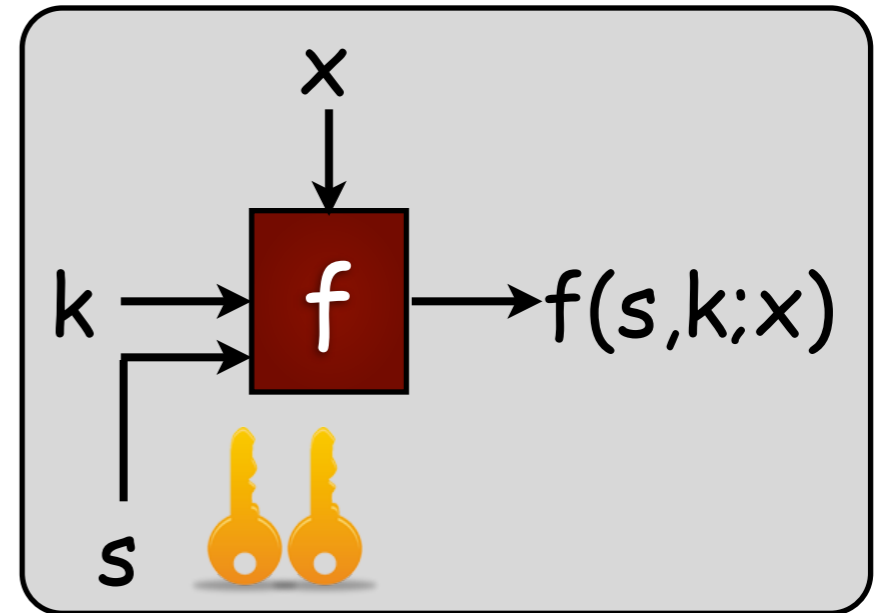
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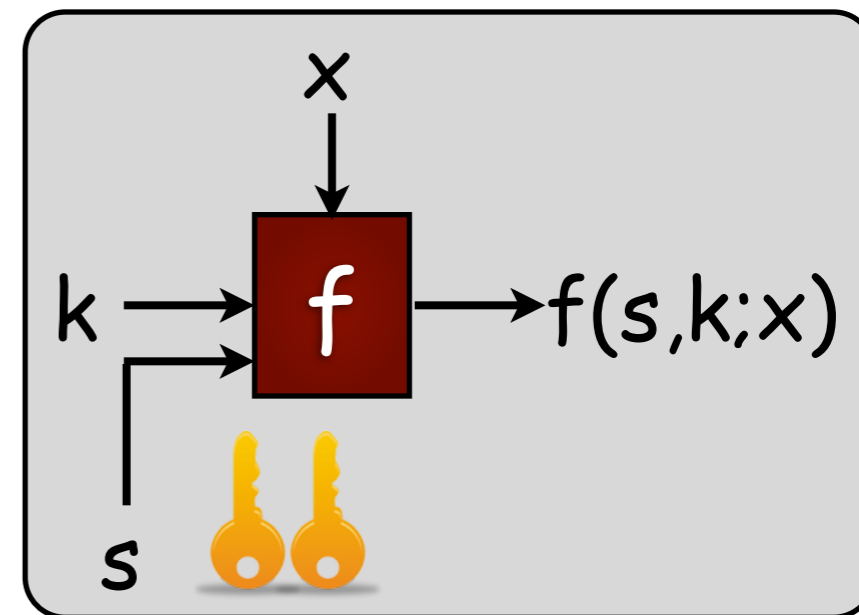
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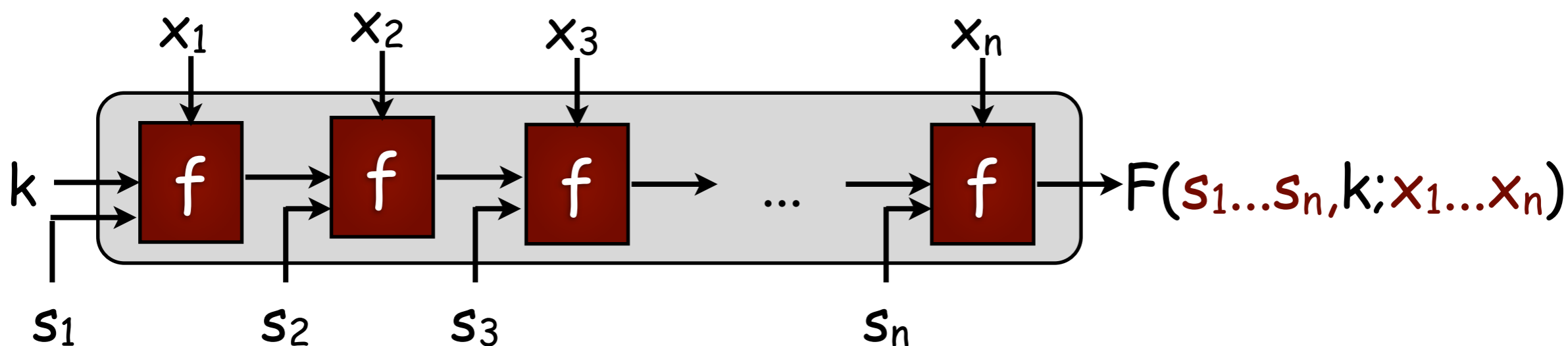
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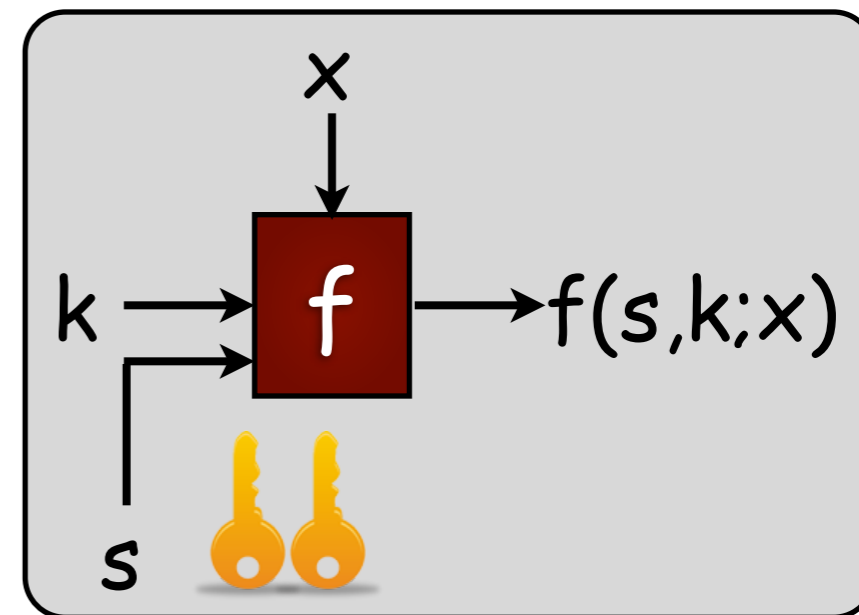
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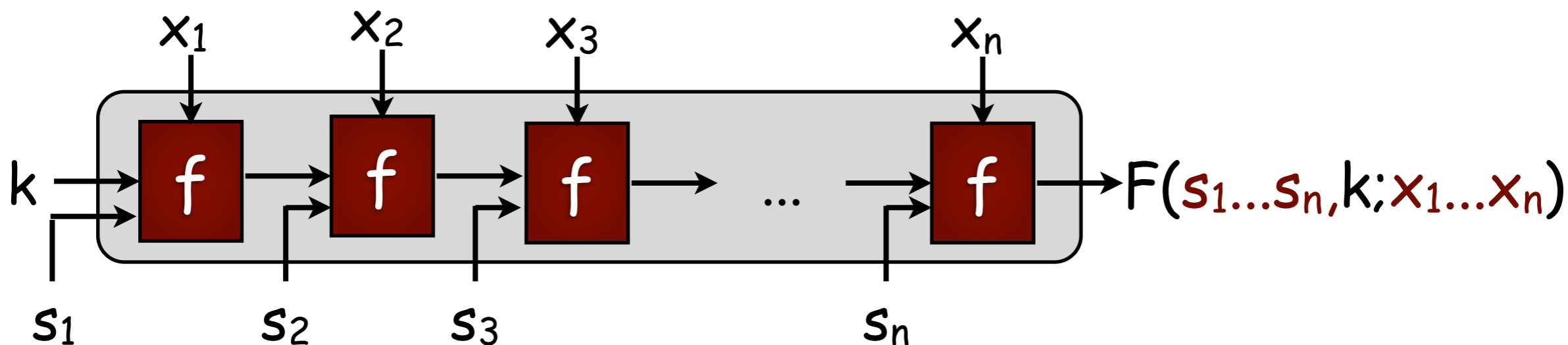
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Augmented Cascade:



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Is Augmented Cascade secure?



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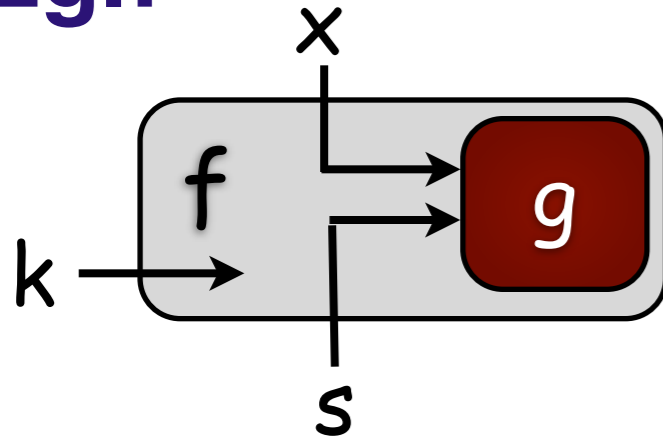
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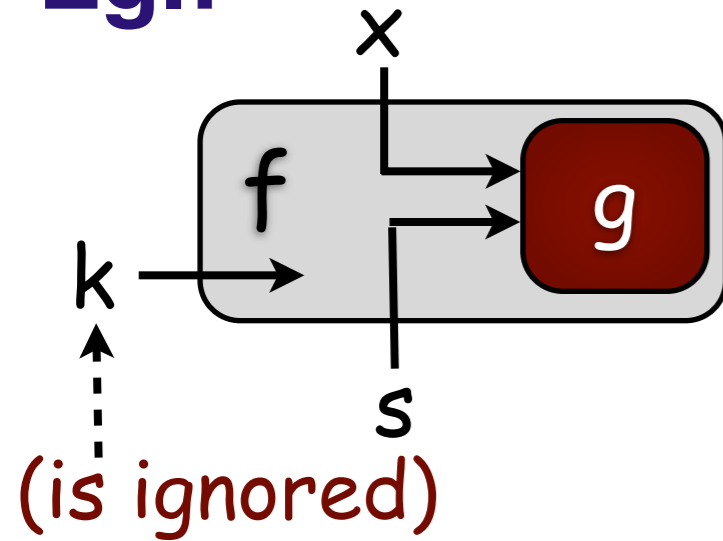


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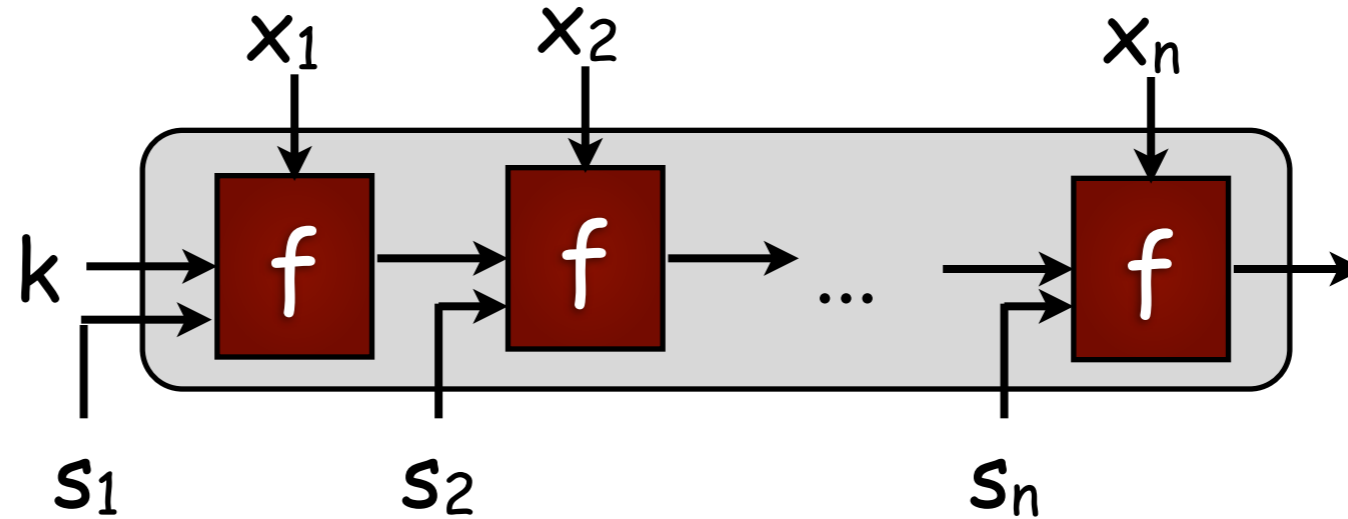
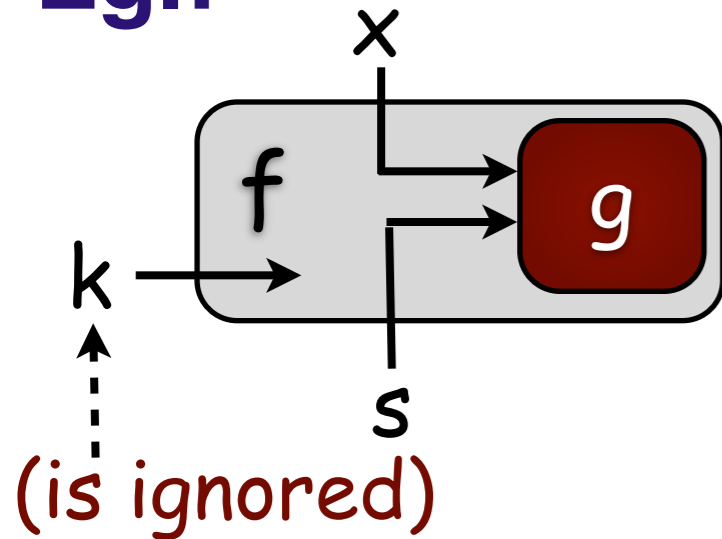


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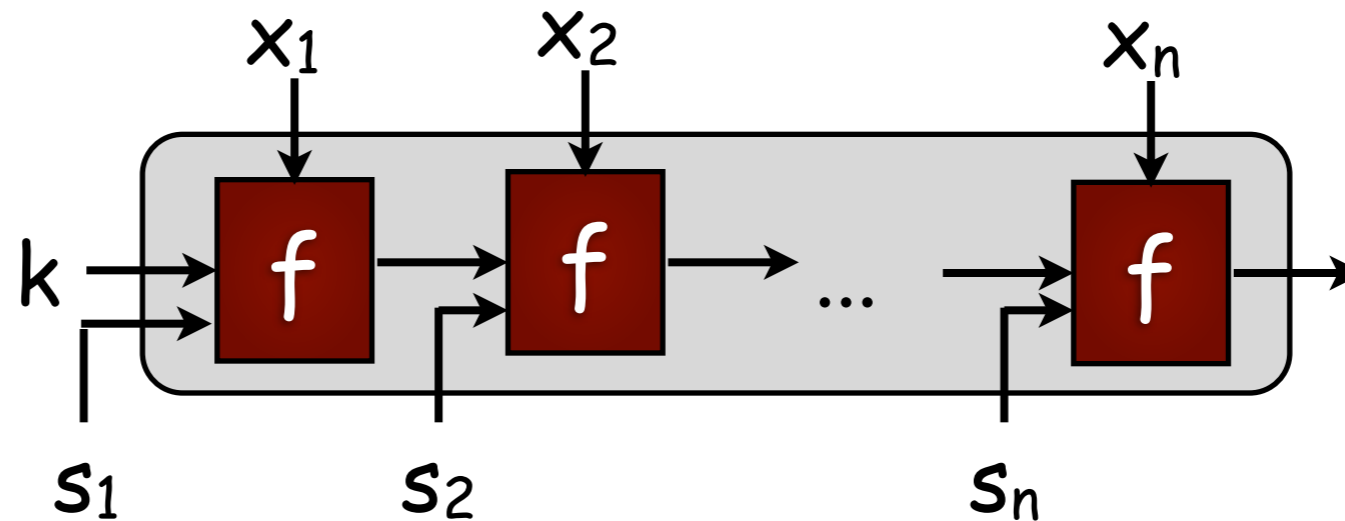
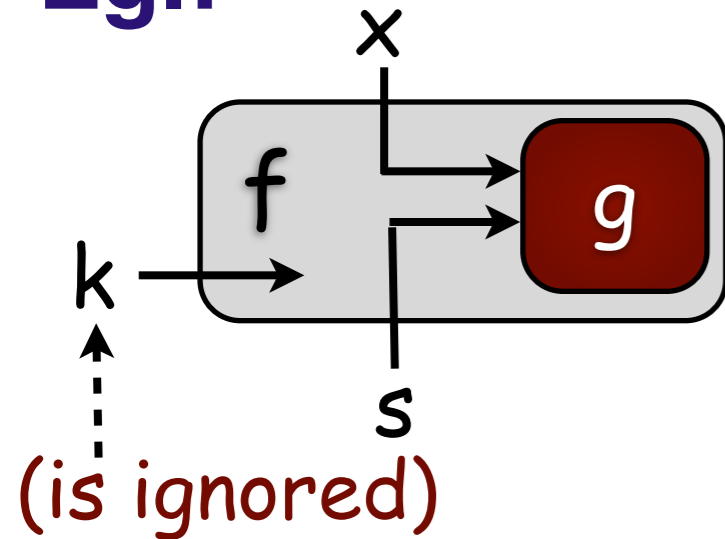


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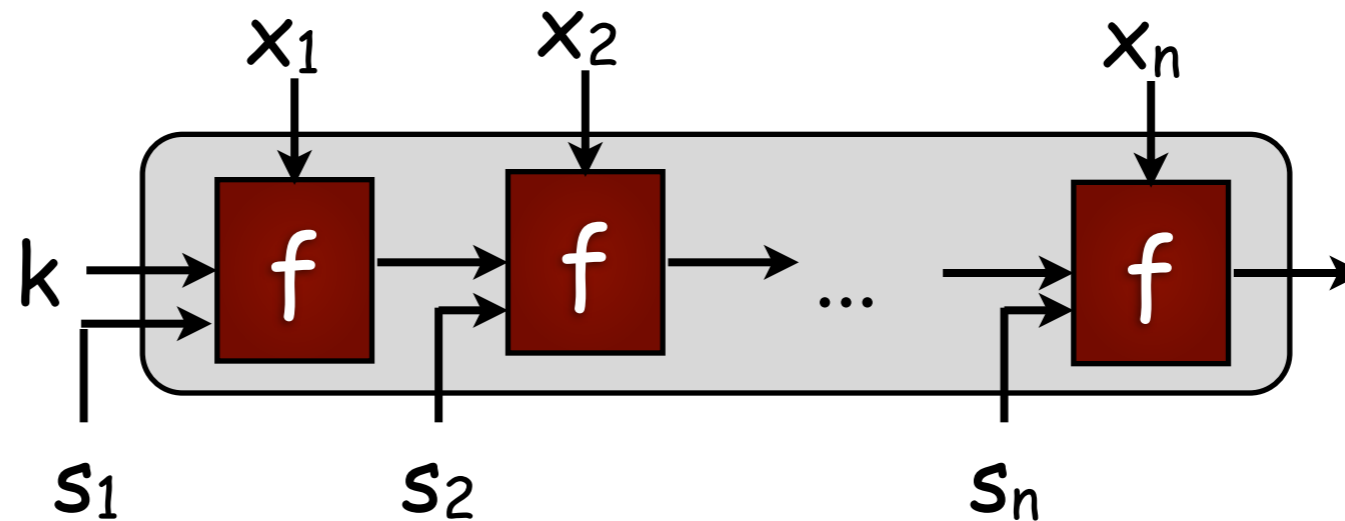
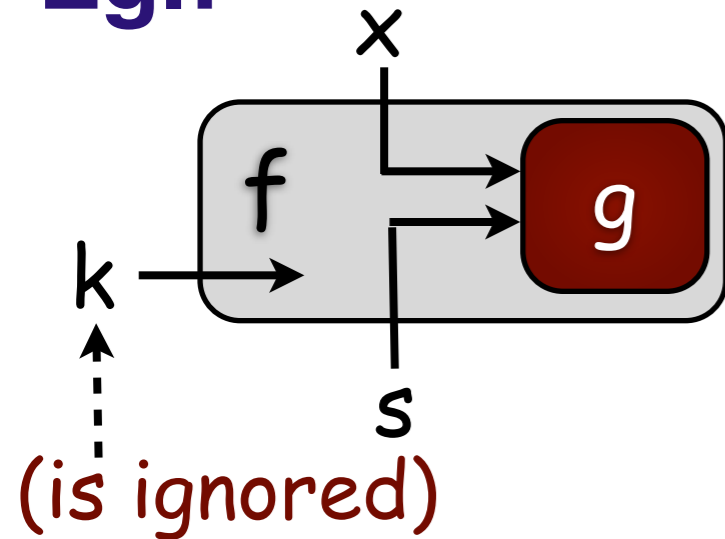
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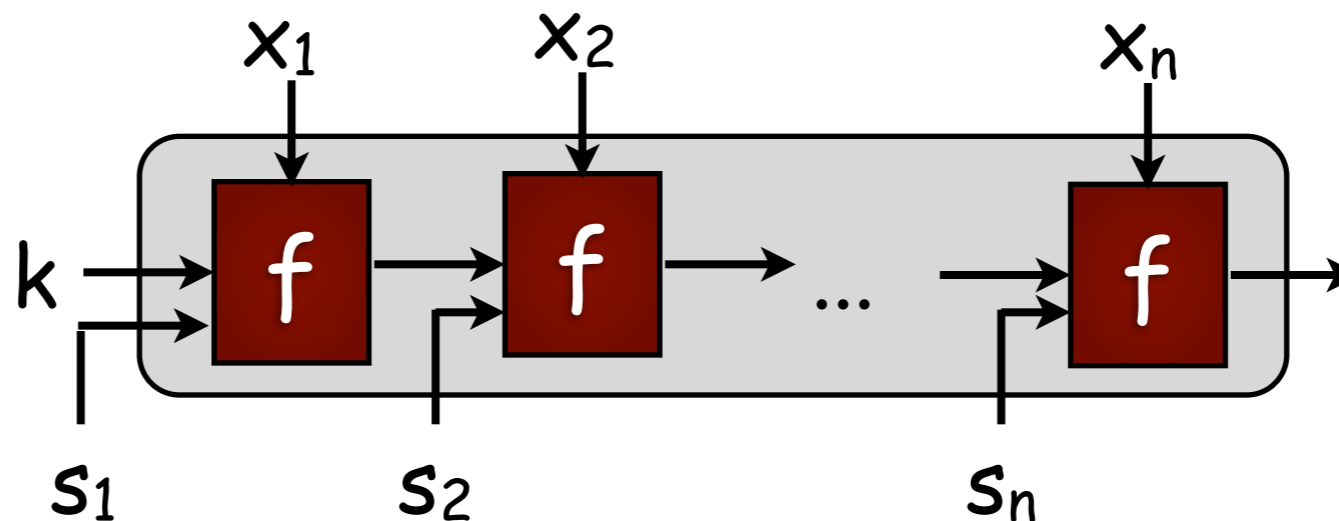
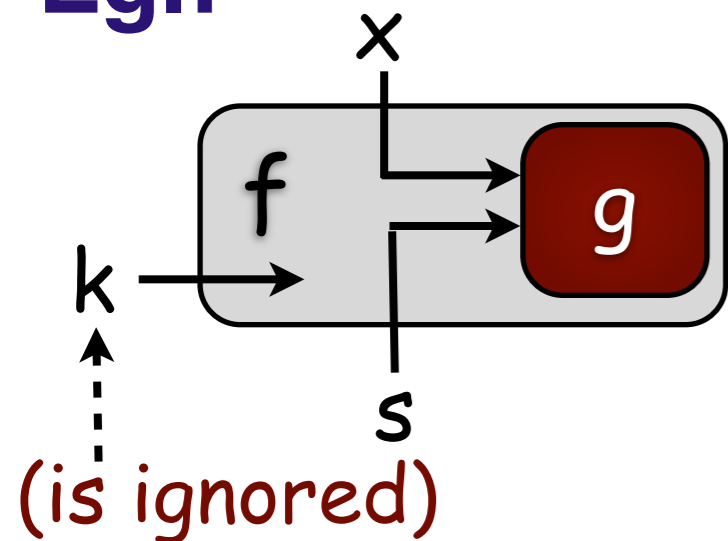


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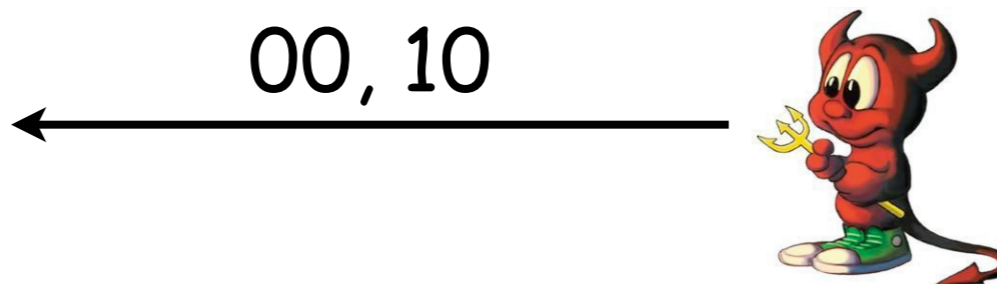
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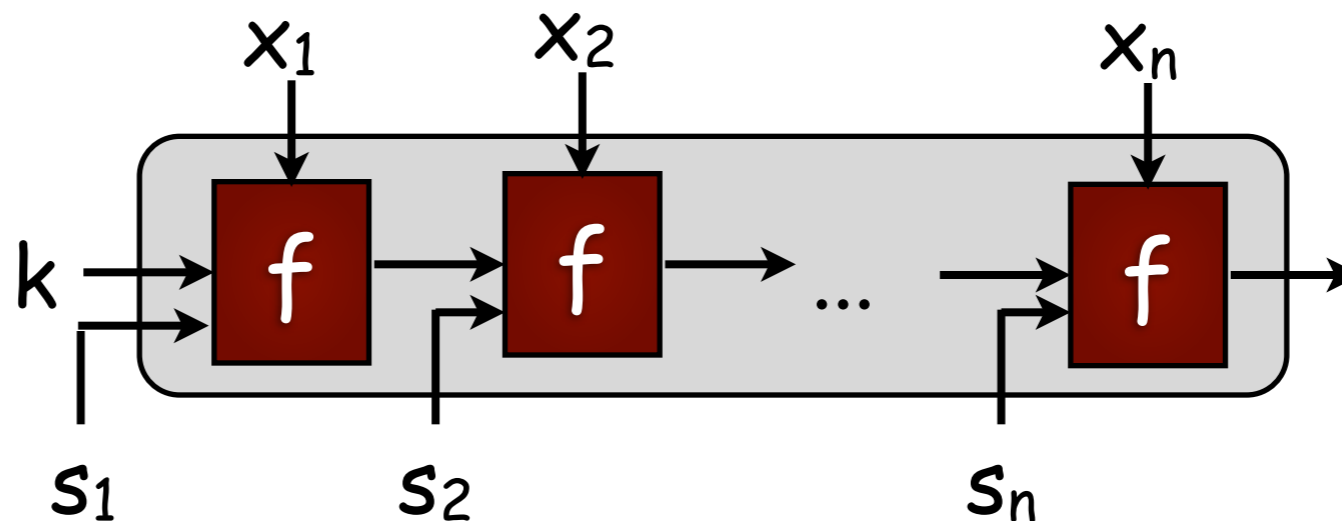
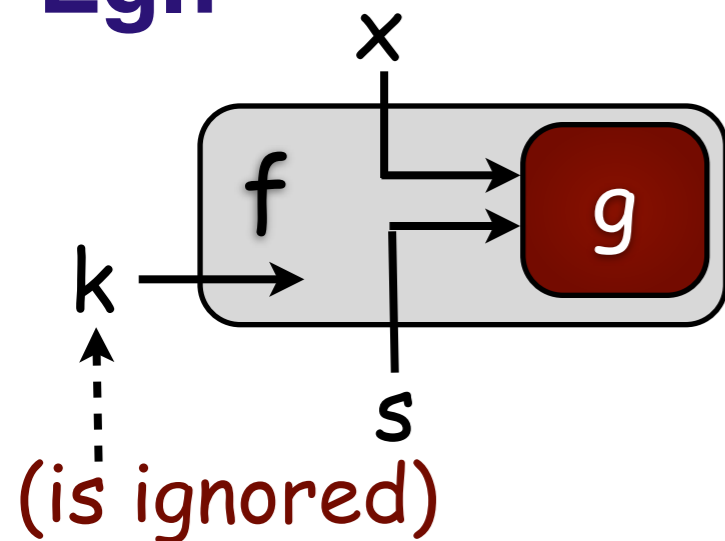


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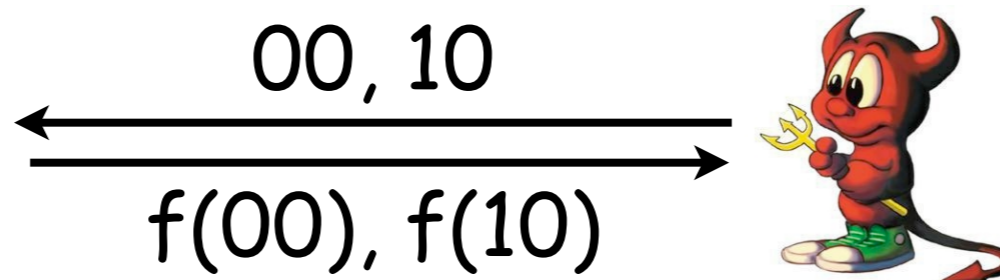
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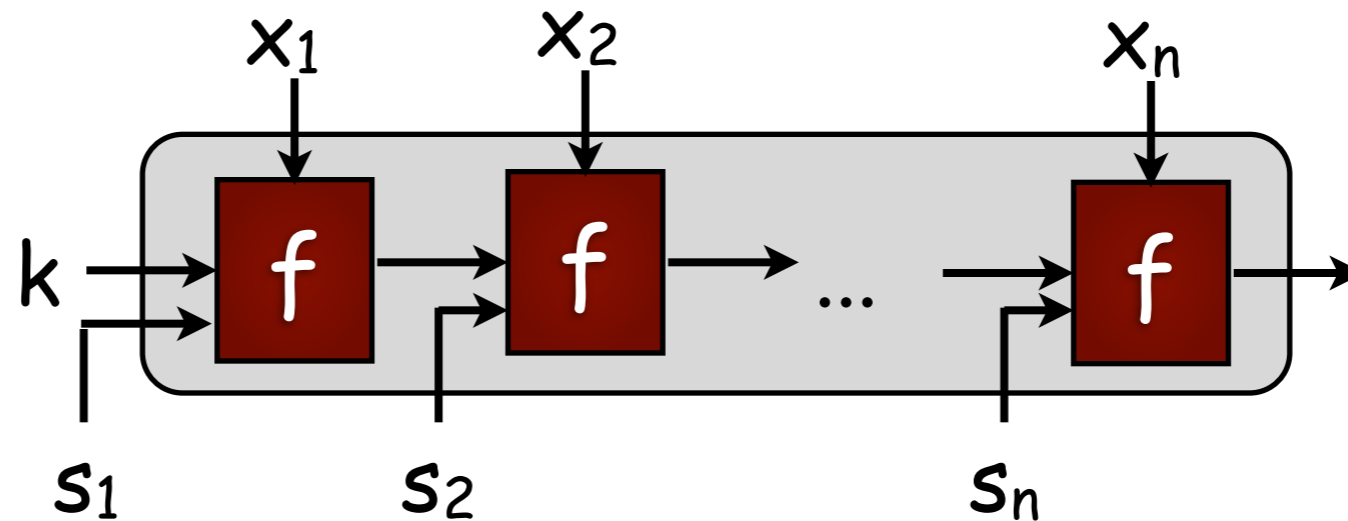
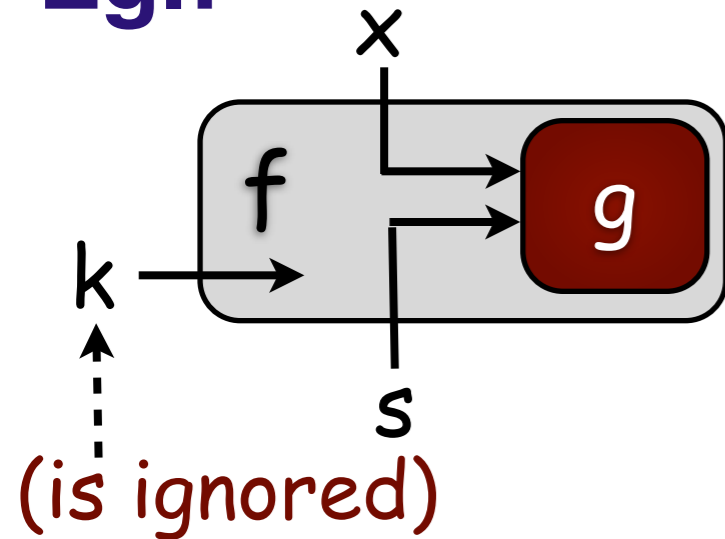


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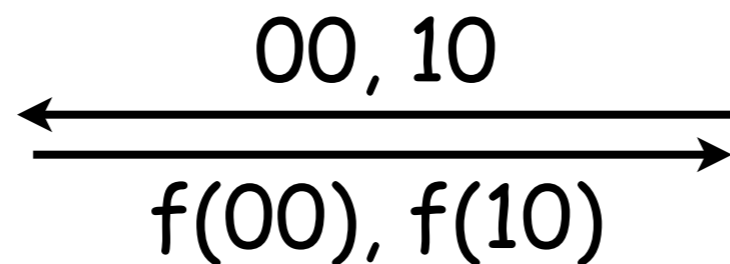
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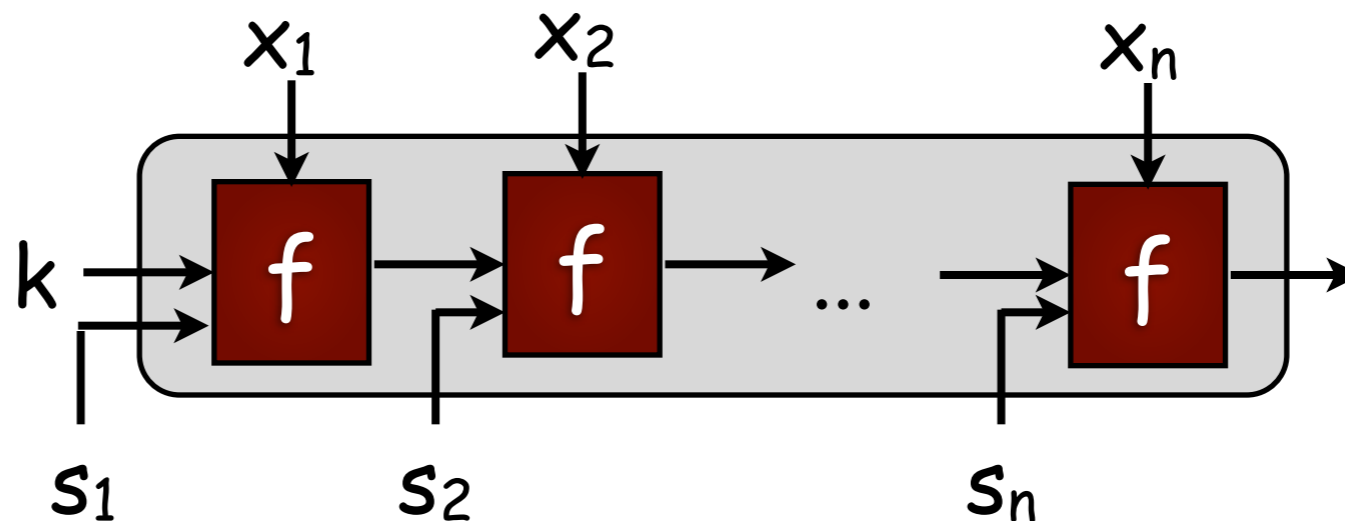
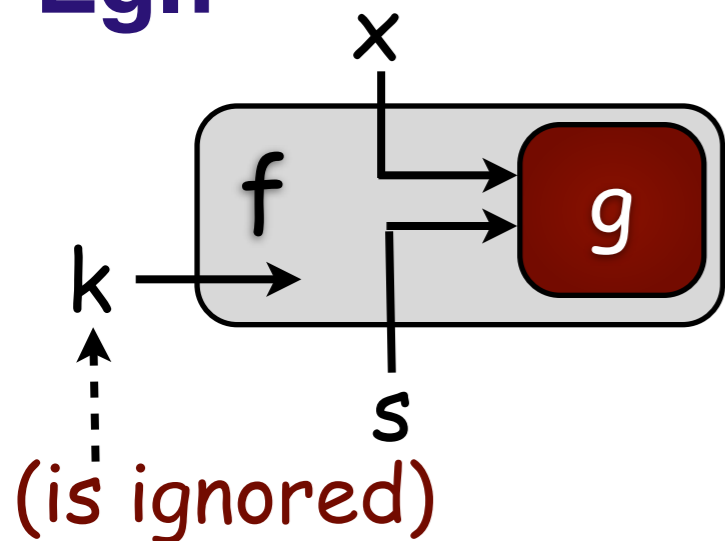
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output "PRF"

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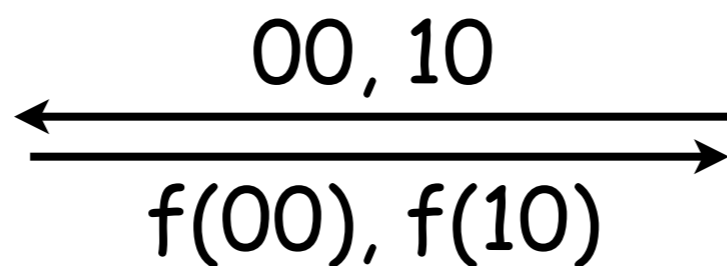
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If $f(00) = f(10)$
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$f(00) = f(10)$ for random f with very low probability

Therefore, F is not a secure PRF!

Parallel Composition Security



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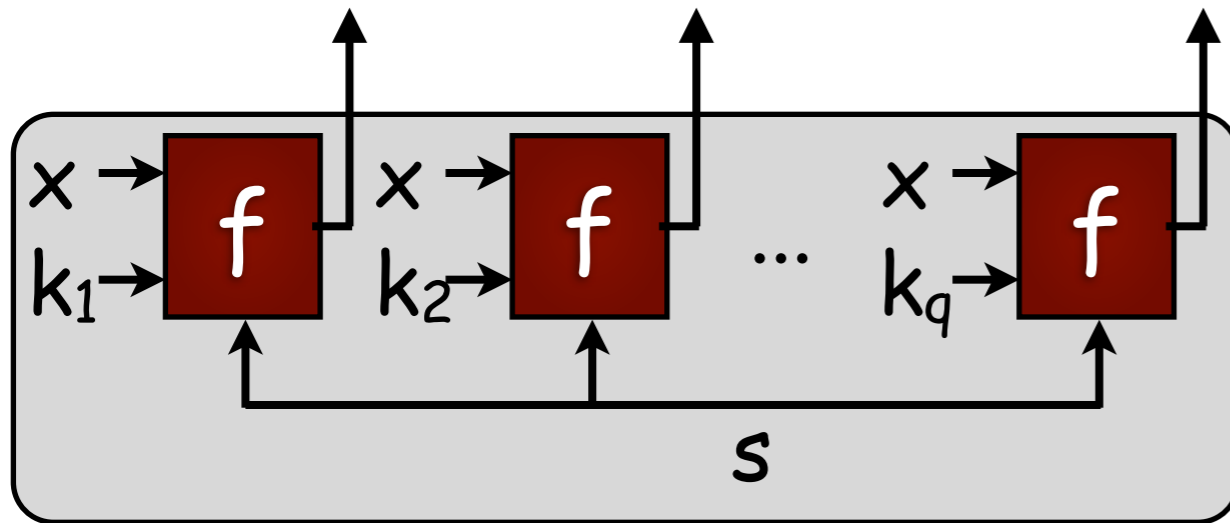


Consider q related keys $(s, k_1), \dots, (s, k_q)$

Parallel Composition Security



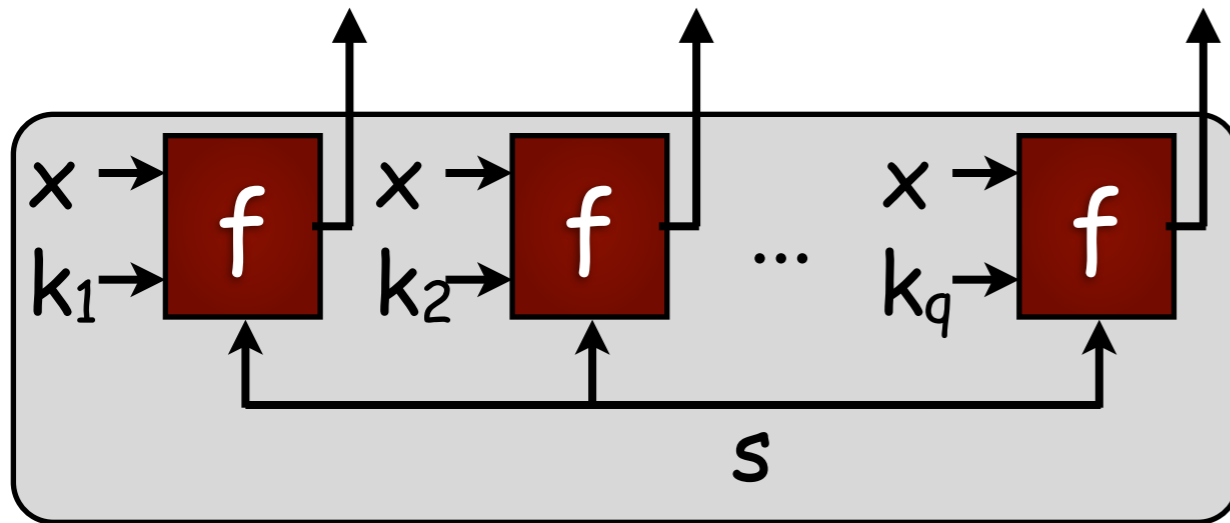
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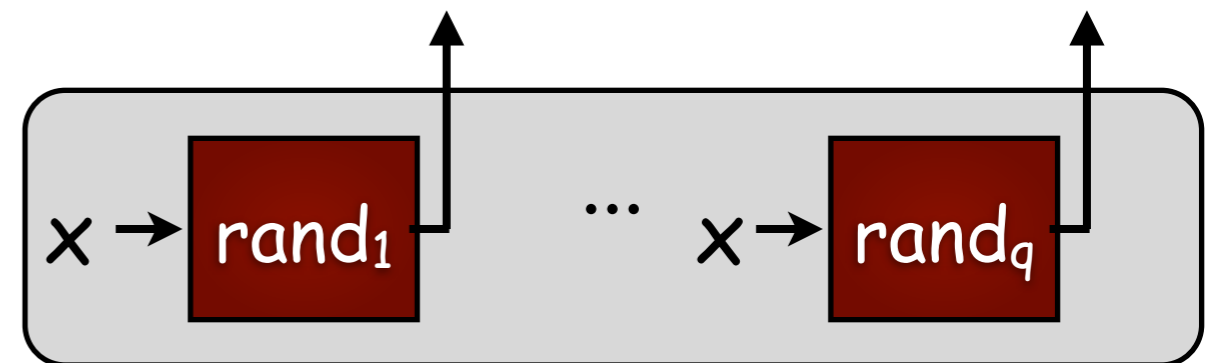
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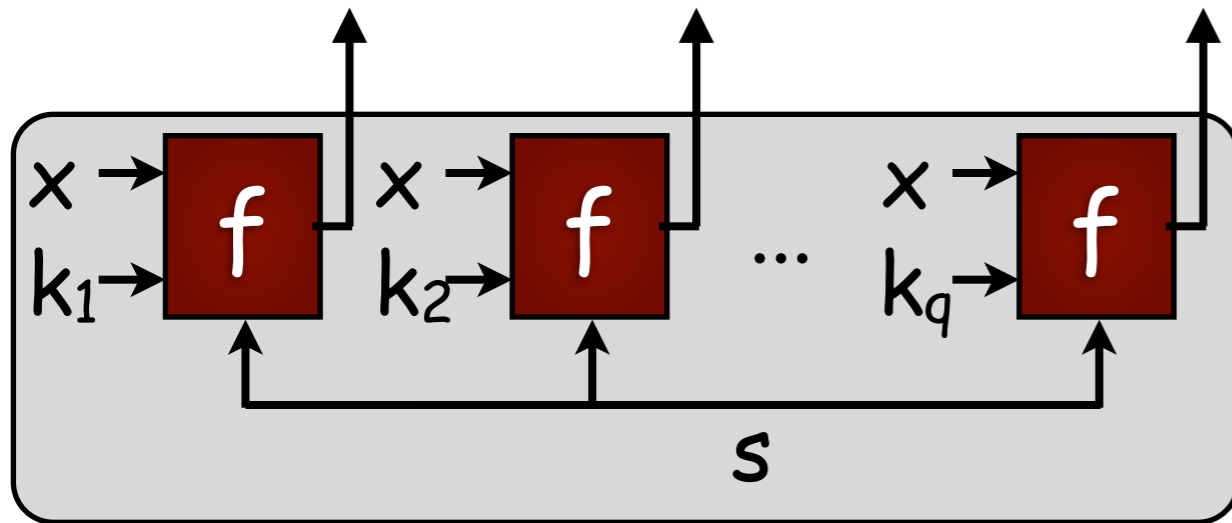
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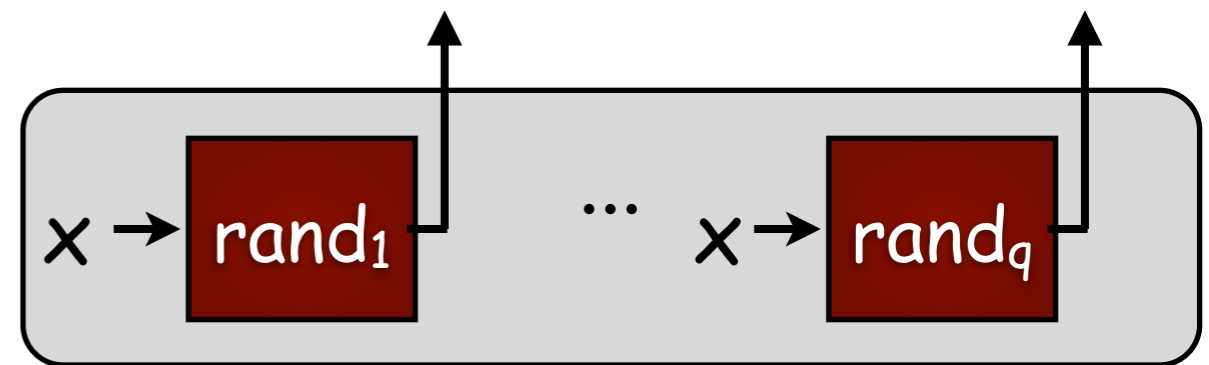


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In other words:
"Simultaneously Secure"

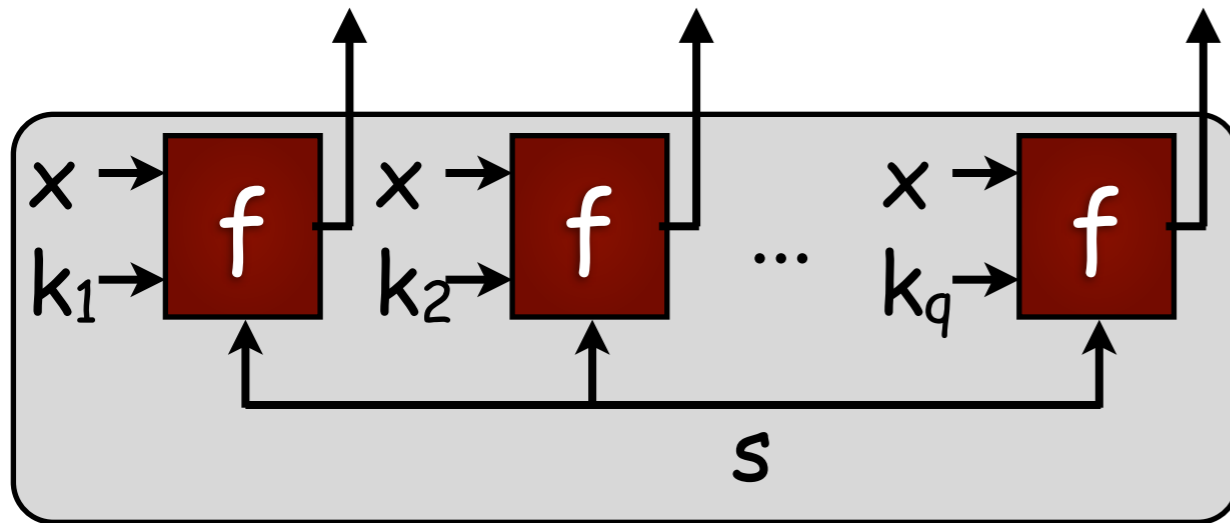
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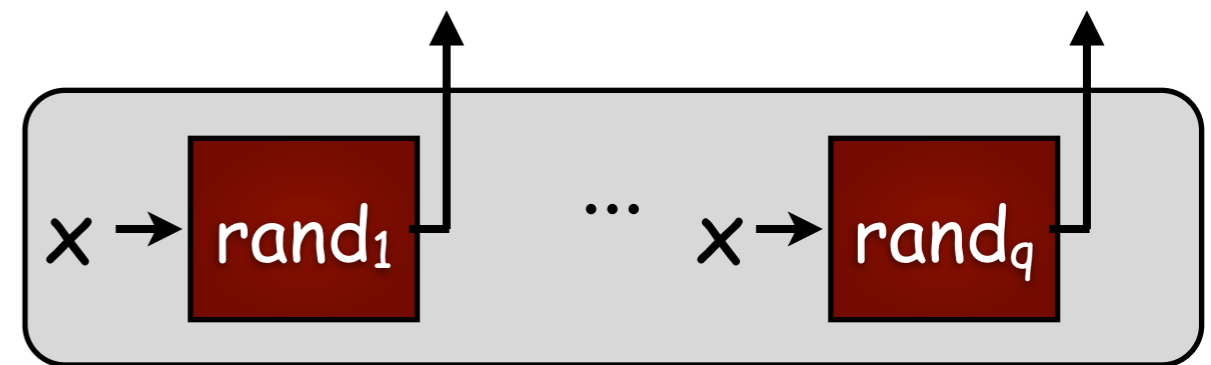
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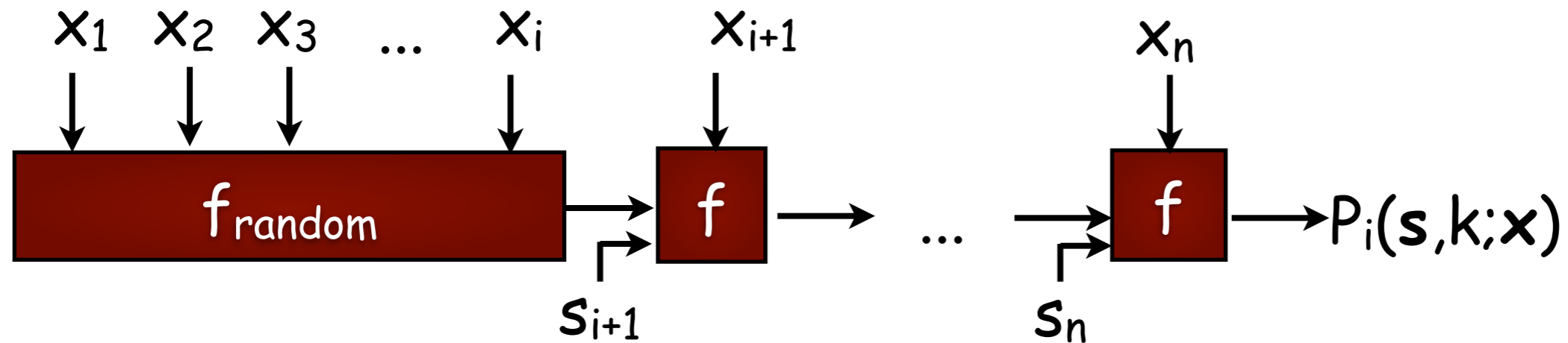
Theorem

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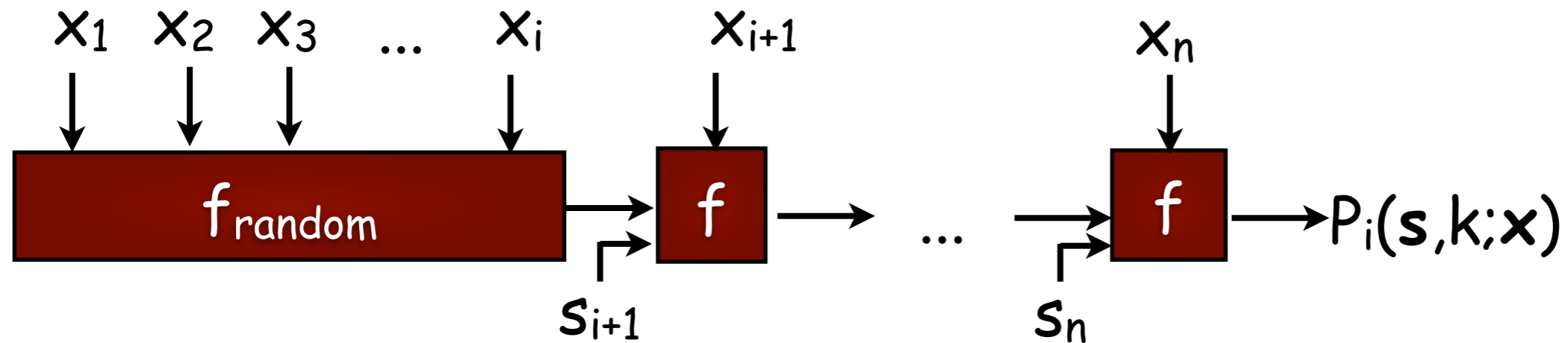
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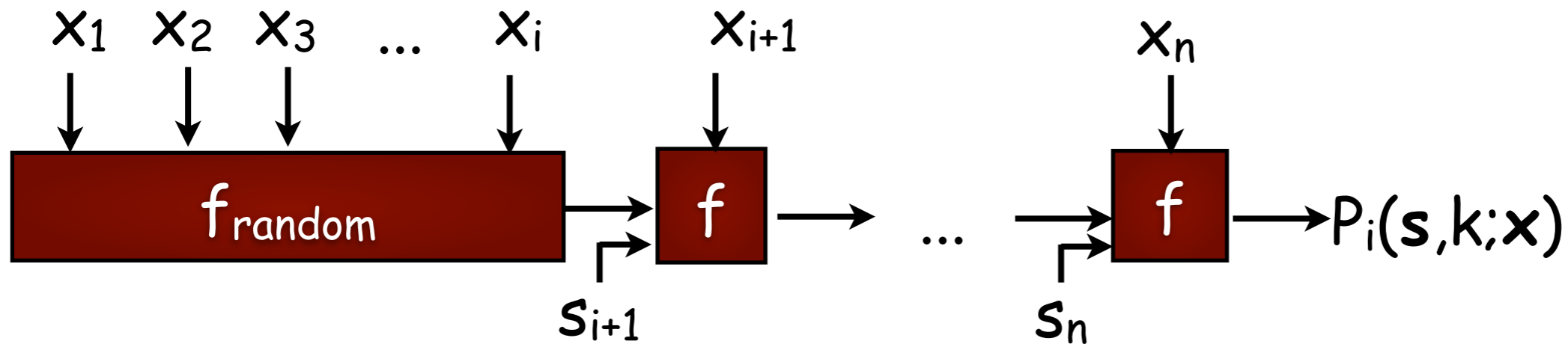


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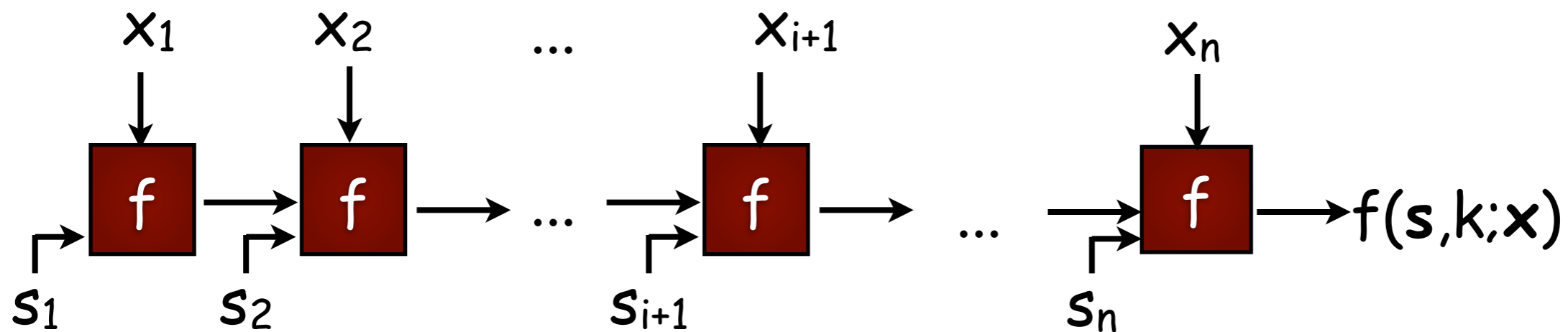


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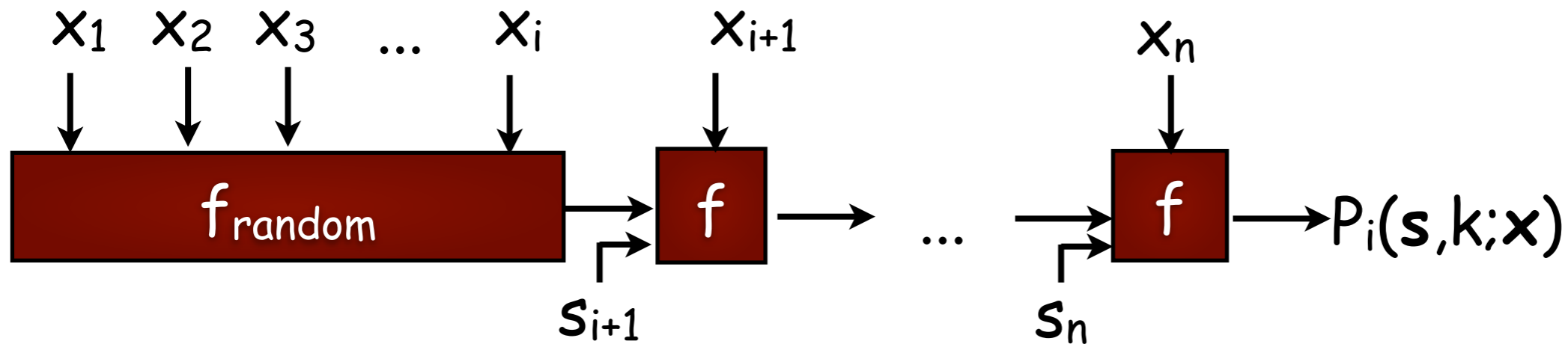
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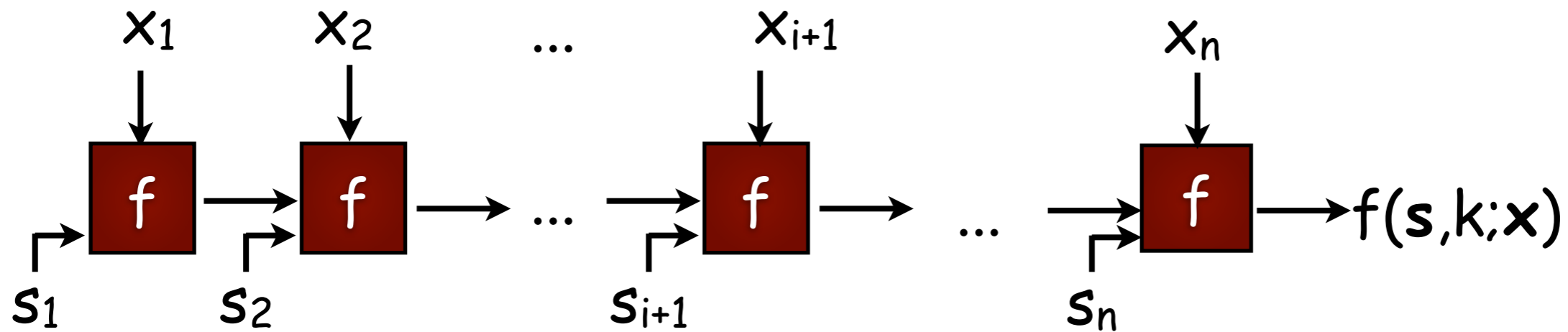
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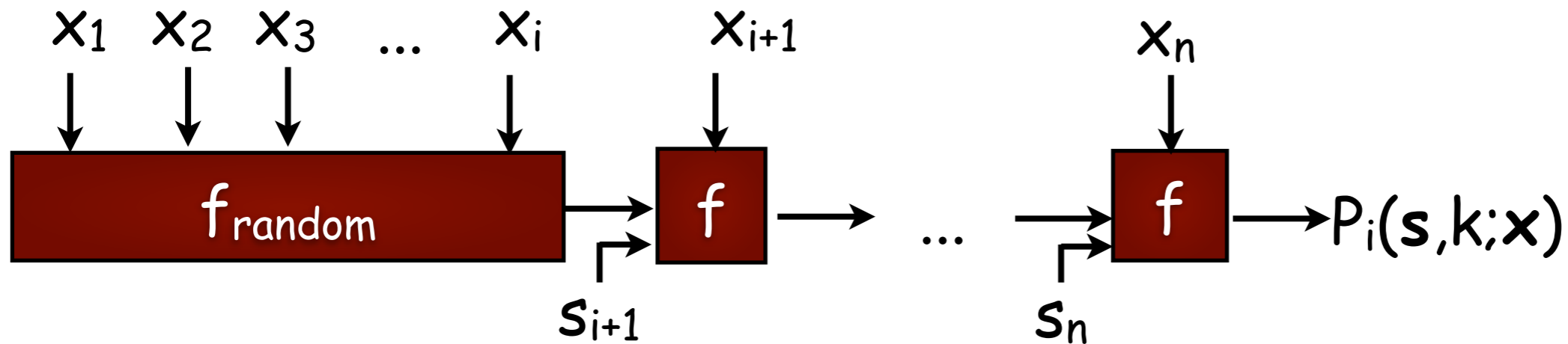


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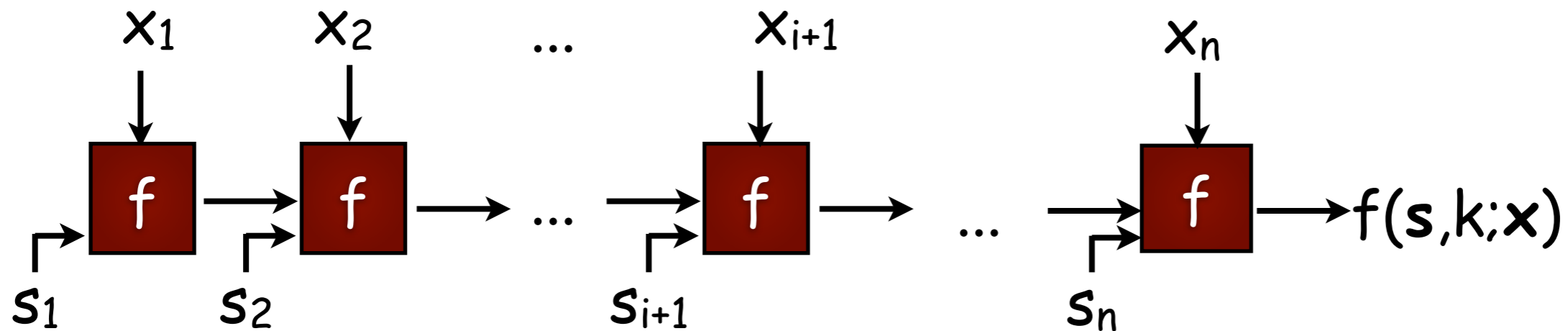


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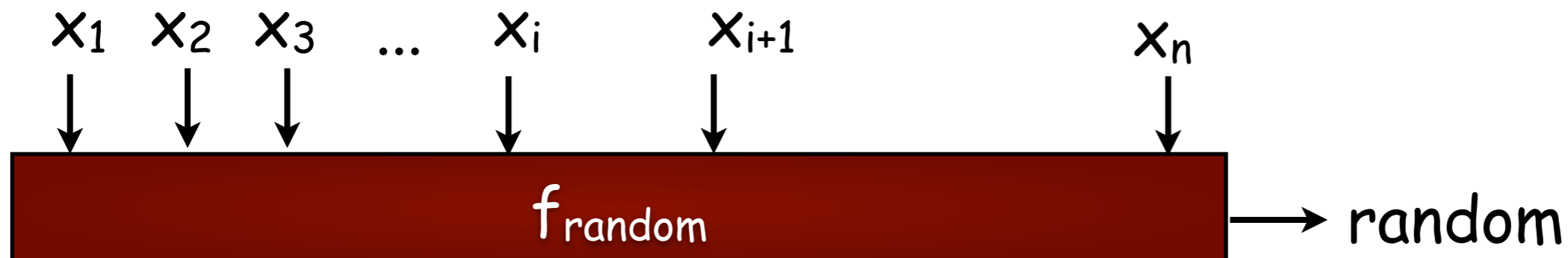
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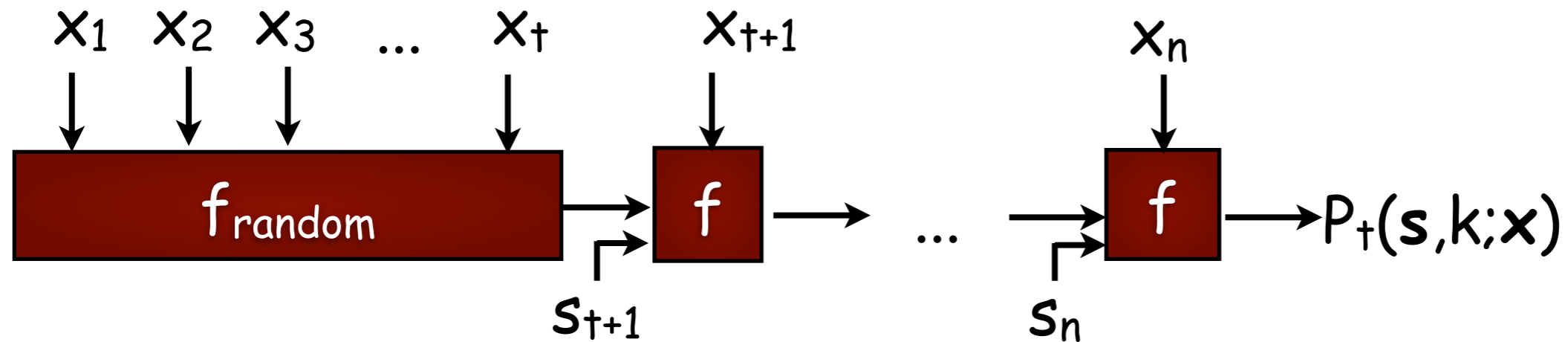
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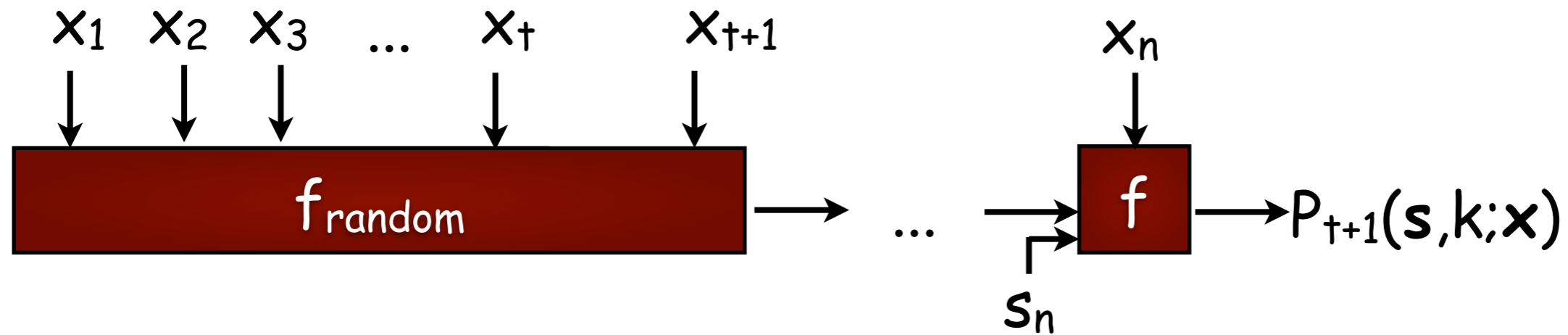
Finally:



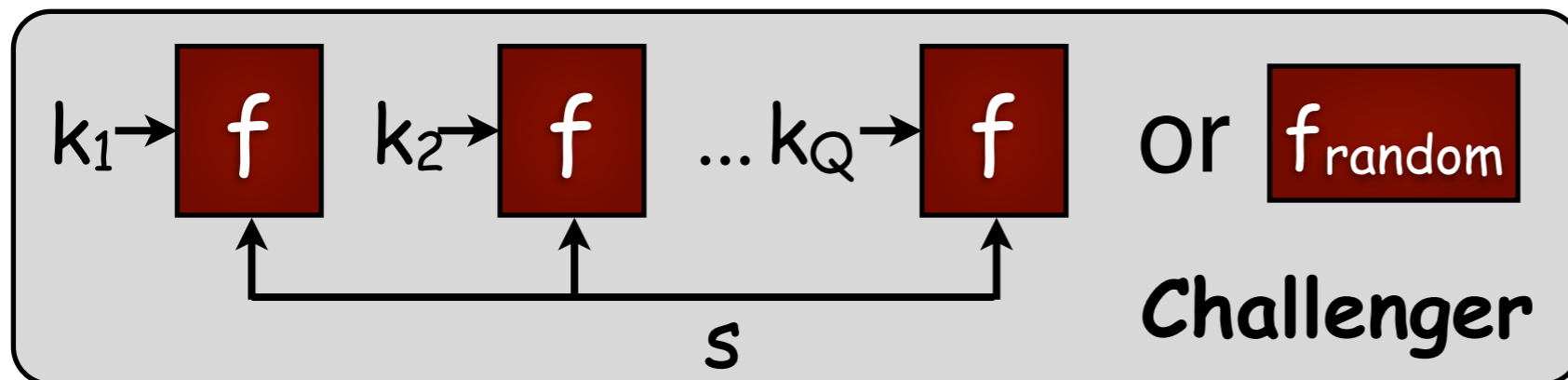
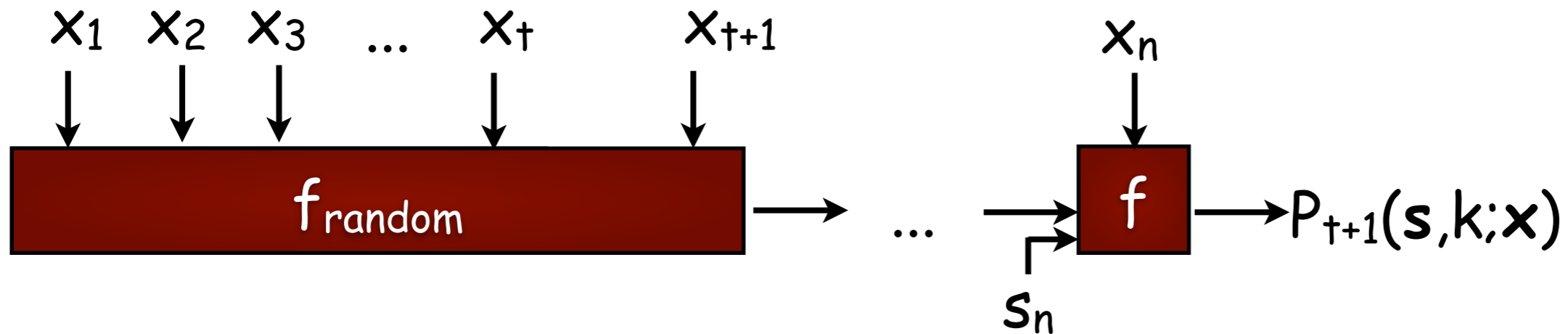
Proof Outline



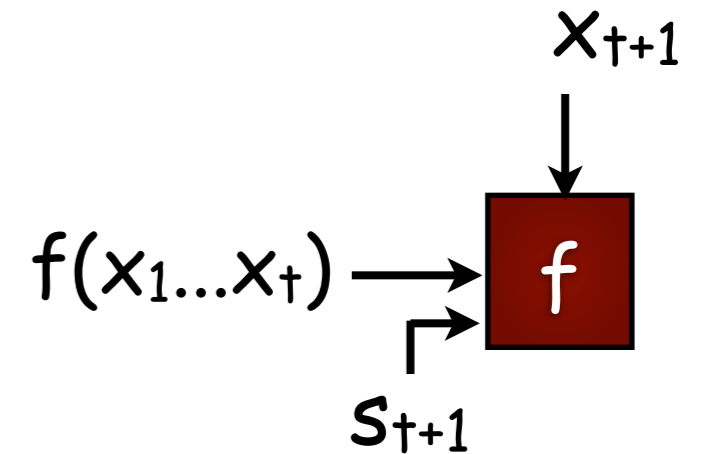
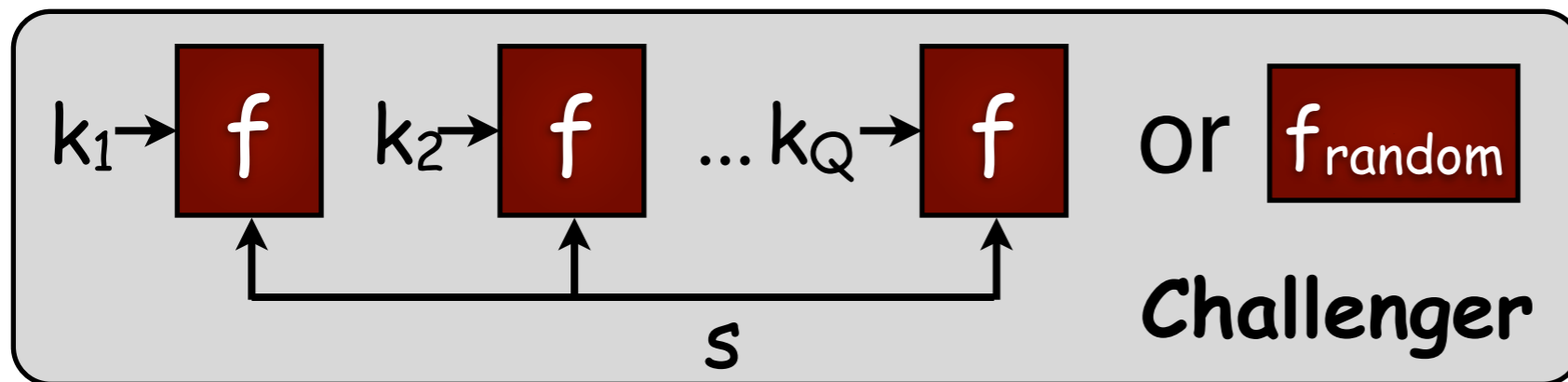
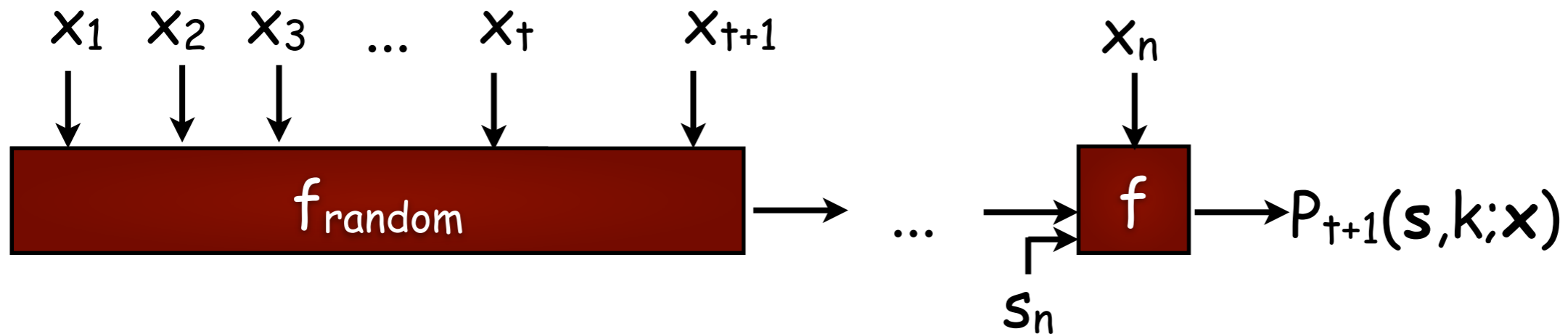
Proof Outline



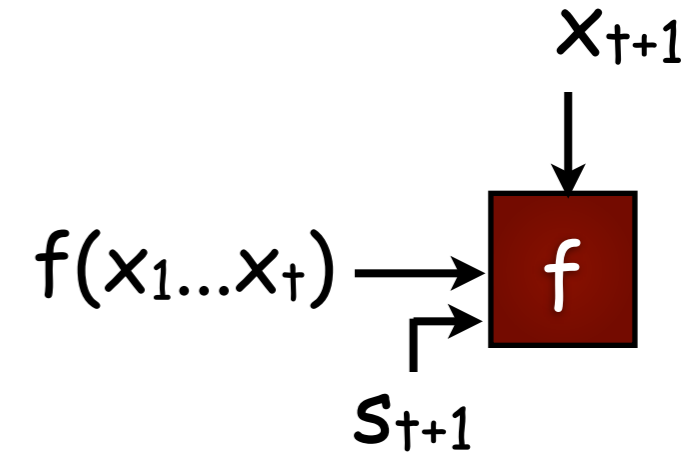
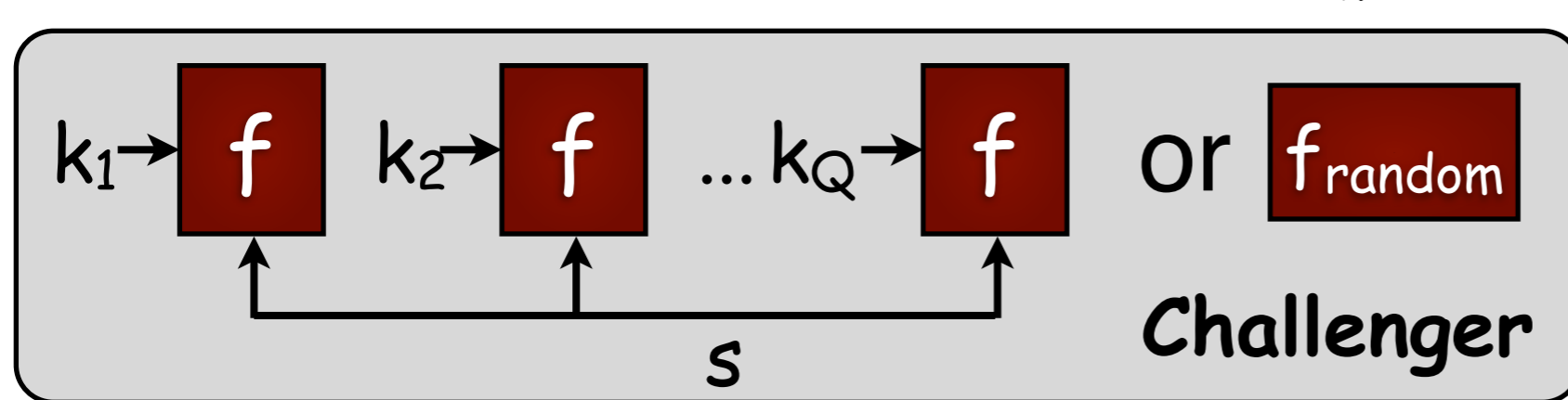
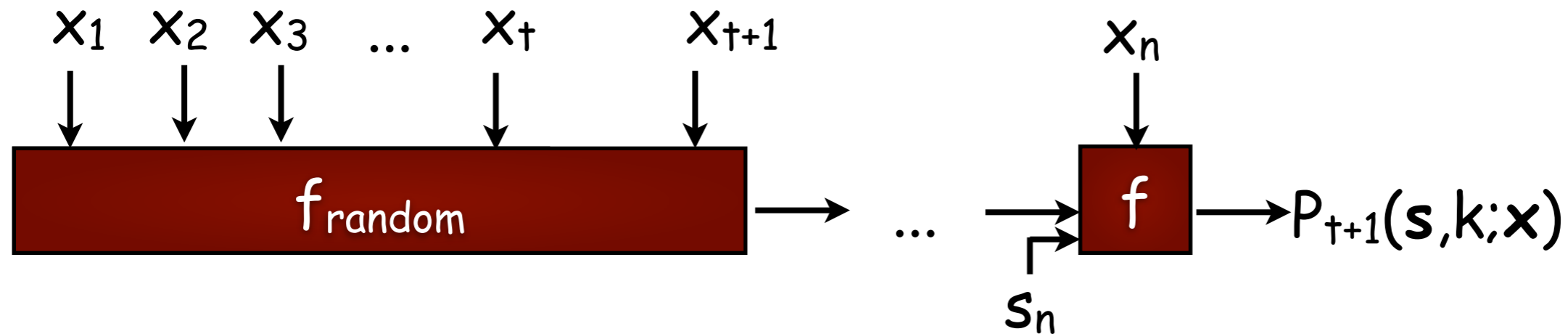
Proof Outline



Proof Outline



Proof Outline



s_{t+1} is set to s

Depending on $x_1 \dots x_t$ we choose the value of $f(x_1 \dots x_t)$ to be some key k_j - maintained in an associative table

Easy to see: We simulate either P_t or P_{t+1} depending upon Challenger

Why Augmented Cascade?



Why Augmented Cascade?

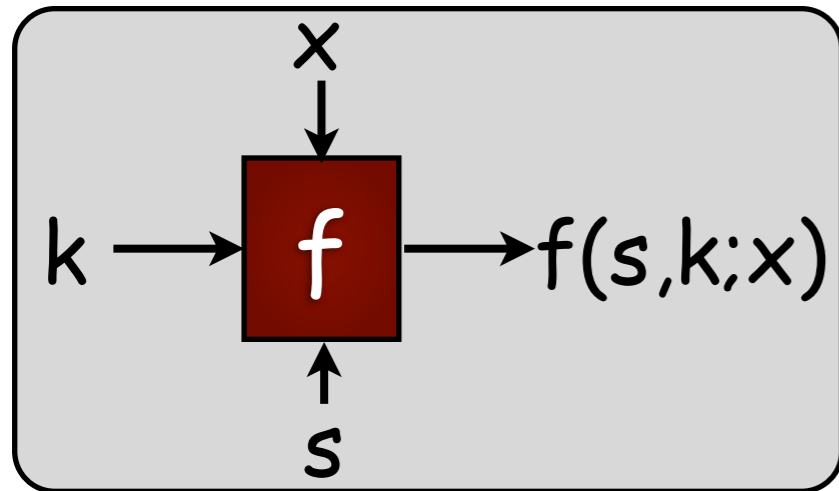


- Generic tool to build efficient algebraic PRFs

Why Augmented Cascade?



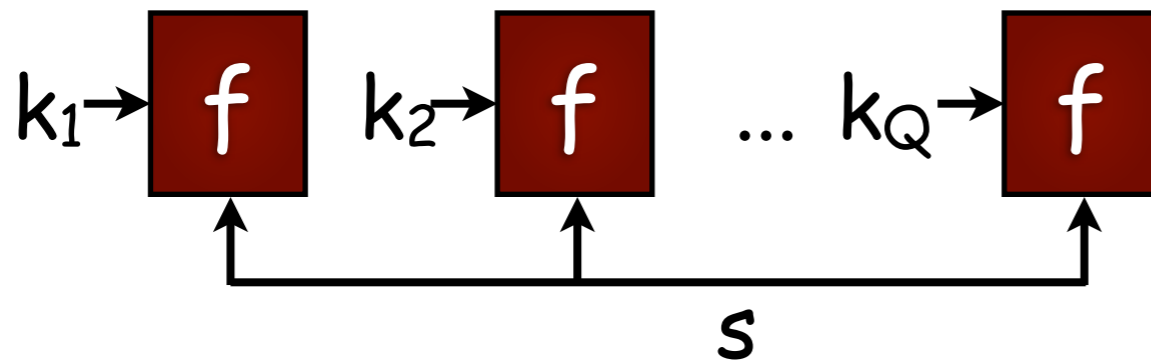
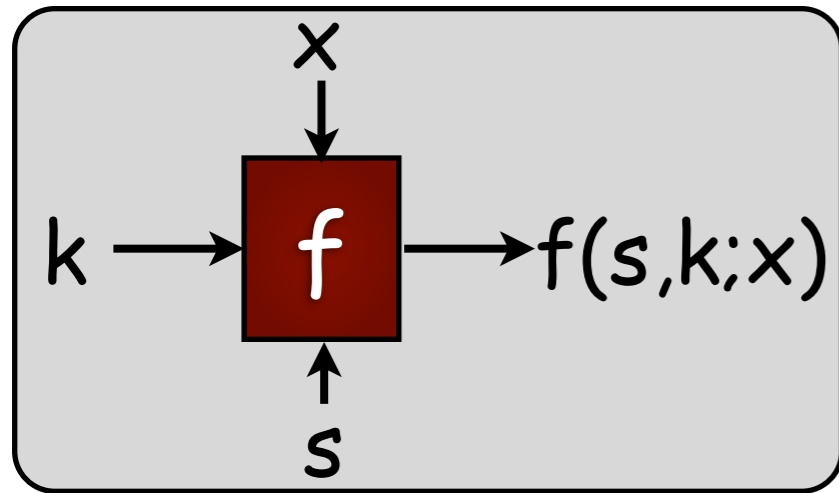
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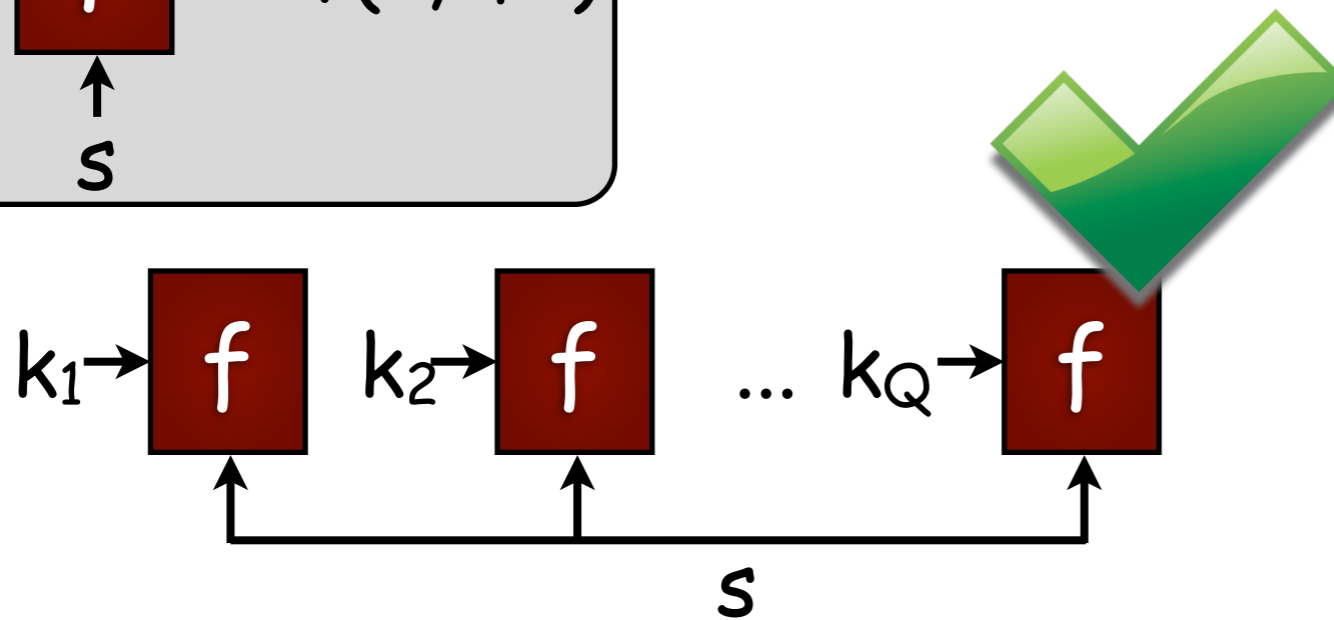
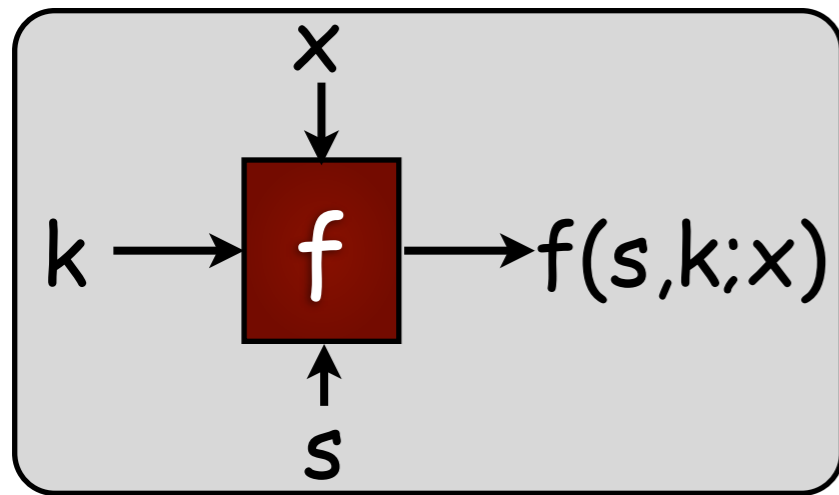
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Why Augmented Cascade?



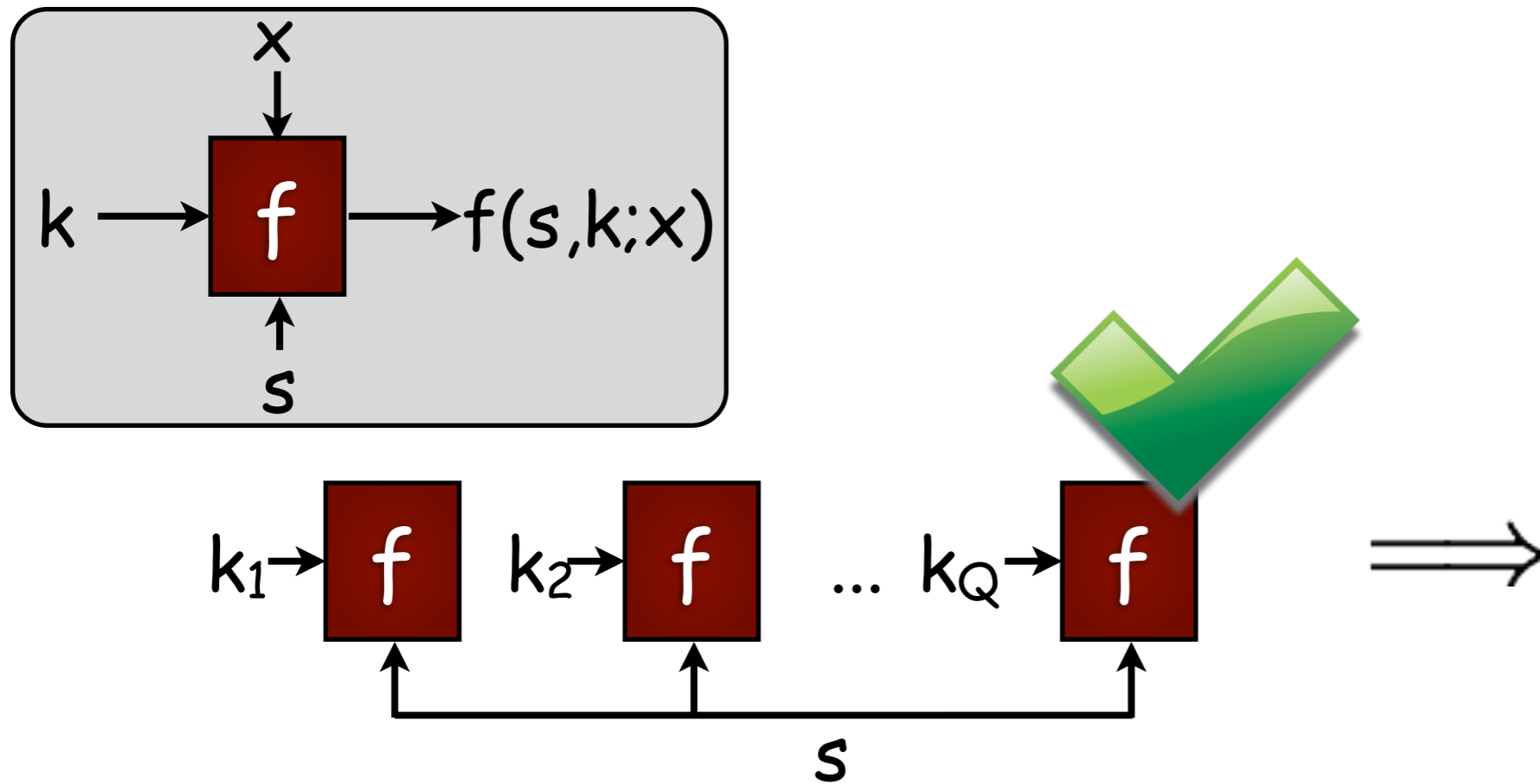
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Why Augmented Cascade?



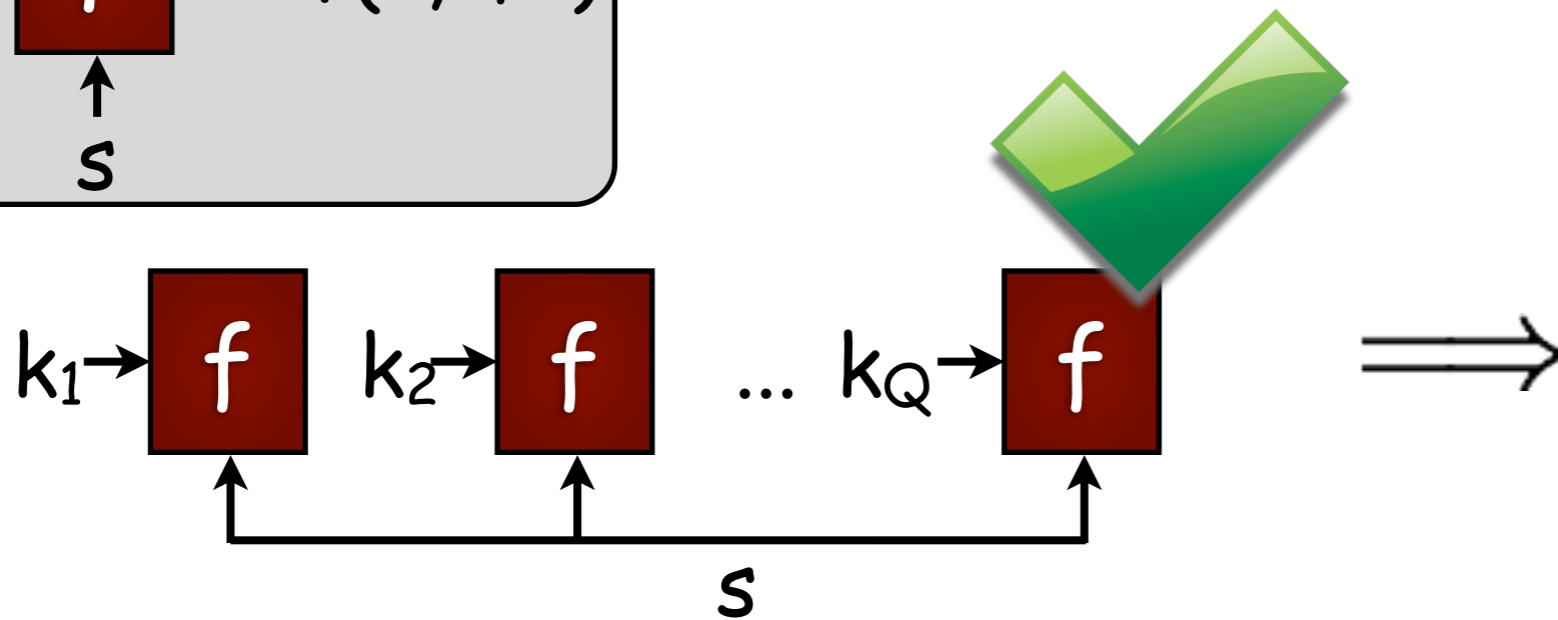
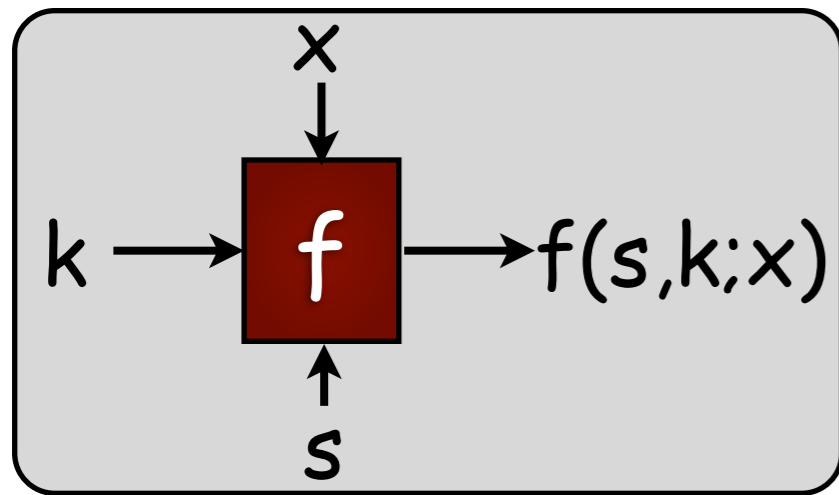
- Generic tool to build efficient algebraic PRFs



Why Augmented Cascade?



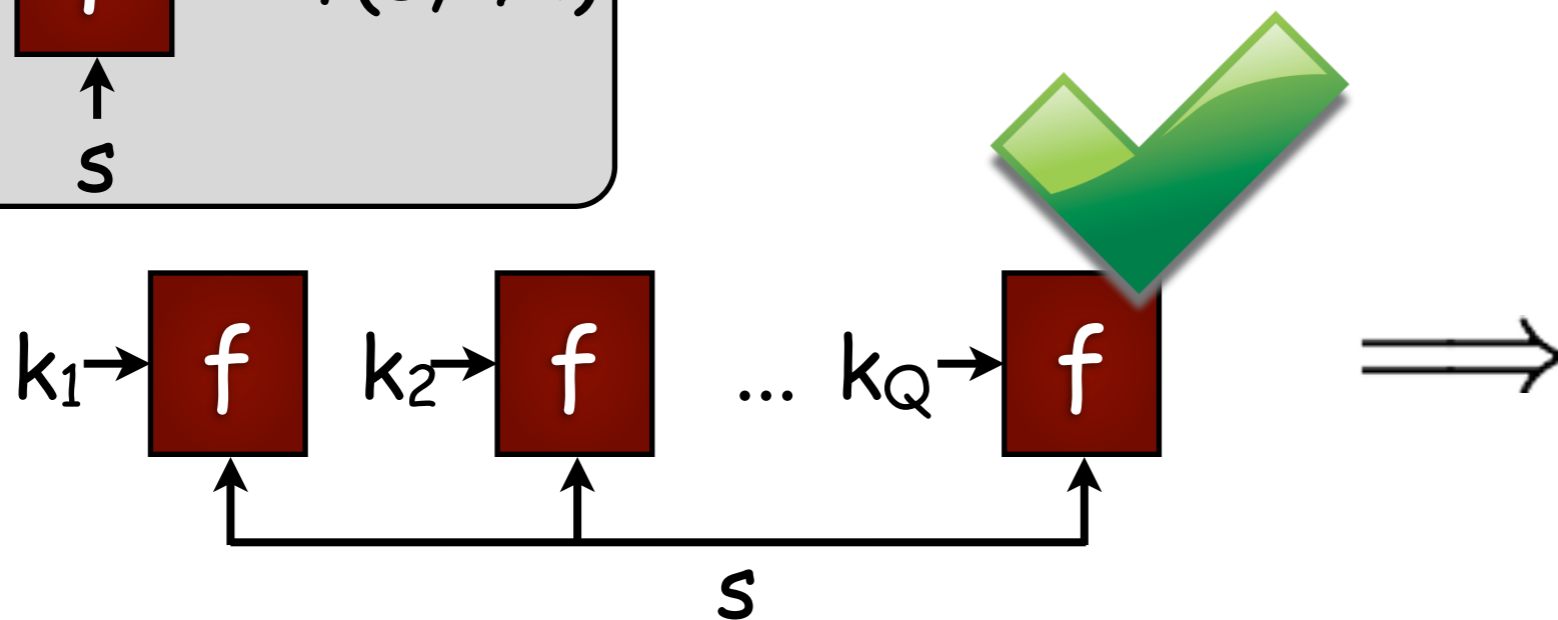
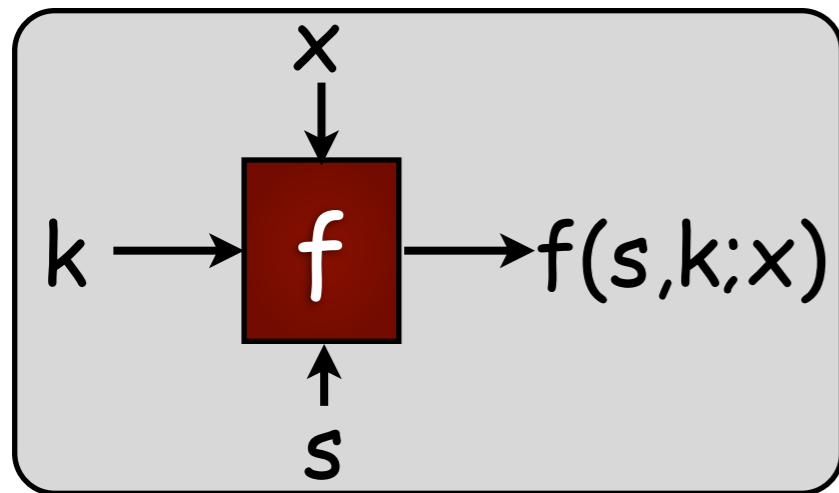
- Generic tool to build efficient algebraic PRFs



Why Augmented Cascade?



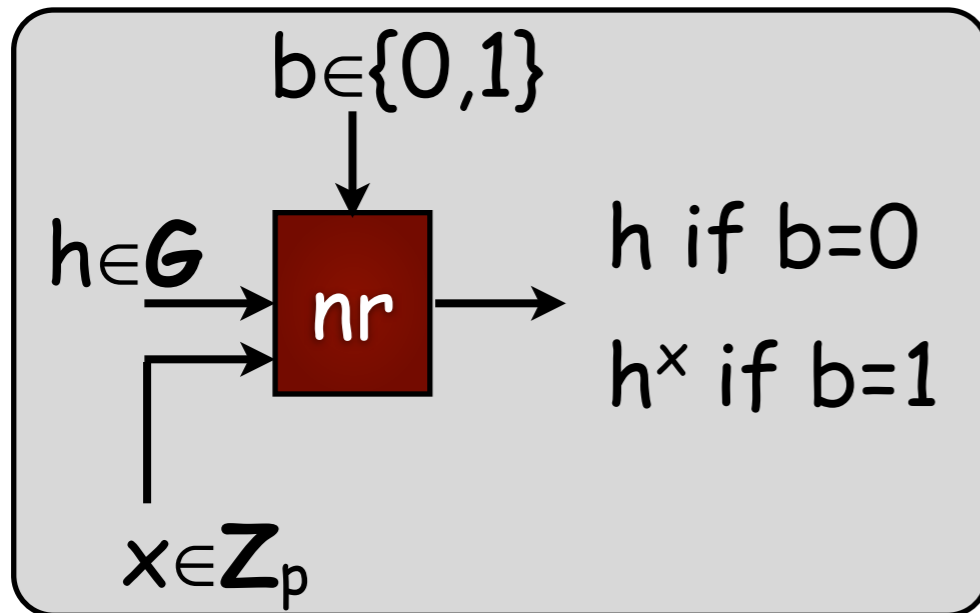
- Generic tool to build **efficient algebraic PRFs**

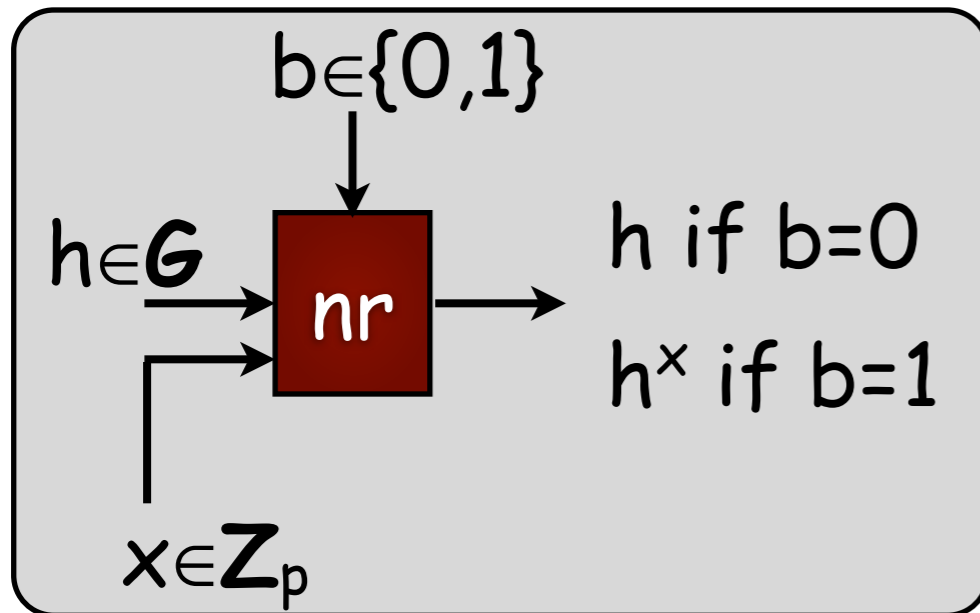


- Simple proofs for existing algebraic PRFs. We show **q -parallel security** of:
Naor-Reingold [FOCS '97] & Lewko-Waters [CCS '09]

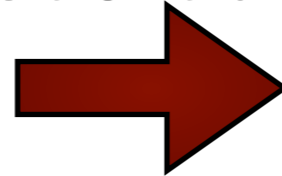
Naor-Reingold [FOCS '97]



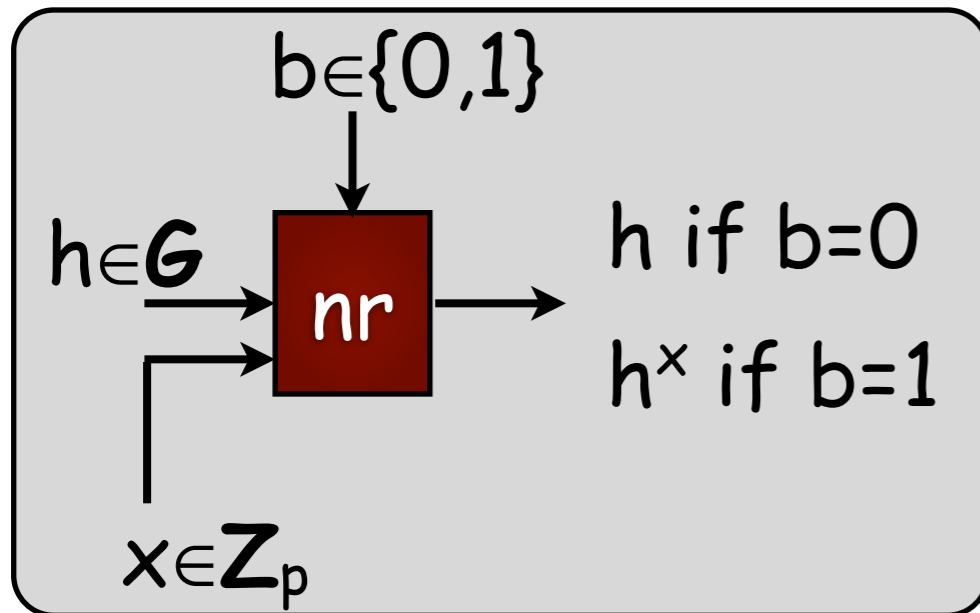




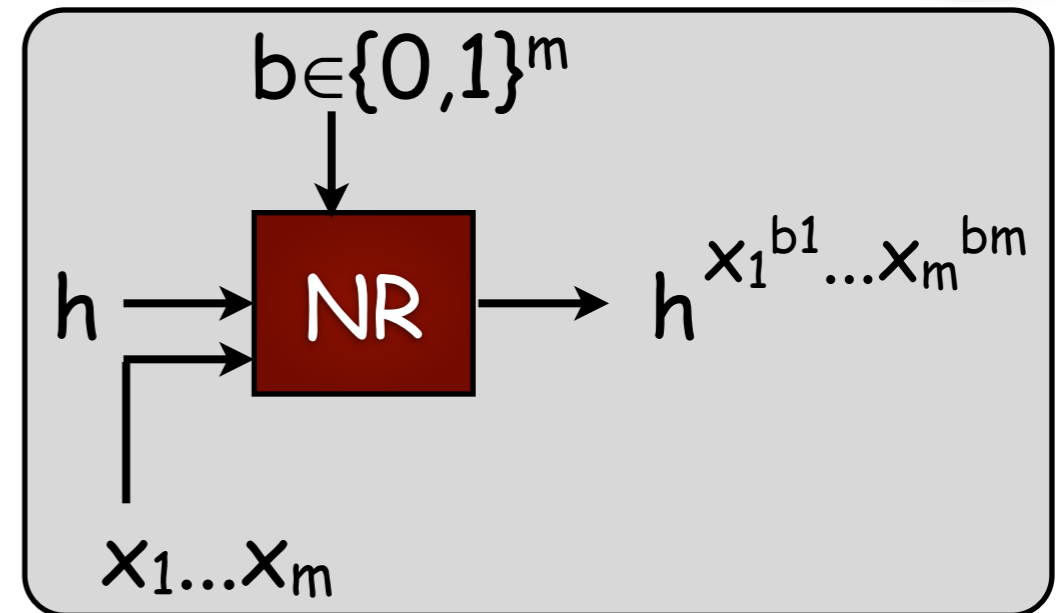
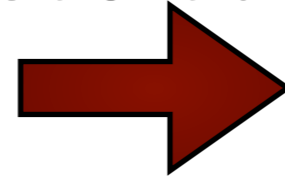
Aug.
Cascade

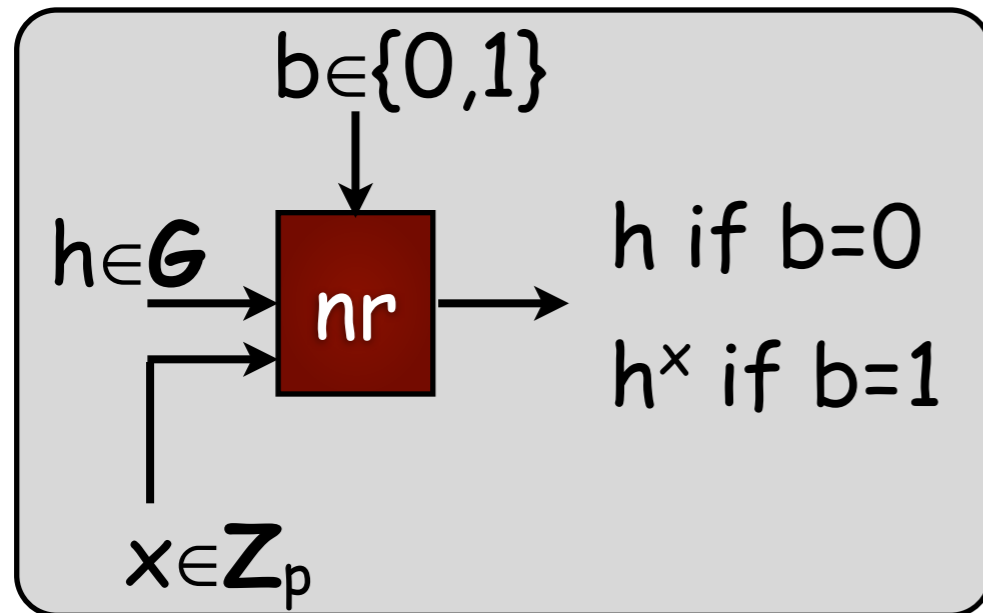


Naor-Reingold [FOCS '97]

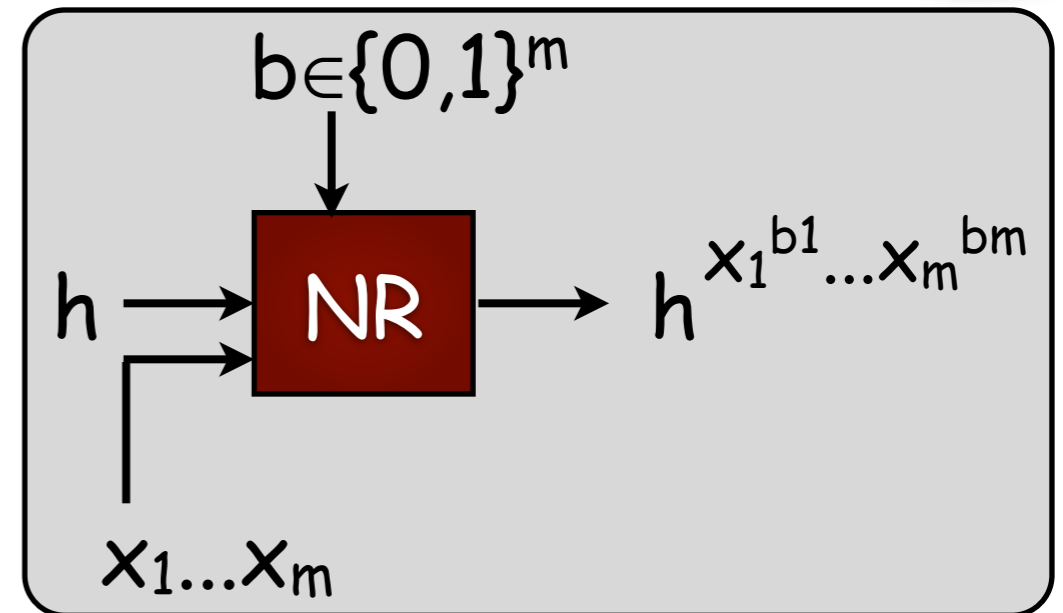


Aug.
Cascade



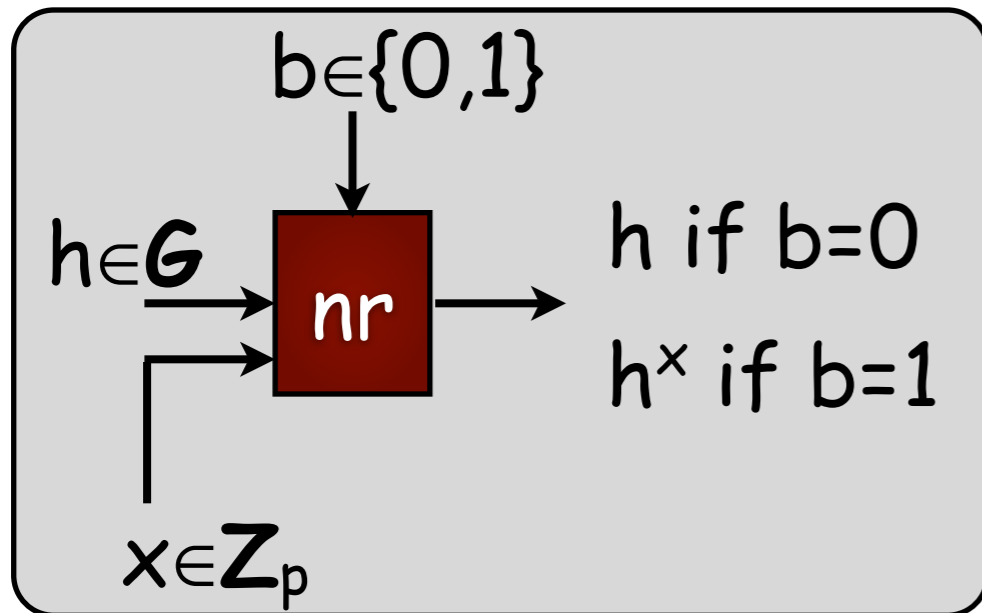


Aug.
Cascade
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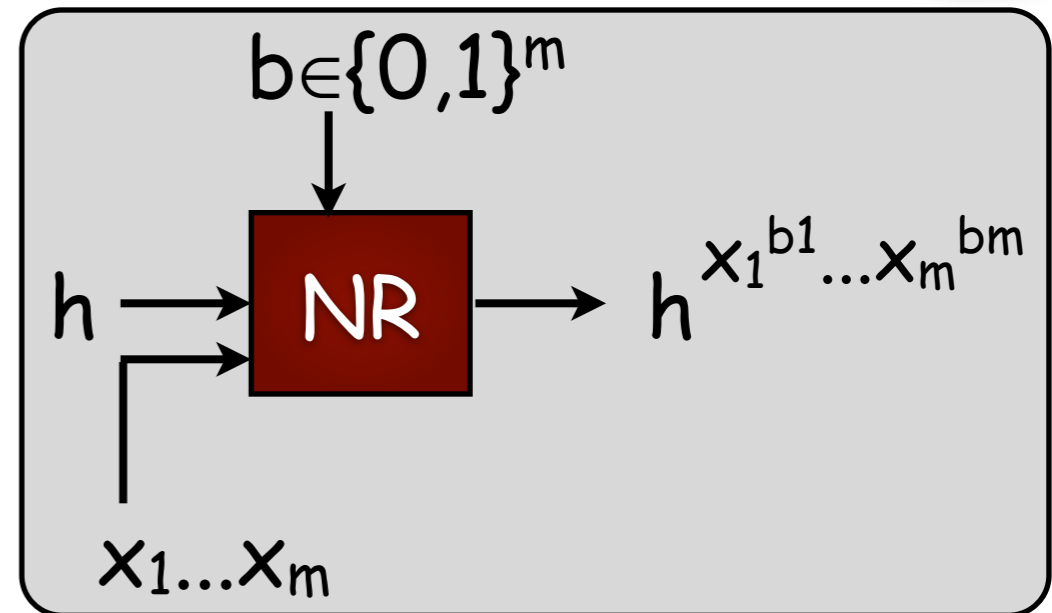


Theorem: **nr** is q -parallel secure under the DDH assumption

Naor-Reingold [FOCS '97]

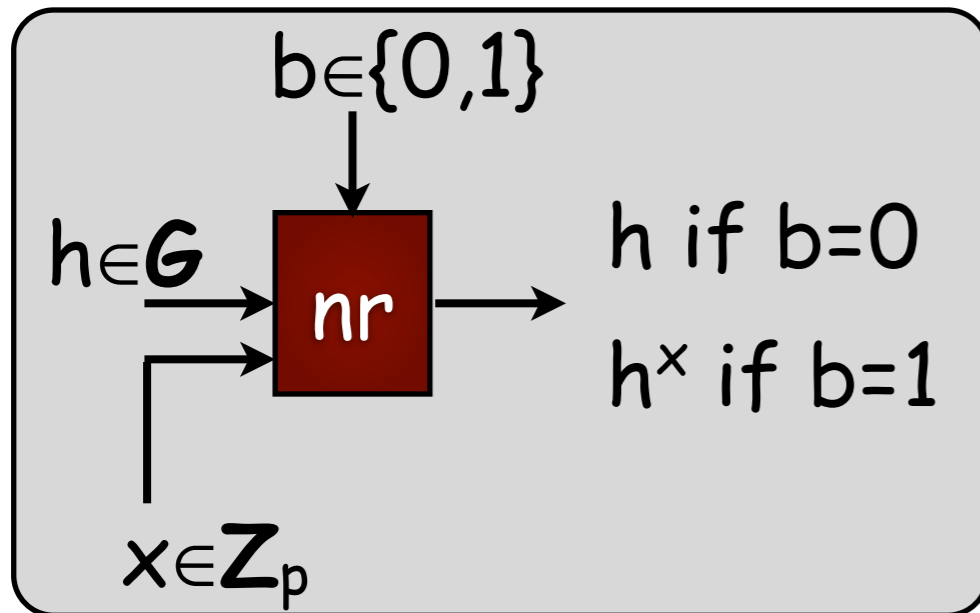


Aug.
Cascade
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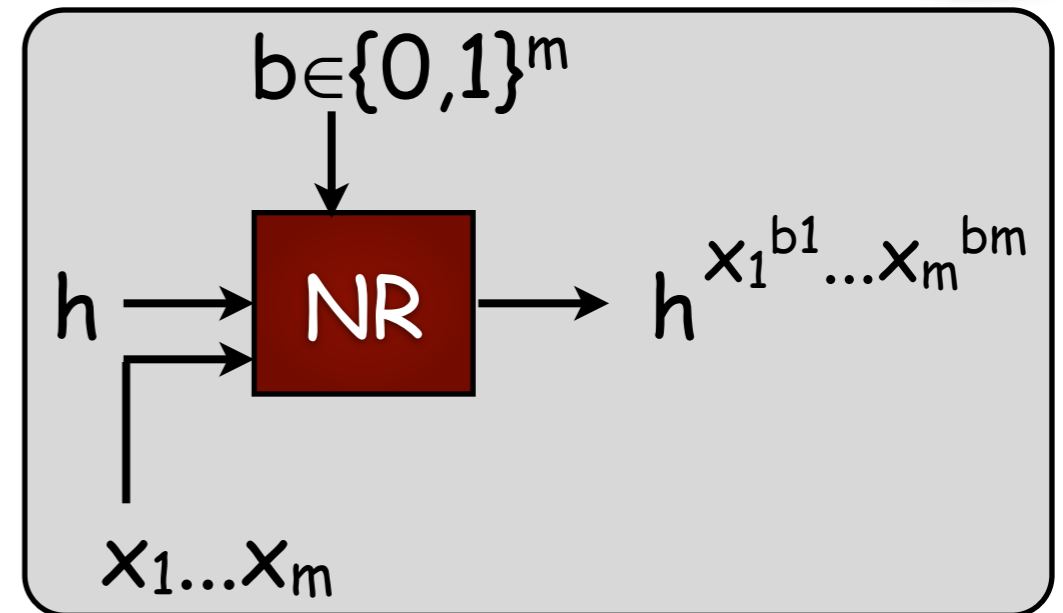
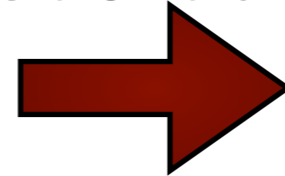


Theorem: **nr** is q -parallel secure under the DDH assumption

Group G of prime order p with generator g .
 g^{ab} looks random in G , given g^a, g^b for random a, b ,



Aug.
Cascade



Theorem: **nr** is q -parallel secure under the DDH assumption

Group G of prime order p with generator g .
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Corollary: **NR** is secure PRF under the DDH assumption



- Details in the paper



- Details in the paper

Theorem: lw is q -parallel secure under the k -linear assumption



- Details in the paper

Theorem: lw is q -parallel secure under the k -linear assumption

Follows from the randomized self-reducibility (due to Lewko-Waters) of the k -linear assumption



- Details in the paper

Theorem: lw is q -parallel secure under the k -linear assumption

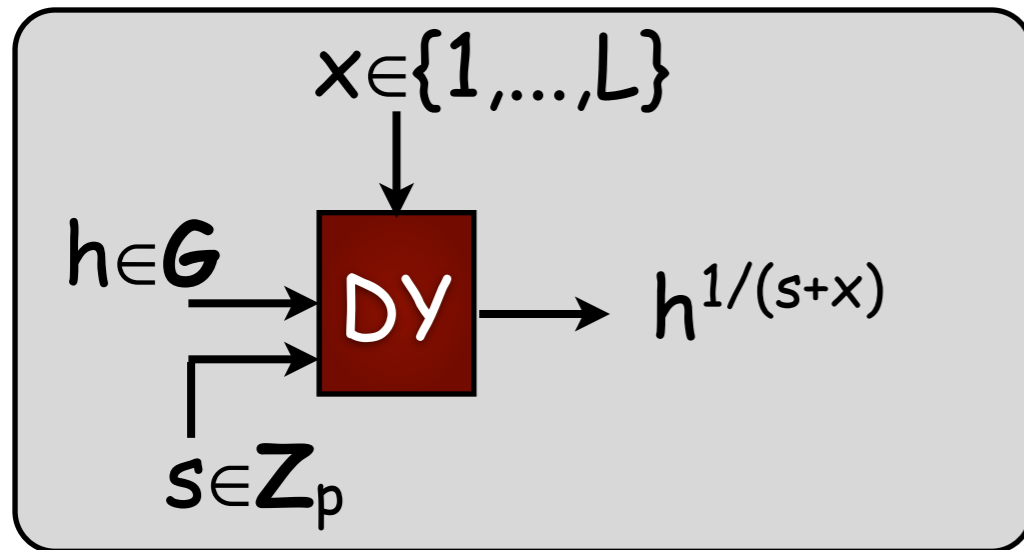
Follows from the randomized self-reducibility (due to Lewko-Waters) of the k -linear assumption

Corollary: LW is secure PRF under the k -linear assumption

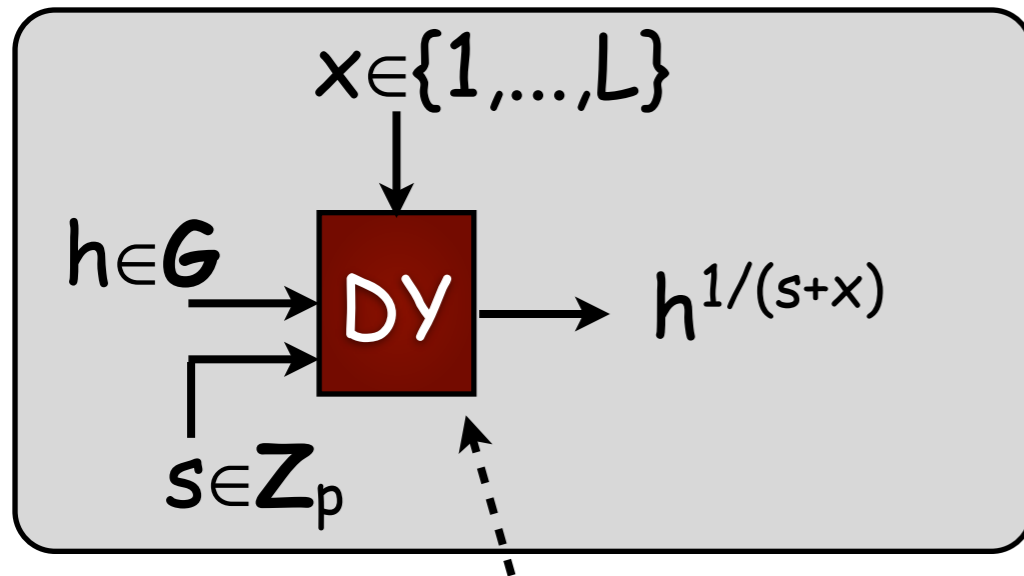
New Algebraic PRF



New Algebraic PRF

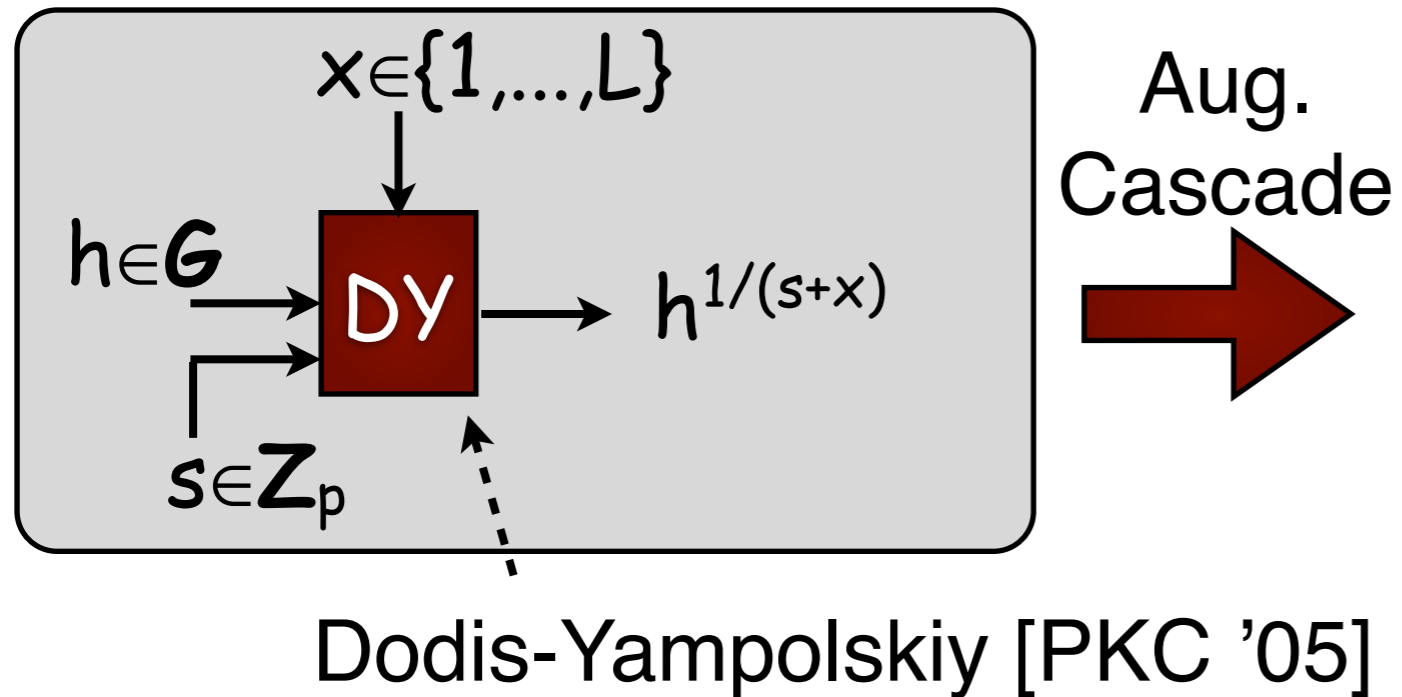


New Algebraic PRF

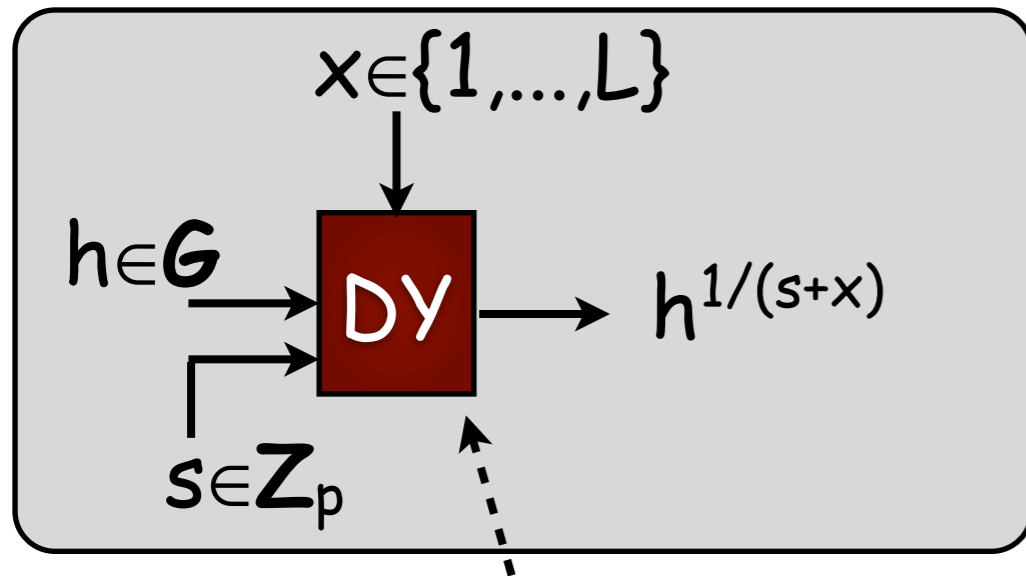


Dodis-Yampolskiy [PKC '05]

New Algebraic PRF

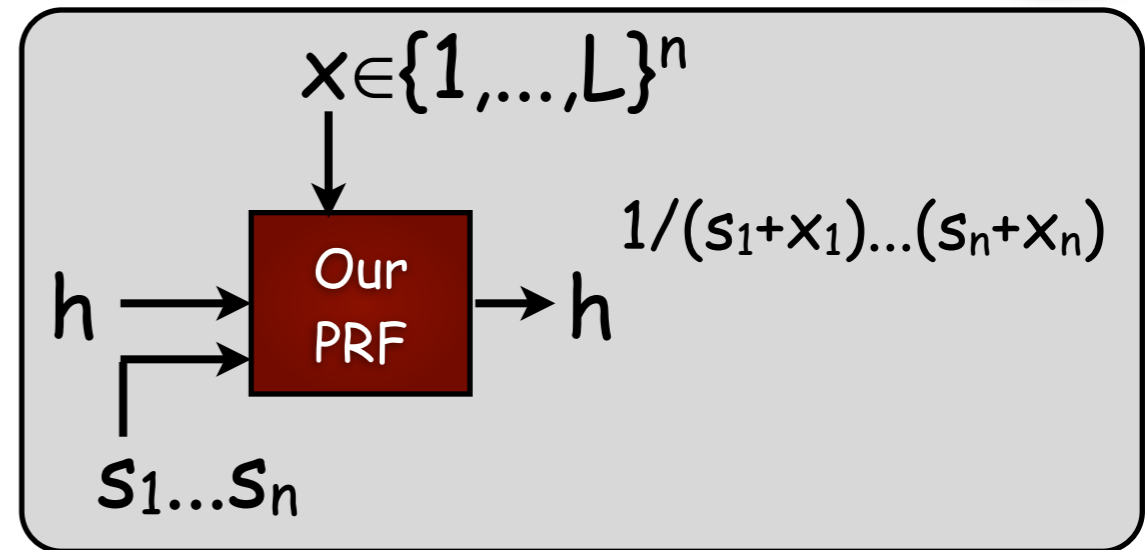
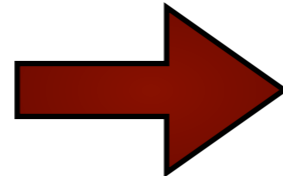


New Algebraic PRF

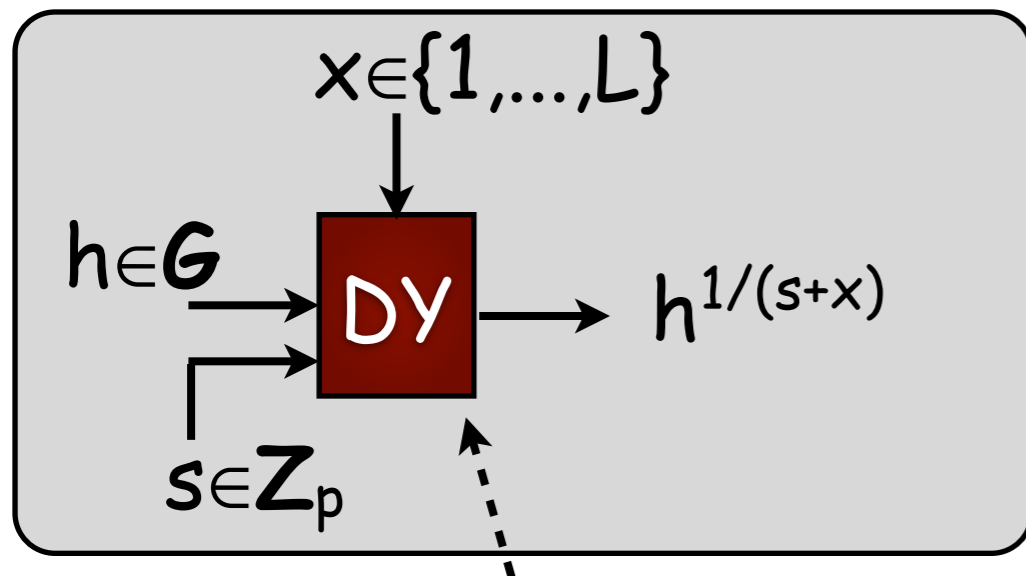


Dodis-Yampolskiy [PKC '05]

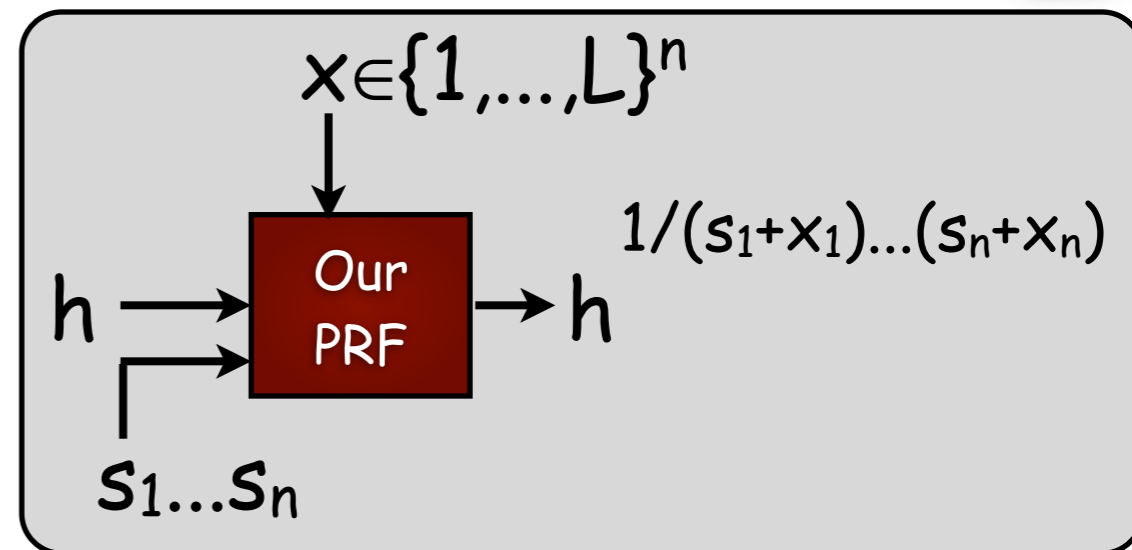
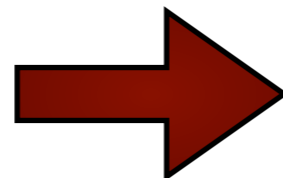
Aug.
Cascade



New Algebraic PRF



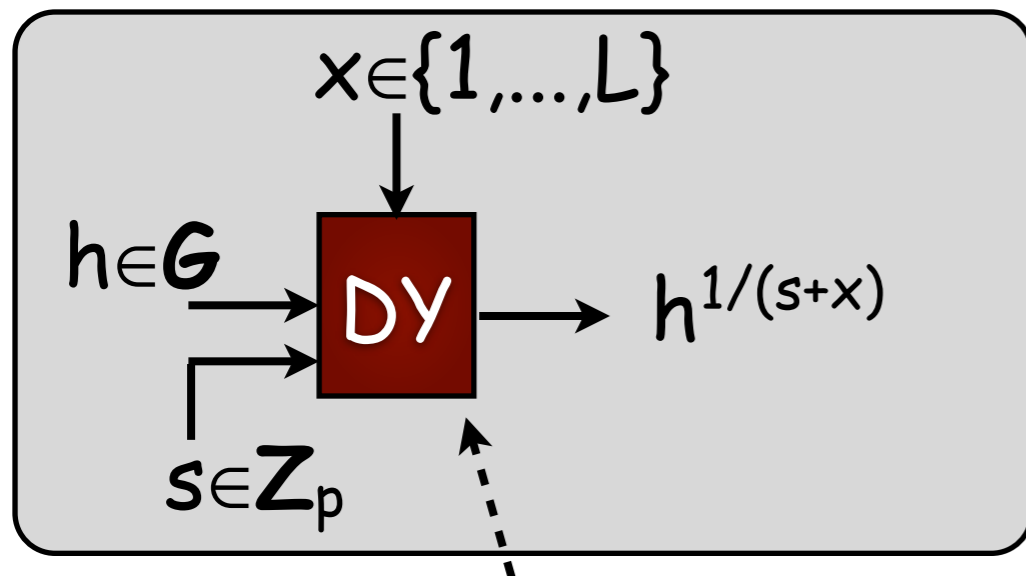
Aug.
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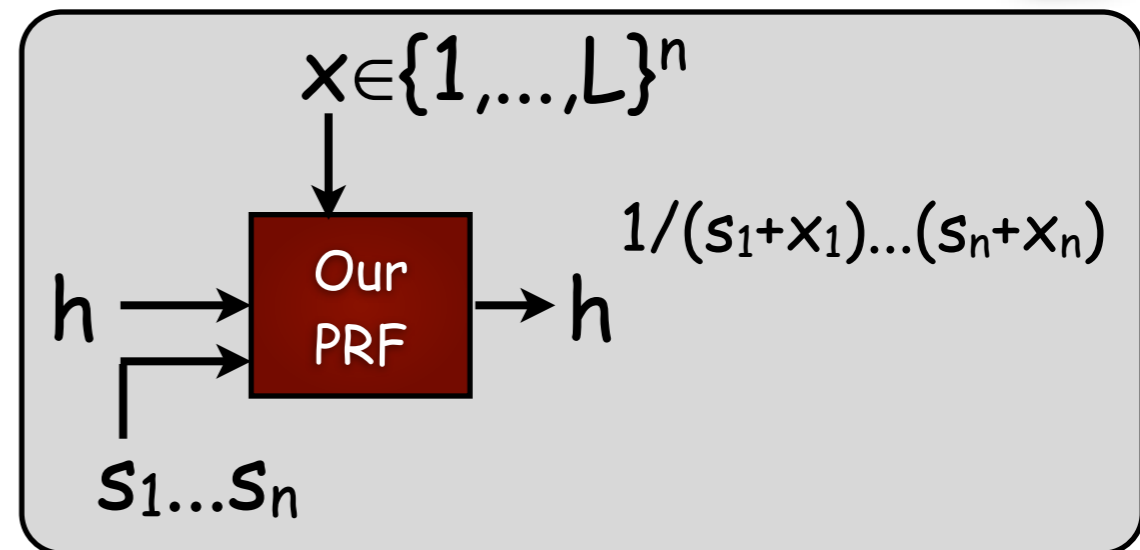
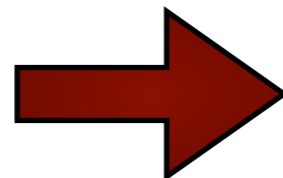
Dodis-Yampolskiy [PKC '05]

Theorem: **DY** is q -parallel secure under the **L-DDH**
(inversion) assumption

New Algebraic PRF



Aug.
Cascade

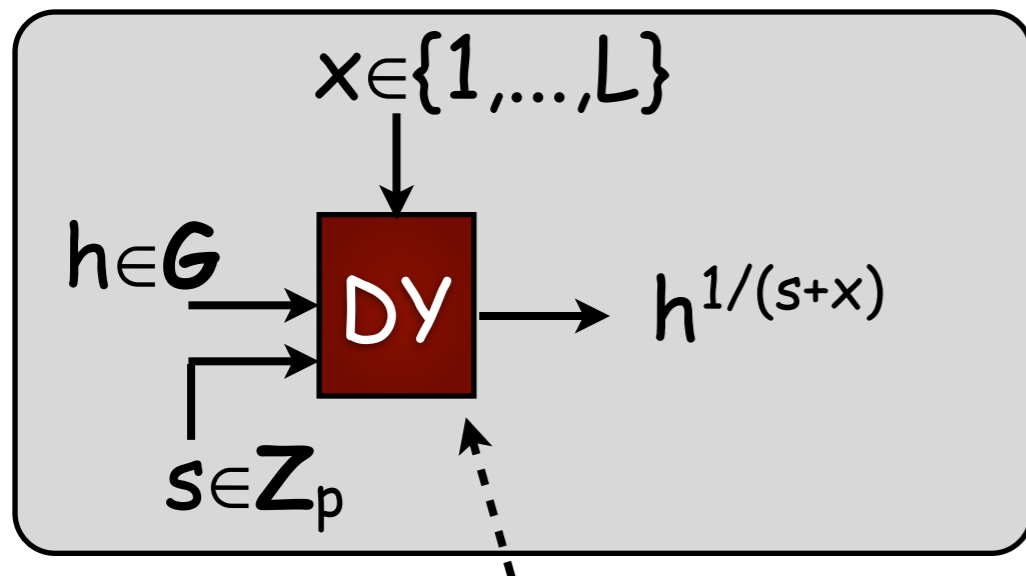


Dodis-Yampolskiy [PKC '05]

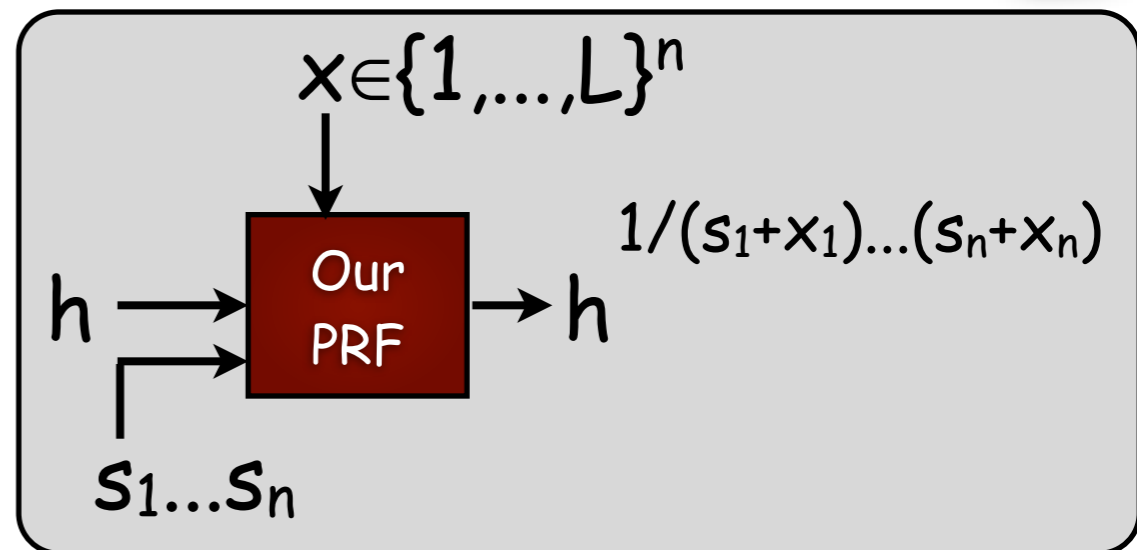
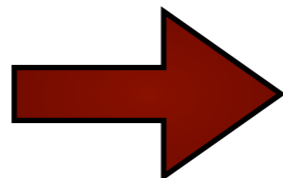
Theorem: **DY** is q -parallel secure under the **L-DDH**
(inversion) assumption

$g^{1/x}$ looks random in \mathbf{G} given
 $(g, g^x, g^{x^2}, \dots, g^{x^L})$

New Algebraic PRF



Aug.
Cascade



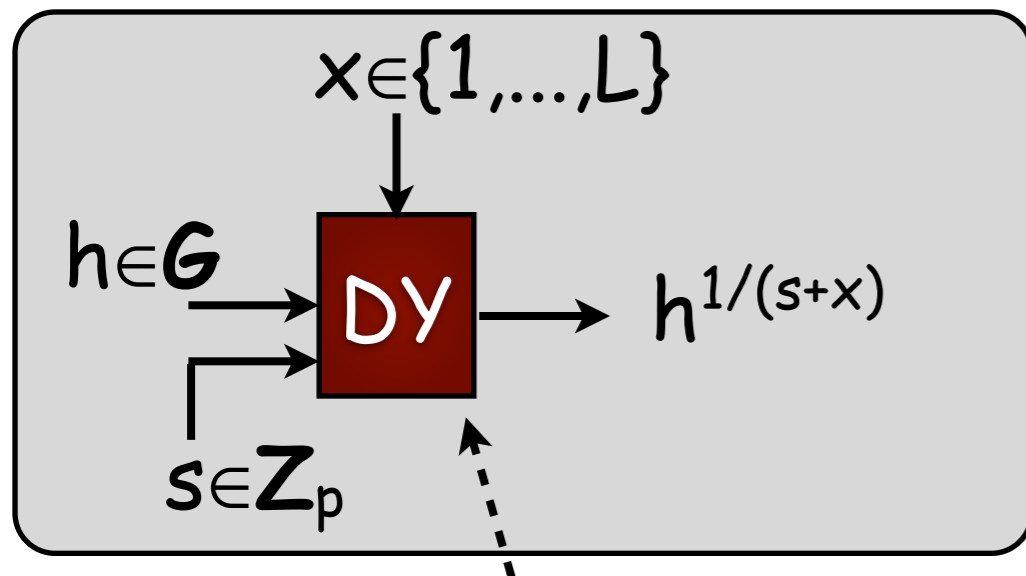
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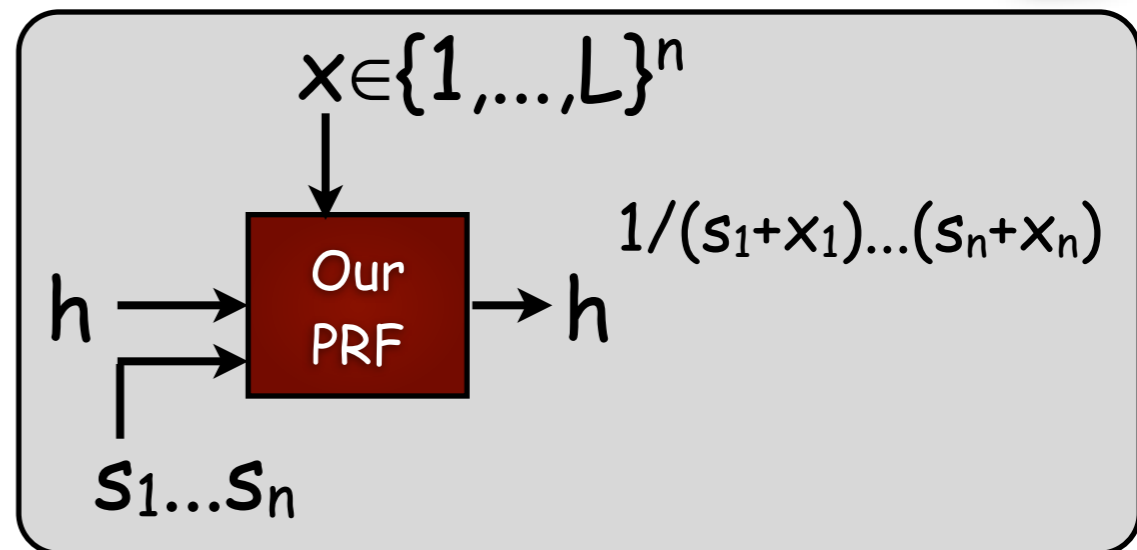
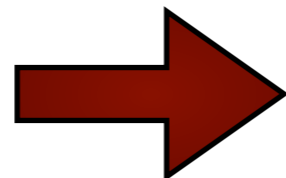
(Details in the paper)

$g^{1/x}$ looks random in \mathbf{G} given
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New Algebraic PRF



Aug.
Cascade



Dodis-Yampolskiy [PKC '05]

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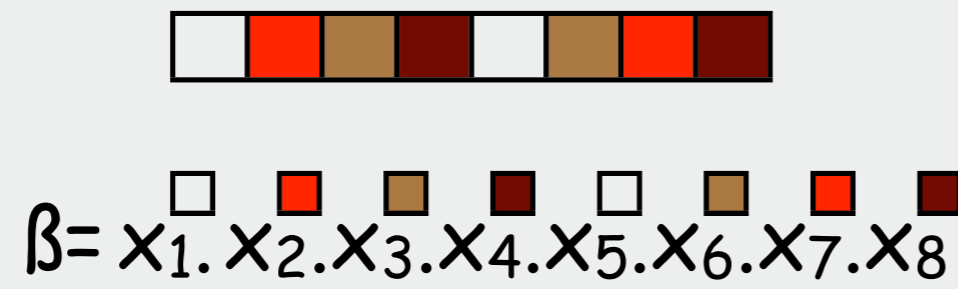
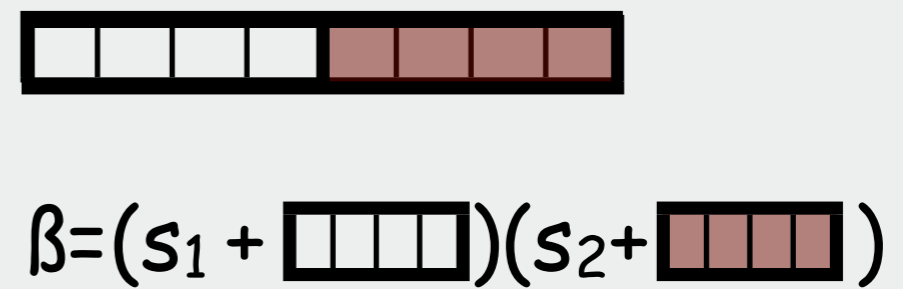
Corollary: **Our PRF** is secure PRF under the **L-DDH** assumption

Comparison to Naor-Reingold



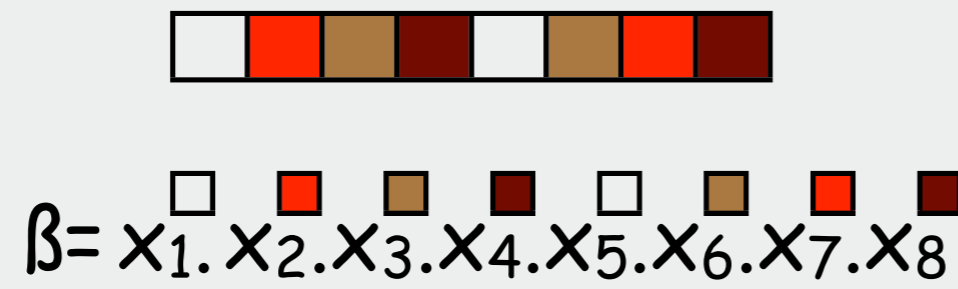
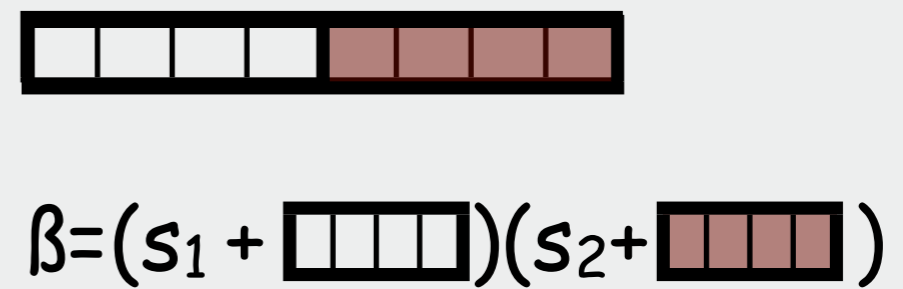
Comparison to Naor-Reingold



	Naor-Reingold PRF	Our PRF
Domain	$\{0,1\}^m$	$[L]^n$ ($L=2^l, n=m/l$)
Keys	h in \mathbf{G} , x_1, \dots, x_m in \mathbf{Z}_p	h in \mathbf{G} , s_1, \dots, s_n in \mathbf{Z}_p
PRF	 $\beta = x_1^{\square} x_2^{\square} x_3^{\square} x_4^{\square} x_5^{\square} x_6^{\square} x_7^{\square} x_8^{\square}$ $F(x) = h^{\beta}$	 $\beta = (s_1 + \square\square\square\square)(s_2 + \square\square\square\square)$ $F(x) = h^{1/\beta}$

Comparison to Naor-Reingold

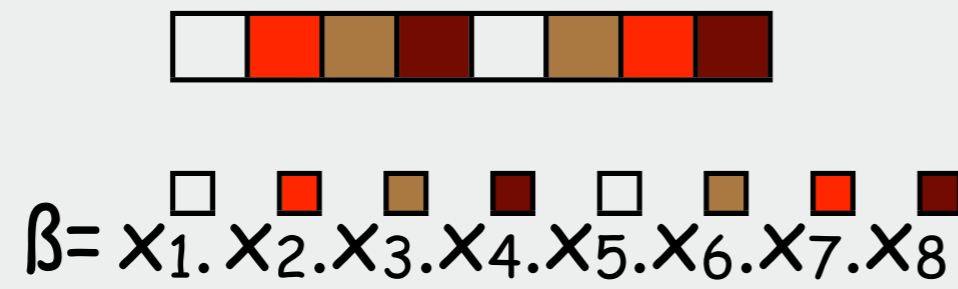
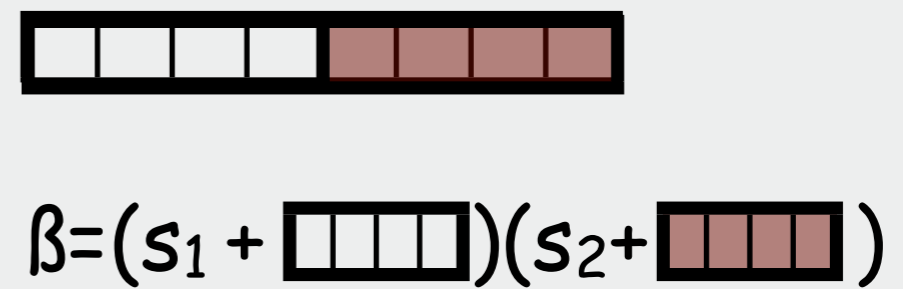


	Naor-Reingold PRF	Our PRF
Domain	$\{0,1\}^m$	$[L]^n$ ($L=2^l, n=m/l$)
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Secret key shorter by a **factor of l**

Comparison to Naor-Reingold





	Naor-Reingold PRF	Our PRF
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Secret key shorter by a **factor of l**

Factor of l fewer multiplications to evaluate β

Comparison to Naor-Reingold



	Naor-Reingold PRF	Our PRF
Domain	$\{0,1\}^m$	$[L]^n$ ($L=2^l, n=m/l$)
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Secret key shorter by a **factor of l**

Factor of l fewer multiplications to evaluate β

However, security becomes weaker as **l increases**

Comparison to Naor-Reingold



	Naor-Reingold PRF	Our PRF
Domain	$\{0,1\}^m$	$[L]^n$ ($L=2^l, n=m/l$)
Keys	h in \mathbf{G} , x_1, \dots, x_m in \mathbf{Z}_p	h in \mathbf{G} , s_1, \dots, s_n in \mathbf{Z}_p
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Secret key shorter by a **factor of l**

Factor of l fewer multiplications to evaluate β

However, security becomes weaker as **l increases**

$l = 4$ or 8 is reasonable

Verifiable Random Functions



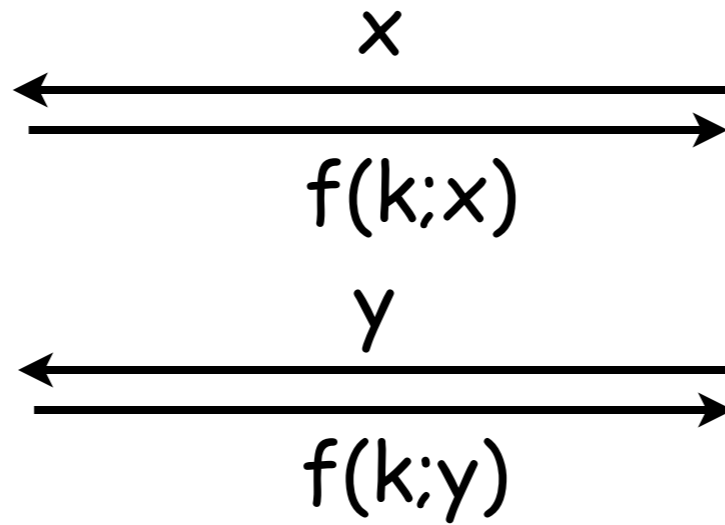
Verifiable Random Functions



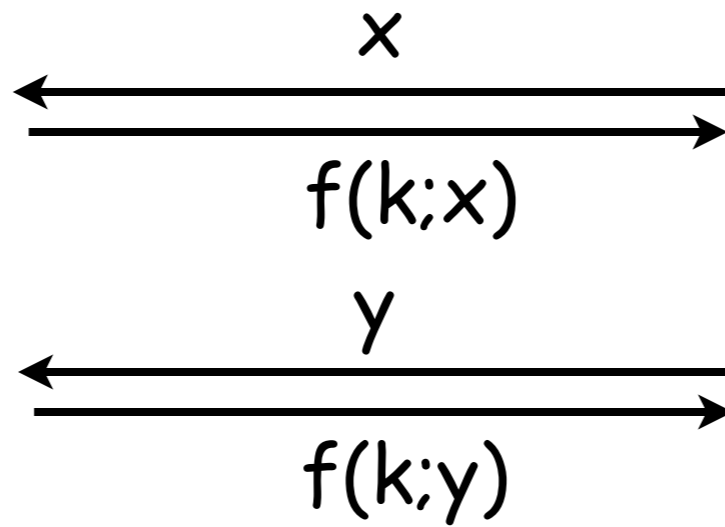
Verifiable Random Functions



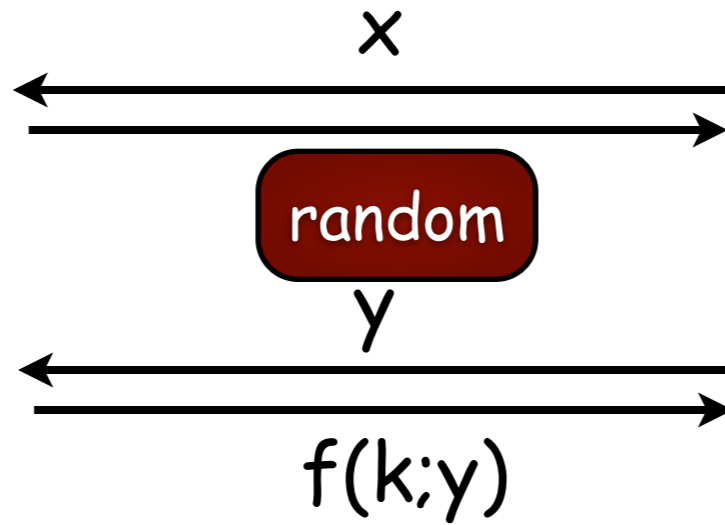
Verifiable Random Functions



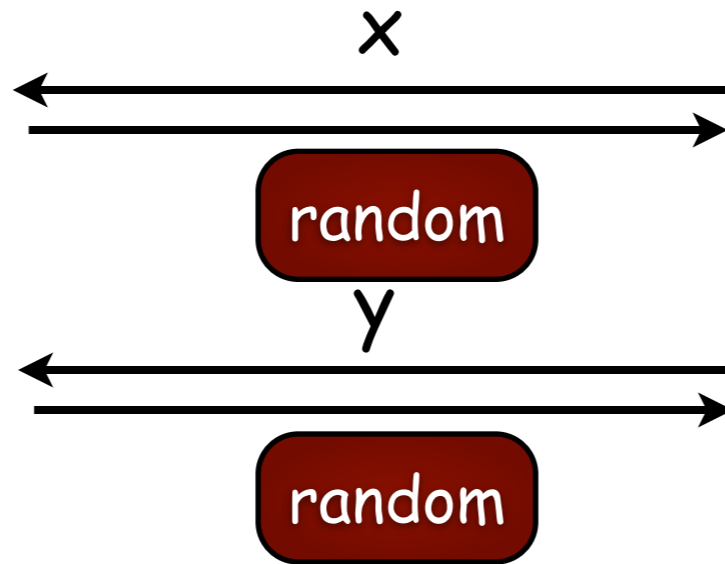
Verifiable Random Functions



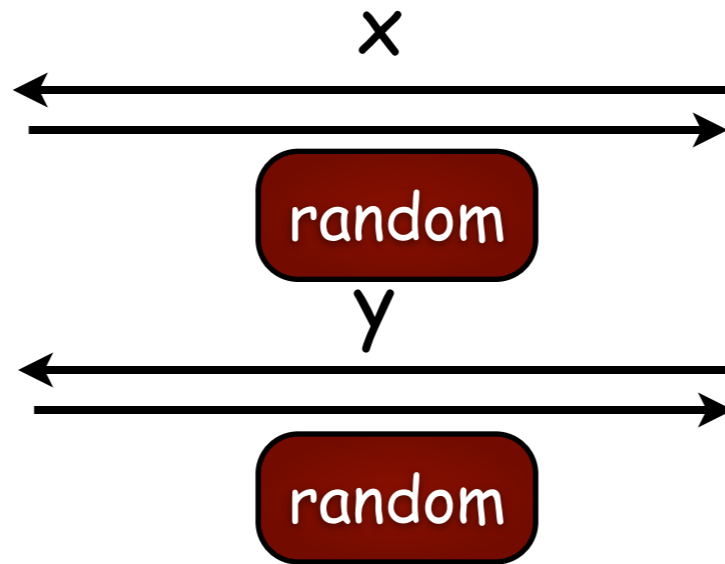
Verifiable Random Functions



Verifiable Random Functions

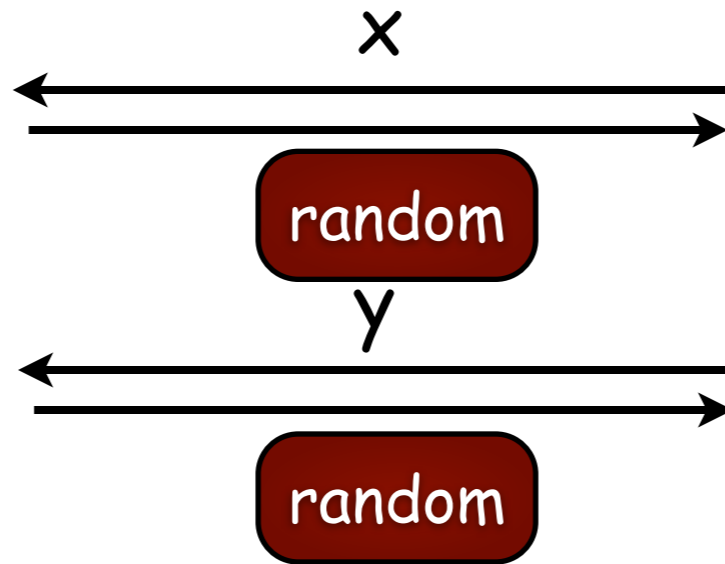


Verifiable Random Functions



How to
guarantee
honest
evaluation?

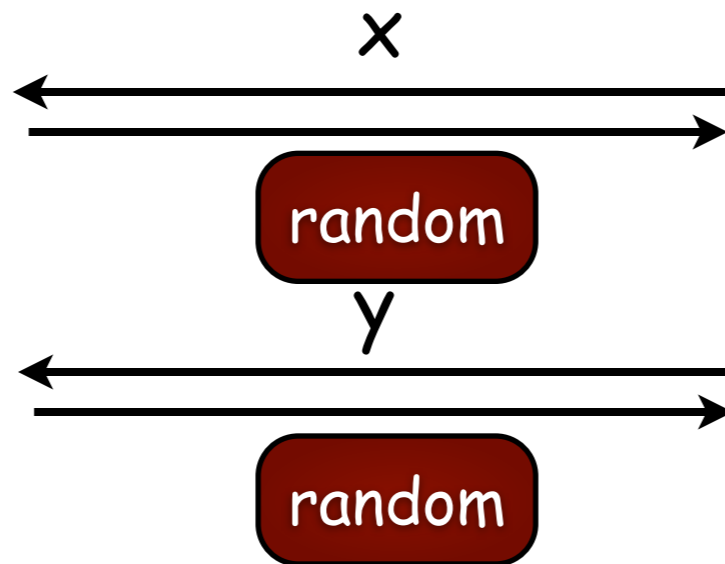
Verifiable Random Functions



How to
guarantee
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- Introduced by Micali-Rabin-Vadhan [FOCS '99]

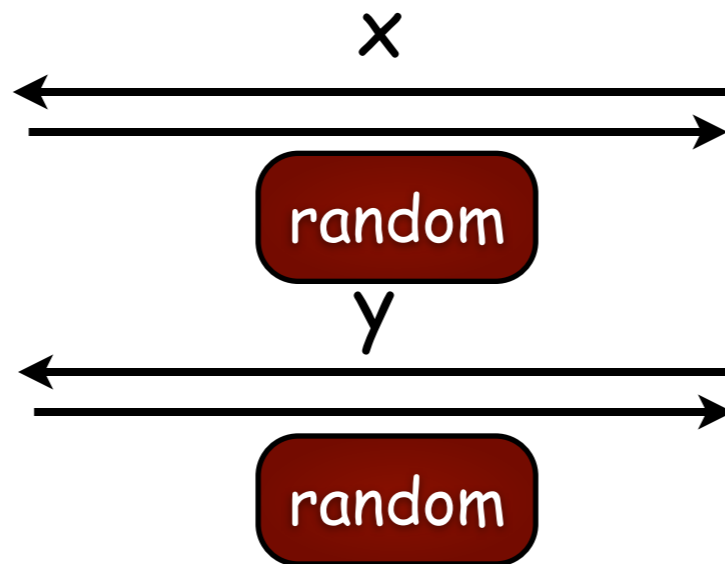
Verifiable Random Functions



How to
guarantee
honest
evaluation?

- Introduced by Micali-Rabin-Vadhan [FOCS '99]
- Produce **non-interactive proofs** (that can be verified by anyone) that the PRF is evaluated correctly

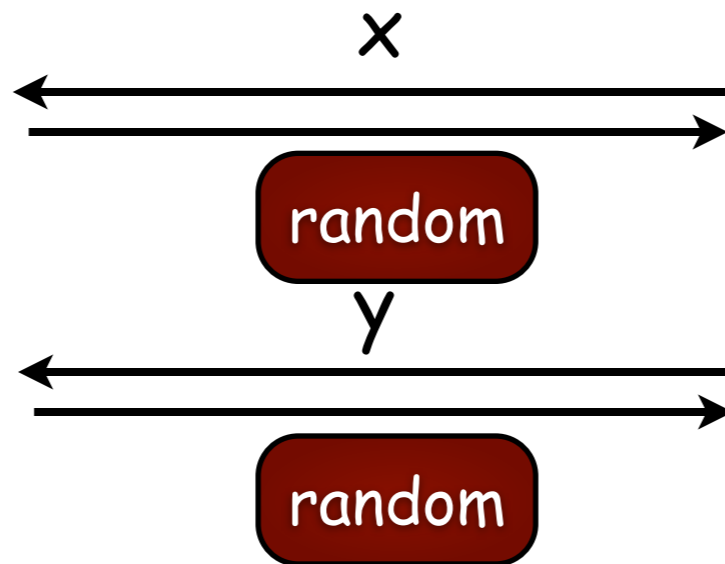
Verifiable Random Functions



How to
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- Produce **non-interactive proofs** (that can be verified by anyone) that the PRF is evaluated correctly
- Not at the cost of pseudorandomness!

Verifiable Random Functions



How to
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- Applications: Unique-signature schemes, e-cash schemes [BCKL '09, ASM '07], updatable zero-knowledge databases [Liskov '05] etc.

Verifiable Random Functions



Verifiable Random Functions



- We construct VRFs using the augmented cascade

Verifiable Random Functions



- We construct VRFs using the **augmented cascade**
- Security from Bilinear Diffie-Hellman Inversion assumption

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[HW '10]	2^m (arbitrary)	$O(mQ)$
our large-domain VRF	2^m (arbitrary)	$O(m)$

Conclusions



Conclusions

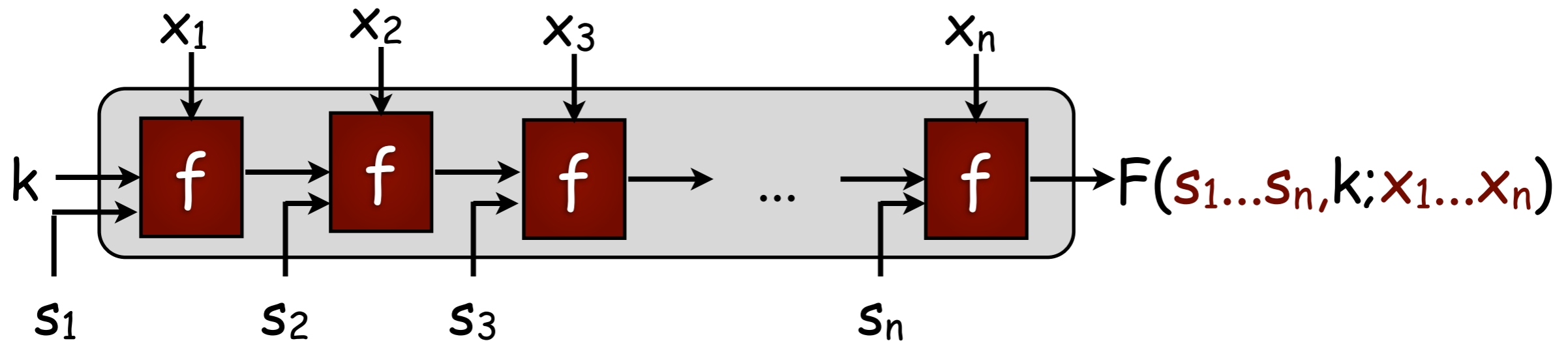


- 1) New generic tool to construct PRFs – **augmented cascade**

Conclusions

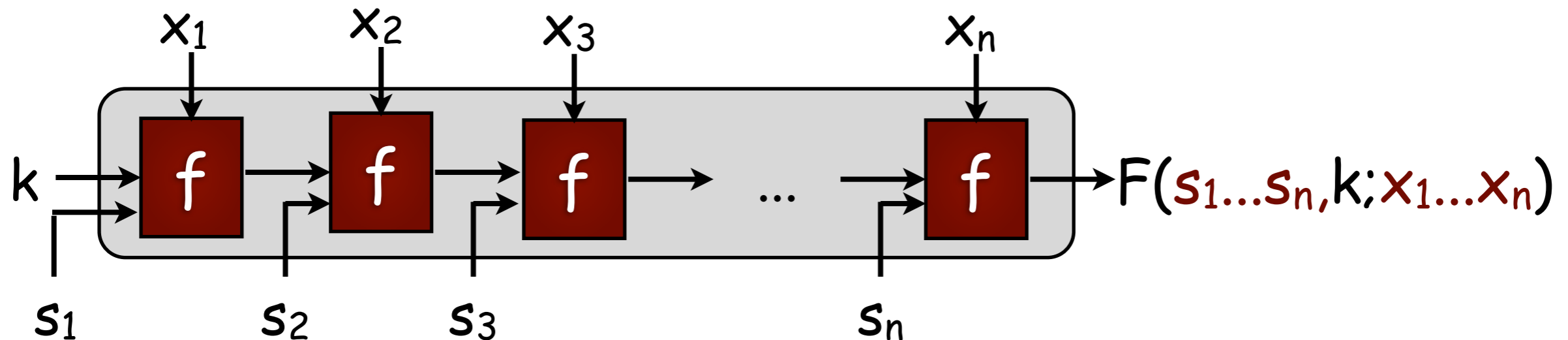


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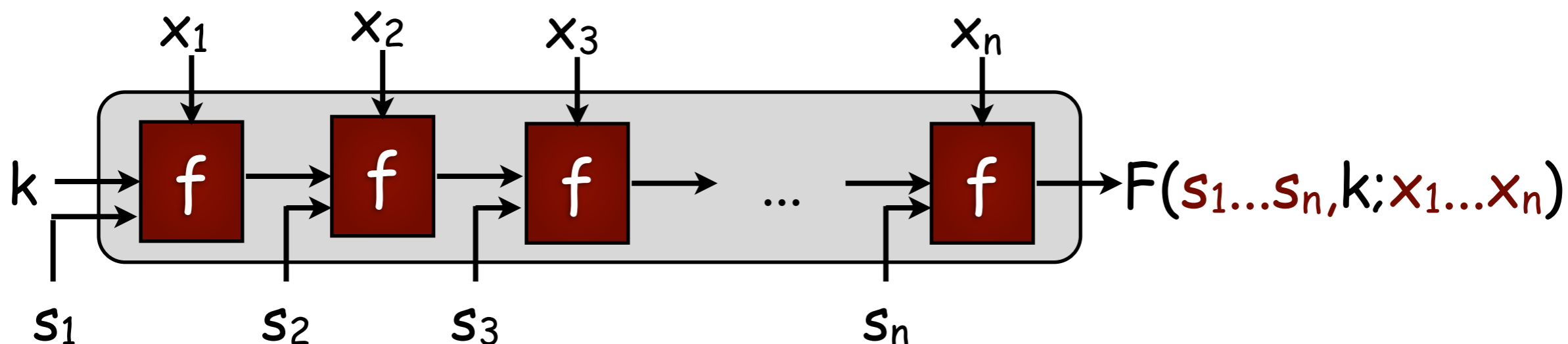


2) Simple proofs of security for existing algebraic PRFs

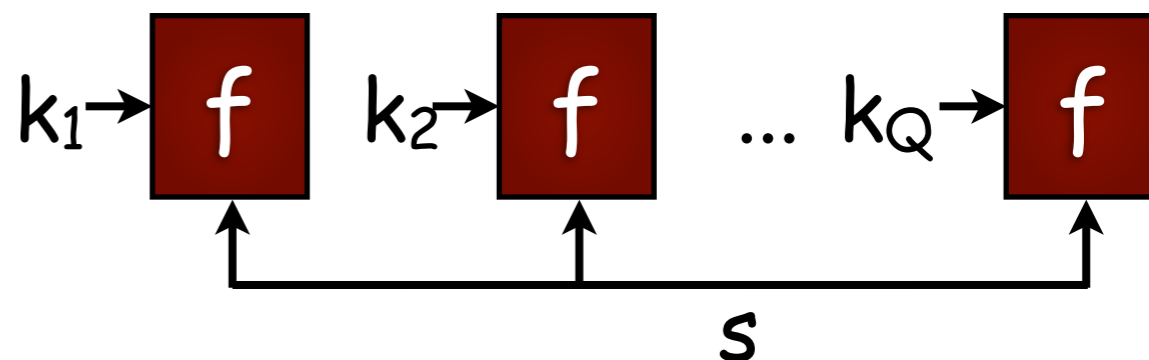
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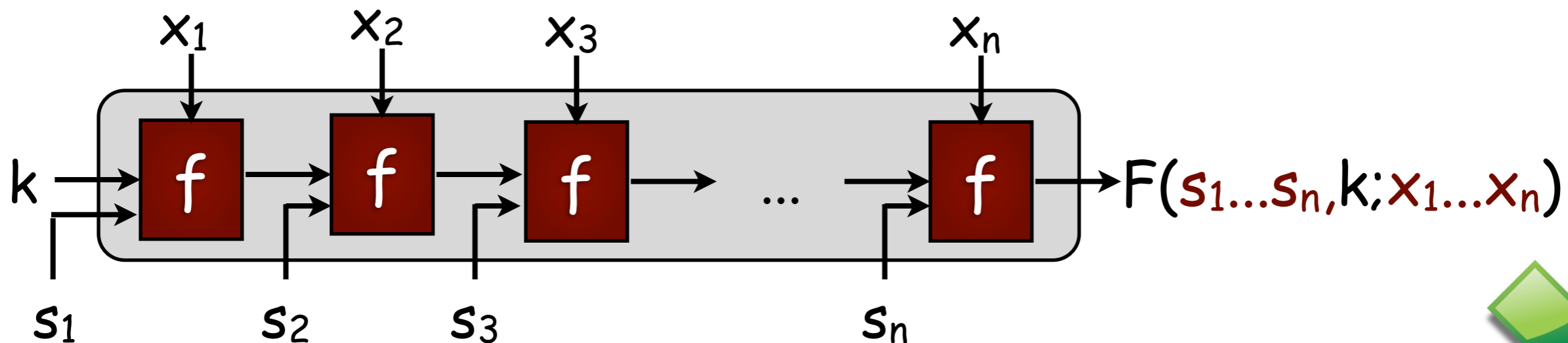
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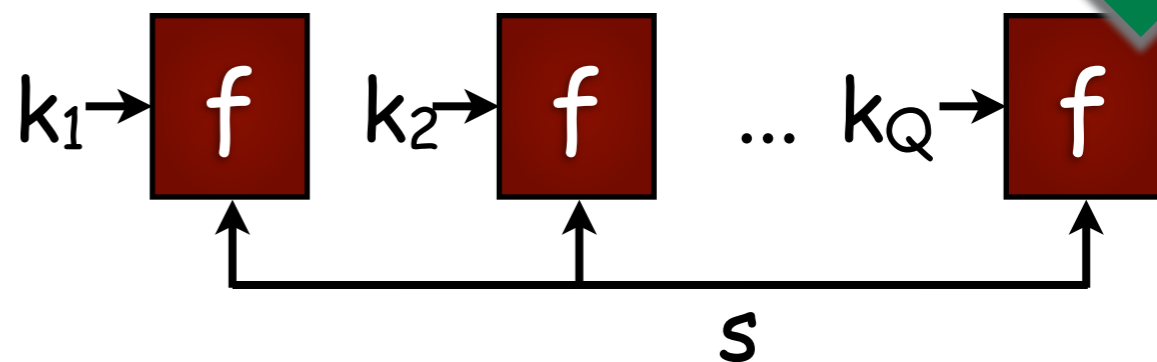
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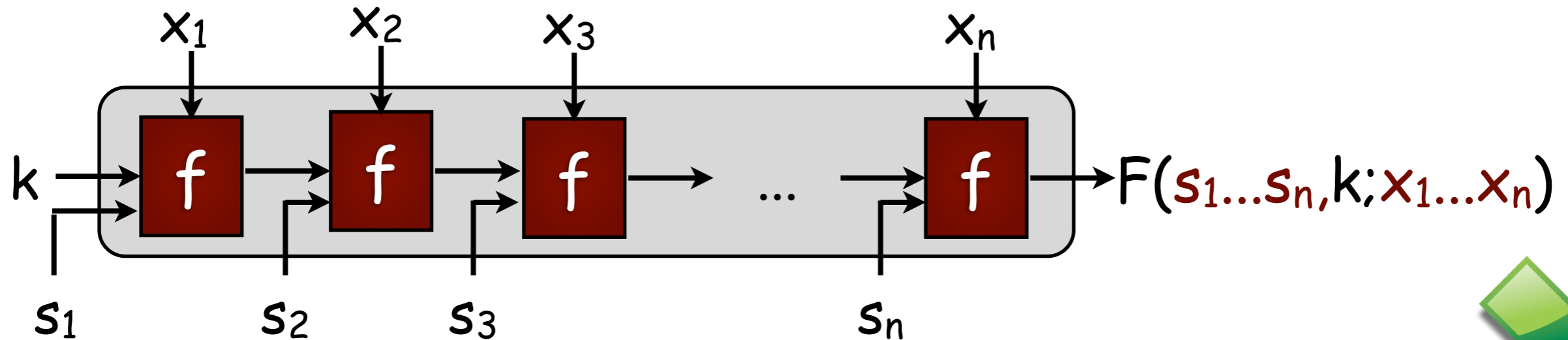
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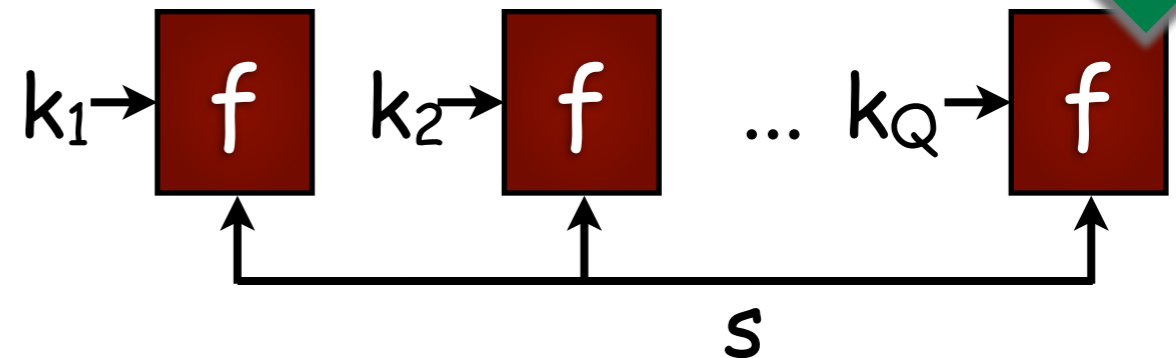


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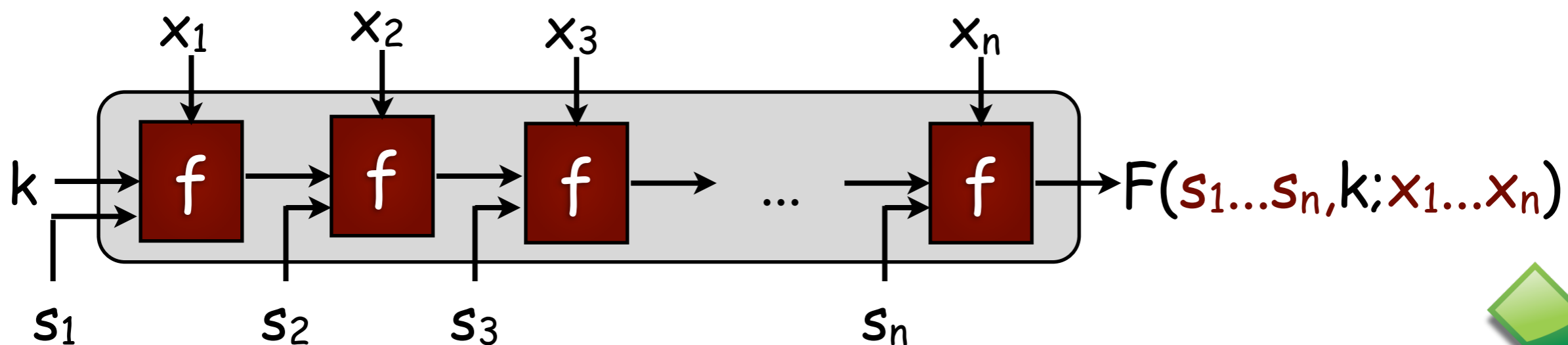
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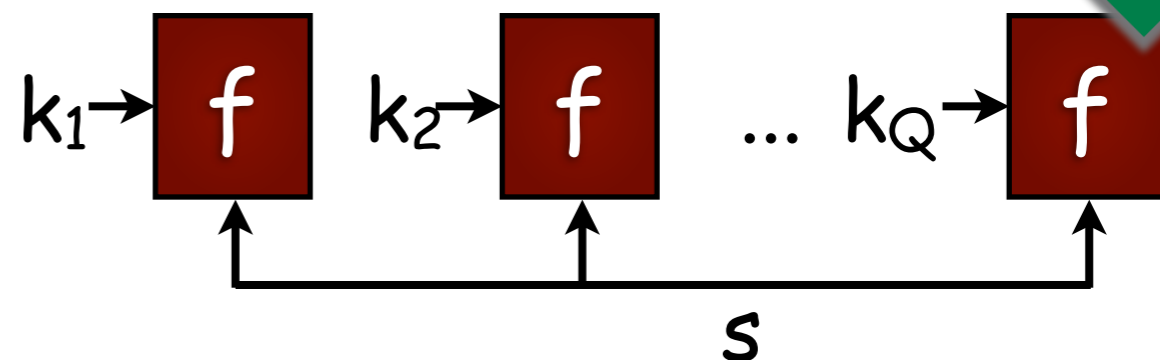
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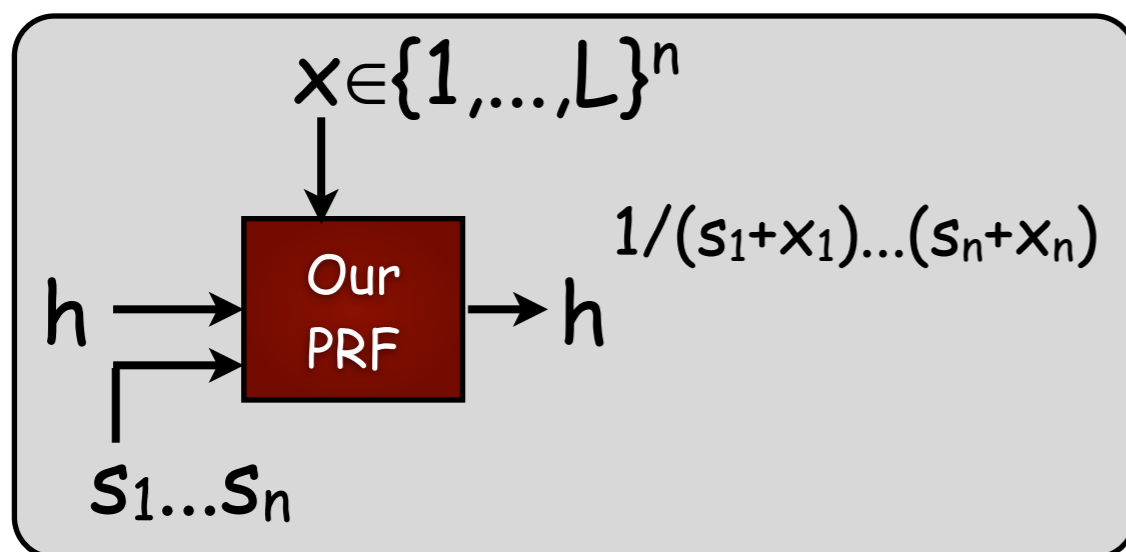
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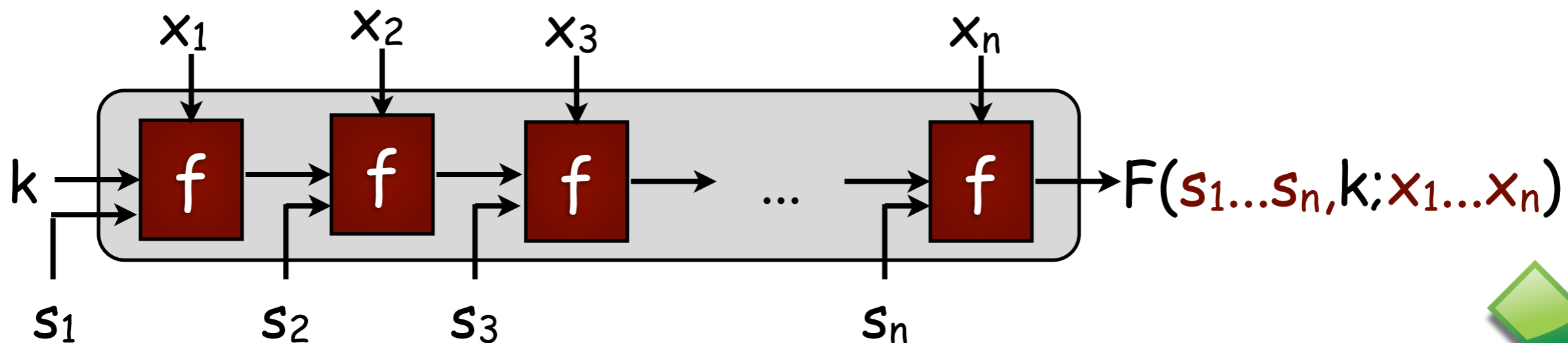
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Conclusions

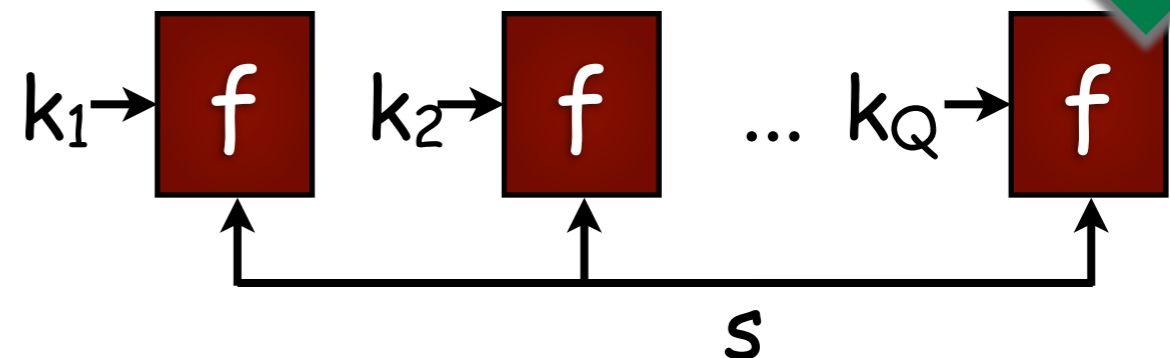
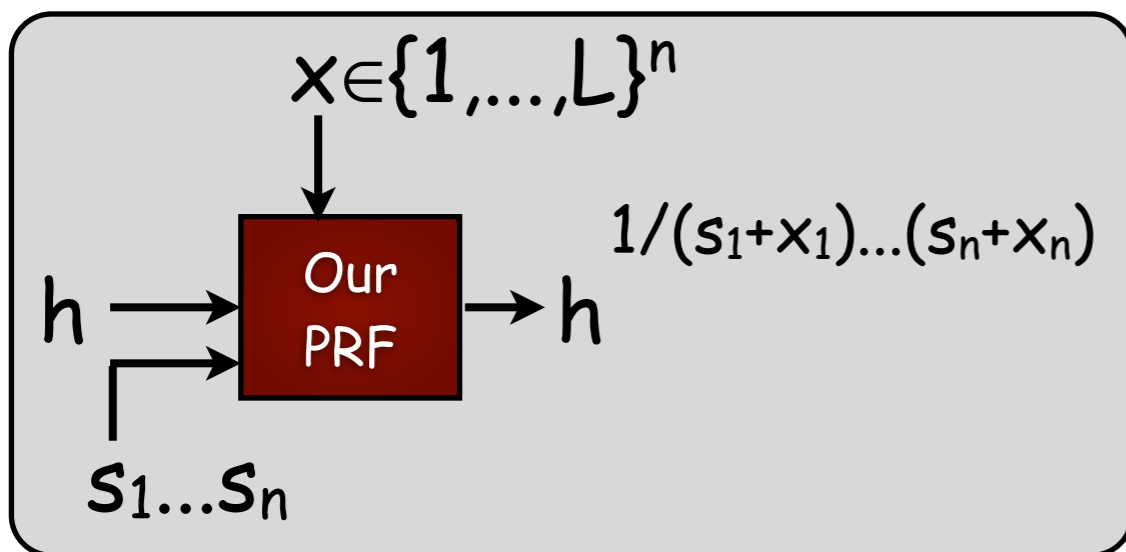


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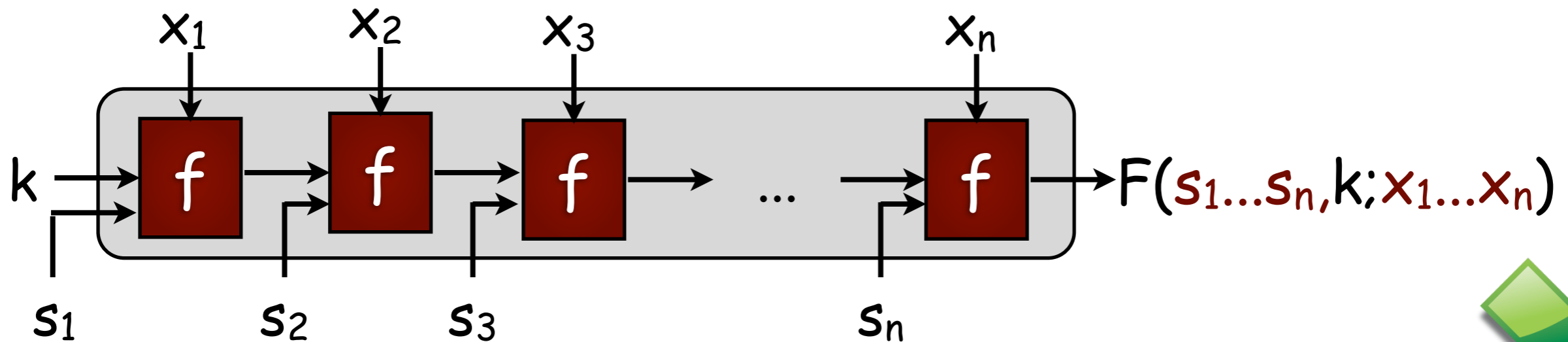


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Conclusions

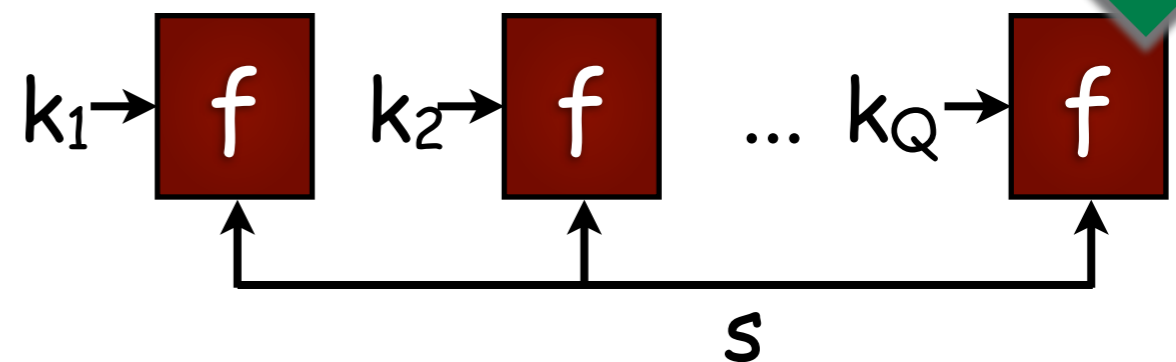
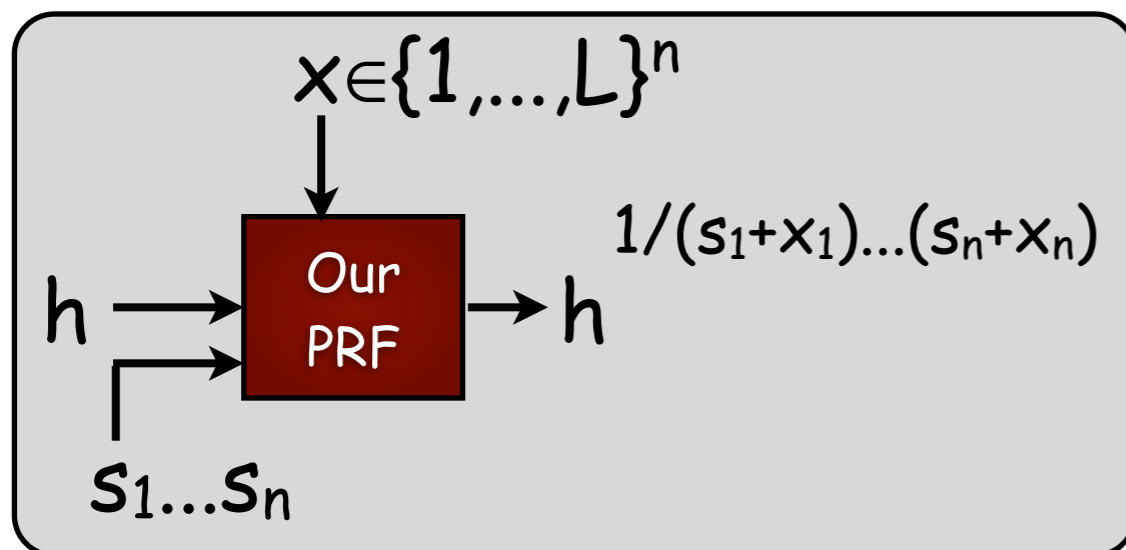


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5) (in paper) Simulatable VRFs

Thank You!



Any questions?