

Lattice-Based Non-Interactive Argument Systems

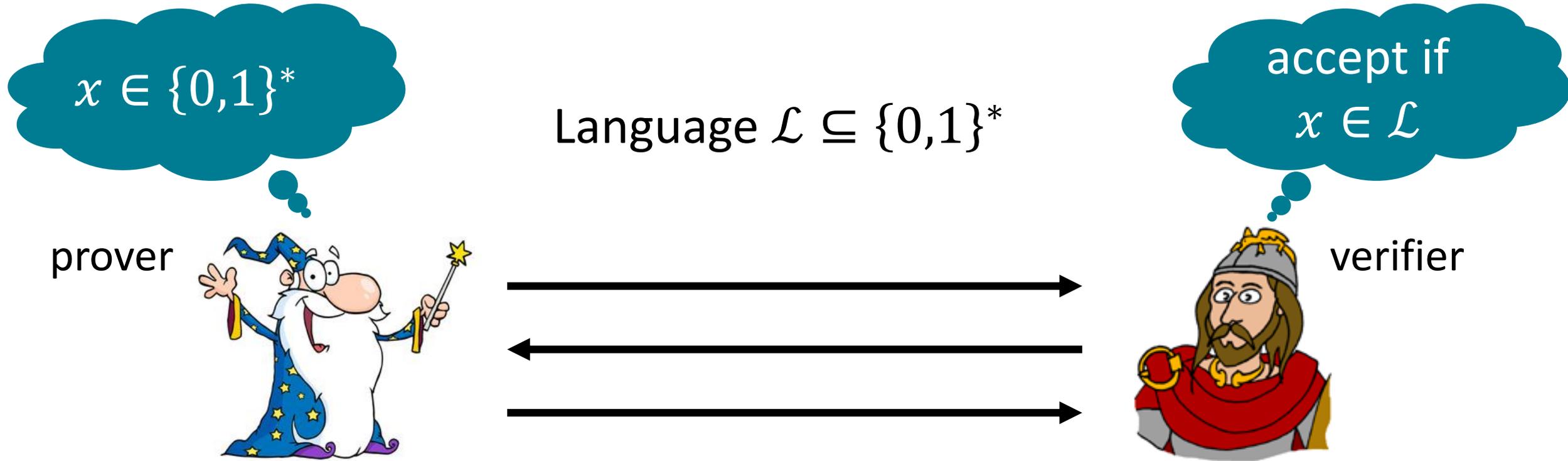
David Wu

Stanford University

Based on joint works with Dan Boneh, Yuval Ishai, Sam Kim, and Amit Sahai

Proof Systems and Argument Systems

[GMR85]



Completeness:

$$\forall x \in \mathcal{L} : \Pr[\langle P, V \rangle(x) = \text{accept}] = 1$$

“Honest prover convinces honest verifier of true statements”

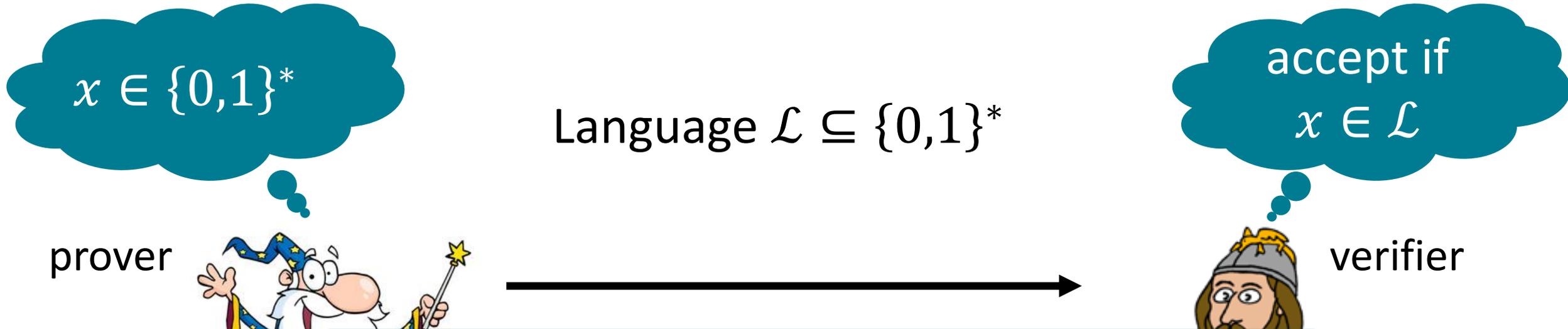
Soundness:

$$\forall x \notin \mathcal{L}, \forall P^* : \Pr[\langle P^*, V \rangle(x) = \text{accept}] = 0$$

“No prover can convince honest verifier of false statement”

Proof Systems and Argument Systems

[GMR85]



In an argument system, we relax soundness to only consider computationally-bounded (i.e., polynomial-time) provers P^*

Completeness:

"Honest prover convinces honest verifier of true statements"

Soundness:

$\forall x \notin \mathcal{L}, \forall P^* : \Pr[\langle P^*, V \rangle(x) = \text{accept}] = 0$

"No prover can convince honest verifier of false statement"

The Complexity Class NP

NP – the class of languages that are *efficiently verifiable*

a language \mathcal{L} is in **NP** if there exists a polynomial-time verifier R such that

$$x \in \mathcal{L} \Leftrightarrow \exists w \in \{0,1\}^{\text{poly}(|x|)} R(x, w) = 1$$

Statement

Witness

The Complexity Class NP

NP – the class of languages that are *efficiently verifiable*

a language \mathcal{L} is in **NP** if there exists a polynomial-time verifier R such that

$$x \in \mathcal{L} \Leftrightarrow \exists w \in \{0,1\}^{\text{poly}(|x|)} R(x, w) = 1$$

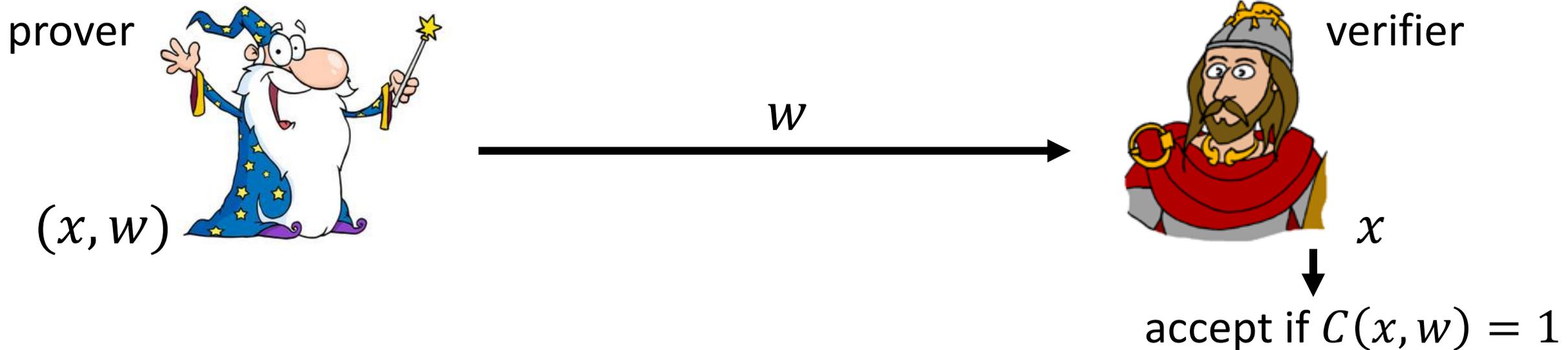
In this talk, will focus on language of Boolean circuit satisfiability:

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$

Boolean circuit

Non-Interactive Proof Systems for NP

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$



NP languages have non-interactive proof systems

But what if we want other properties?

Non-Interactive Proof Systems for NP

Zero-Knowledge: The proof reveals nothing more about the statement x other than $x \in \mathcal{L}_C$ [GMR85]

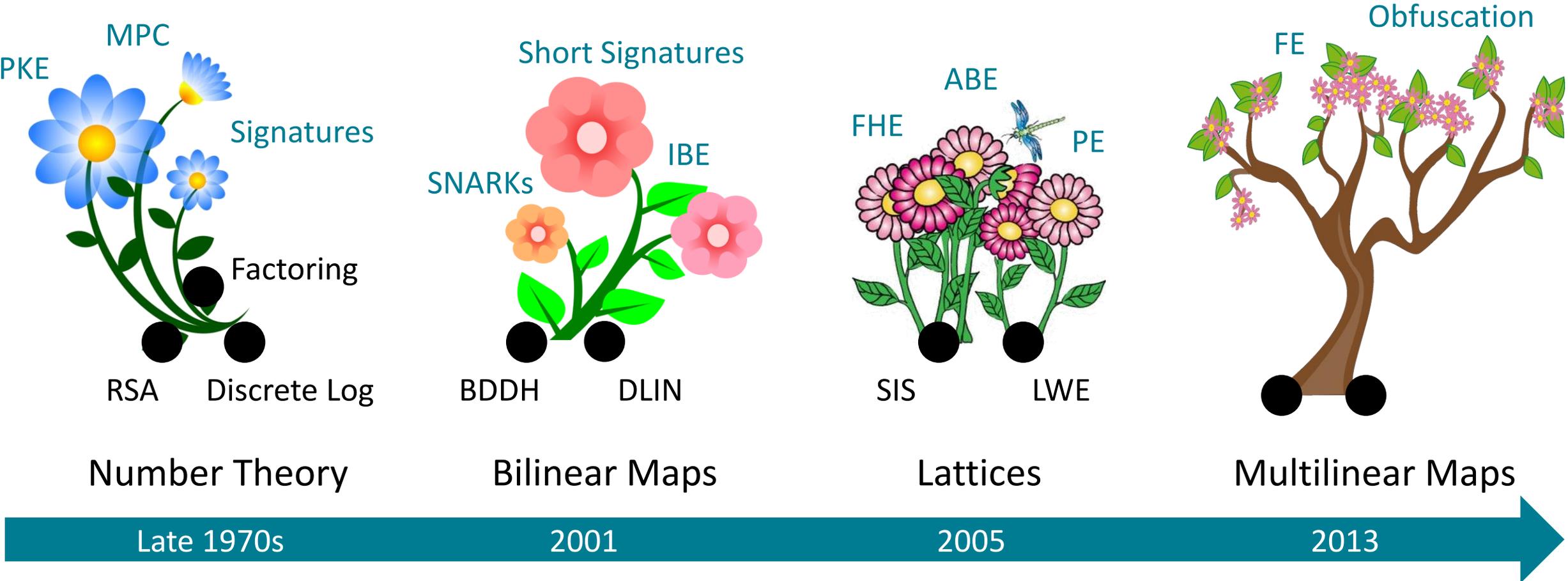
- Fundamental primitive to modern cryptography
- Important building block in many protocols (e.g., identification schemes, digital signatures, multiparty computation)

Succinctness: The proof is *significantly* shorter than $|C|$ (and correspondingly, $|w|$) [Kil92, Mic00, GW11]

- Natural complexity-theoretic question: what is the minimal communication complexity for proofs of NP statements?
- Numerous applications to delegating and verifying computations as well as privacy-preserving cryptocurrencies

But what if we want other properties?

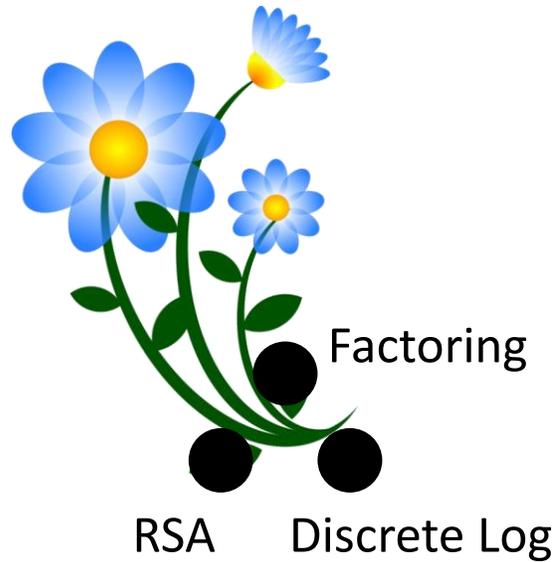
The Landscape of Modern Cryptography



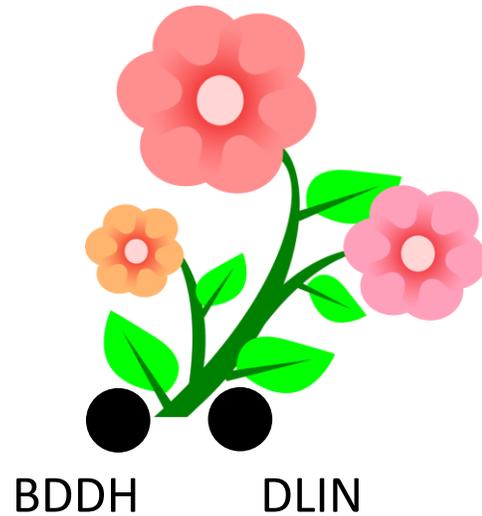
Cryptography is the study of hardness

[Slide inspired by Amit Sahai]

The Landscape of Modern Cryptography



Number Theory



Bilinear Maps



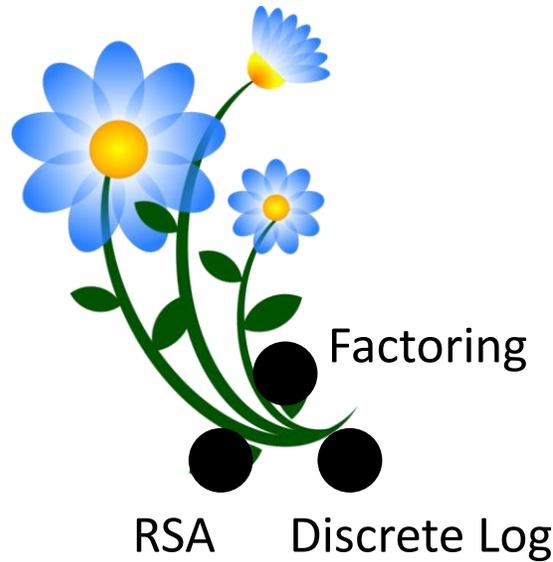
Lattices



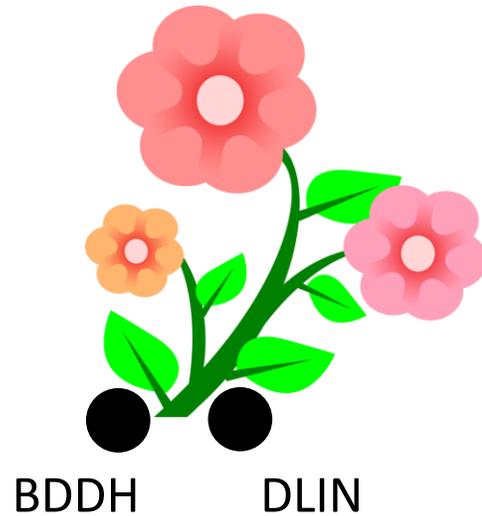
Which assumptions imply non-interactive zero-knowledge?

Which assumptions imply succinct non-interactive arguments?

The Landscape of Modern Cryptography



Number Theory



Bilinear Maps



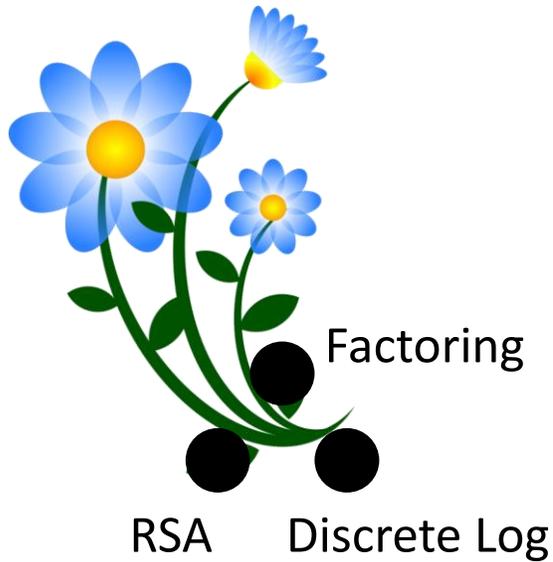
Lattices



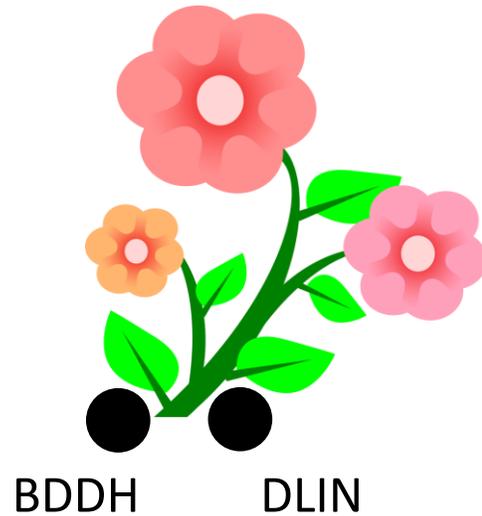
Which assumptions imply non-interactive zero-knowledge?

Which assumptions imply succinct non-interactive arguments?

This Work



Number Theory



Bilinear Maps



Lattices



Which assumptions imply non-interactive zero-knowledge?

* In a weaker preprocessing model

Which assumptions imply succinct non-interactive arguments?

This Work

Which assumptions imply non-interactive zero-knowledge?

Non-interactive zero-knowledge arguments from standard lattice assumptions in a *preprocessing* model [Kim-W; CRYPTO 2018]

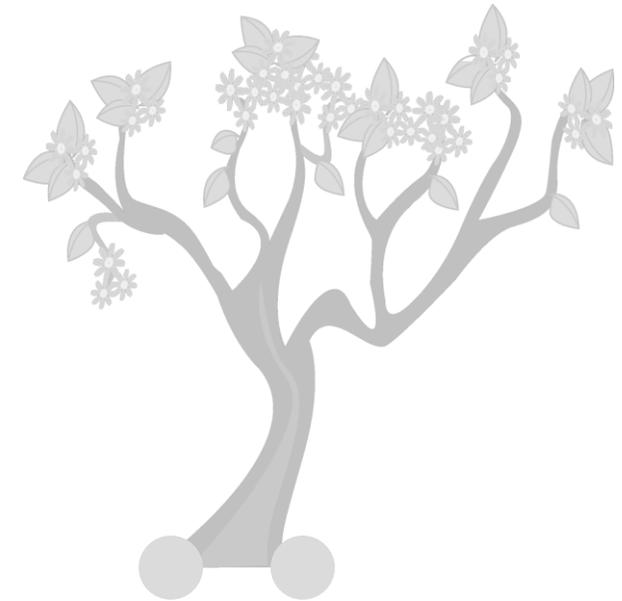
Which assumptions imply succinct non-interactive arguments?

Succinct non-interactive arguments (SNARGs) from lattice-based assumptions
[Boneh-Ishai-Sahai-W; EUROCRYPT 2017]

First construction of a quasi-optimal SNARG from lattice-based assumptions
[Boneh-Ishai-Sahai-W; EUROCRYPT 2018]

Focus of this talk

Why Lattices?



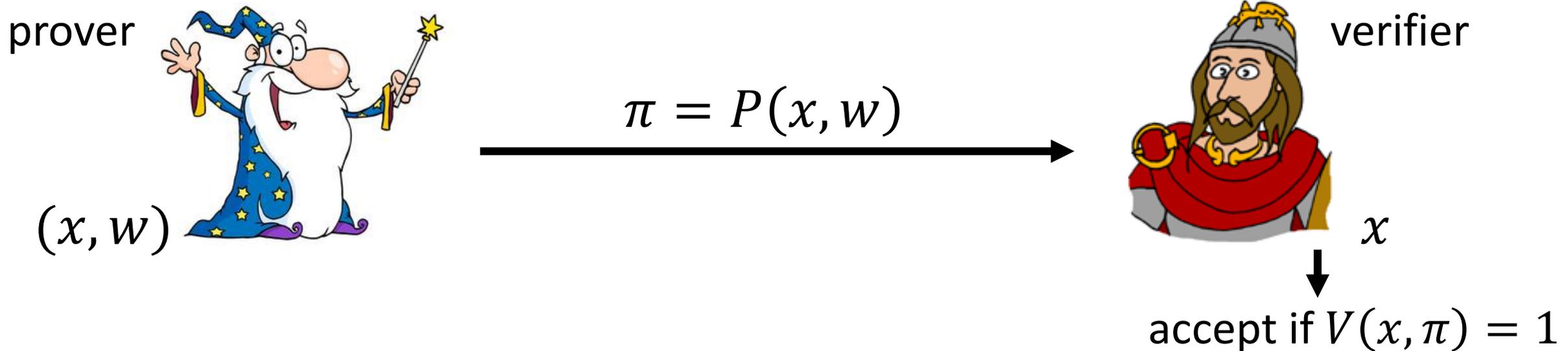
(Conjectured) post-quantum resilience
Diversifying cryptographic assumptions
Enable new properties (e.g., quasi-optimality)

Succinct Non-Interactive Arguments

Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$



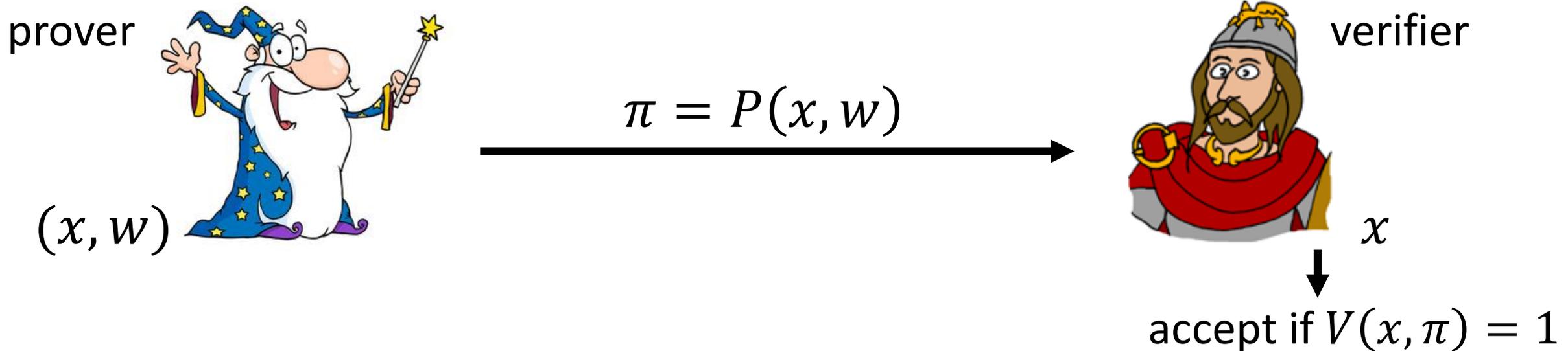
Completeness:

"Honest prover convinces honest verifier of true statements"

Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$



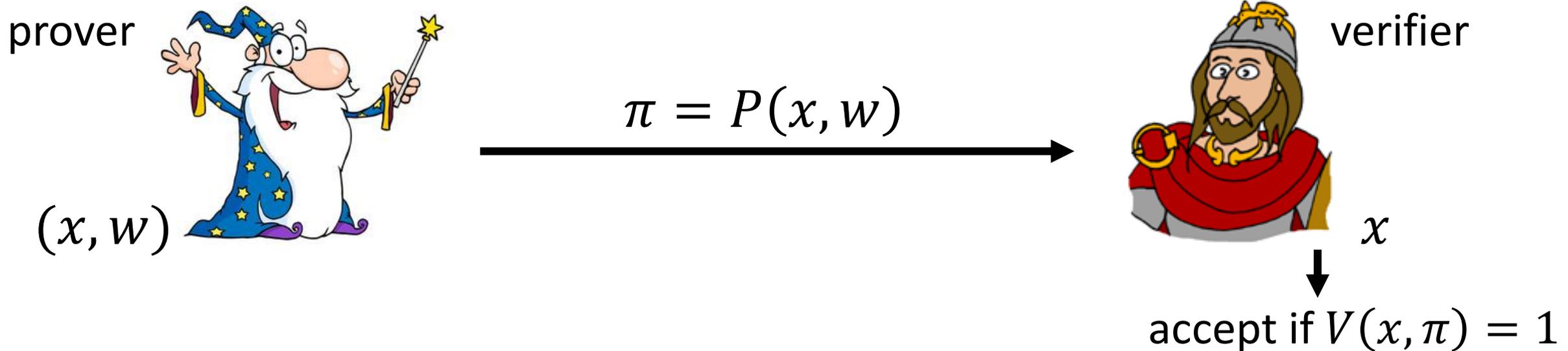
Completeness: $C(x, w) = 1 \Rightarrow \Pr[V(x, P(x, w)) = 1] = 1$

Soundness: *"No efficient prover can convince honest verifier of false statement"*

Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$



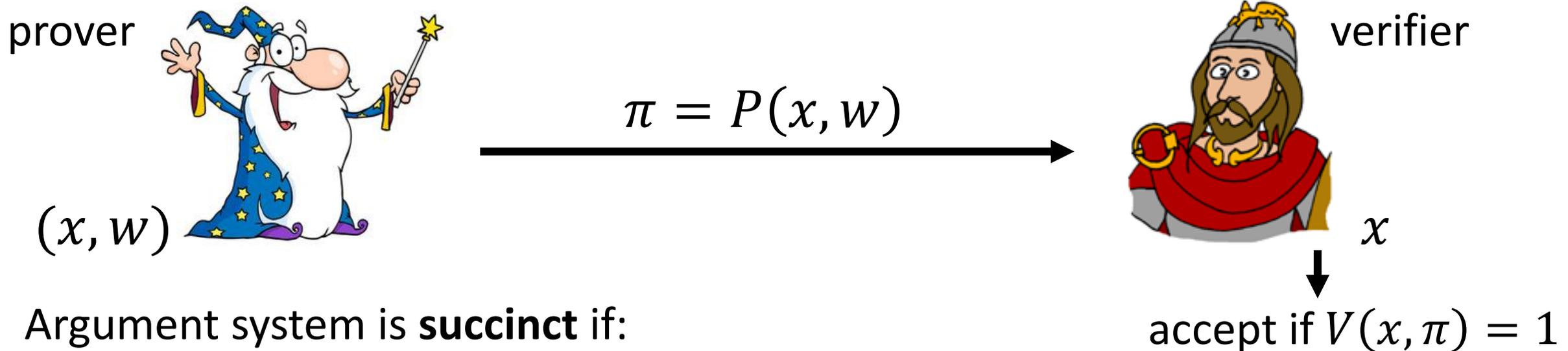
Completeness: $C(x, w) = 1 \Rightarrow \Pr[V(x, P(x, w)) = 1] = 1$

Soundness: for all provers P^* of size 2^λ (λ is a security parameter),
 $x \notin \mathcal{L}_C \Rightarrow \Pr[V(x, P^*(x)) = 1] \leq 2^{-\lambda}$

Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$



Argument system is **succinct** if:

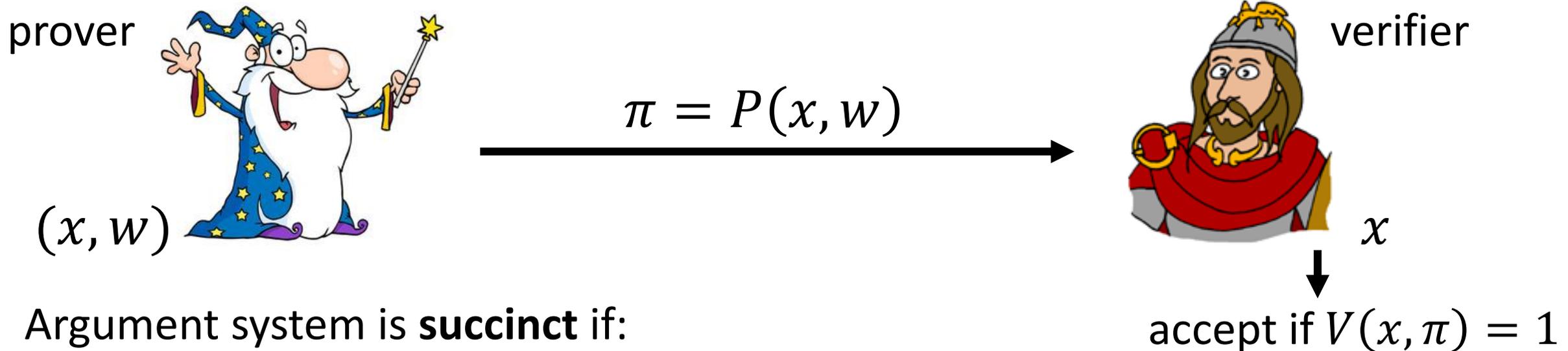
- Prover communication is $\text{poly}(\lambda + \log|C|)$
- V can be implemented by a circuit of size $\text{poly}(\lambda + |x| + \log|C|)$

Verifier complexity significantly smaller than classic NP verifier

Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

$$\mathcal{L}_C = \{x : C(x, w) = 1 \text{ for some } w\}$$



Argument system is **succinct** if:

- Prover communication is $\text{poly}(\lambda + \log|C|)$
- V can be implemented by a circuit of size $\text{poly}(\lambda + |x| + \log|C|)$

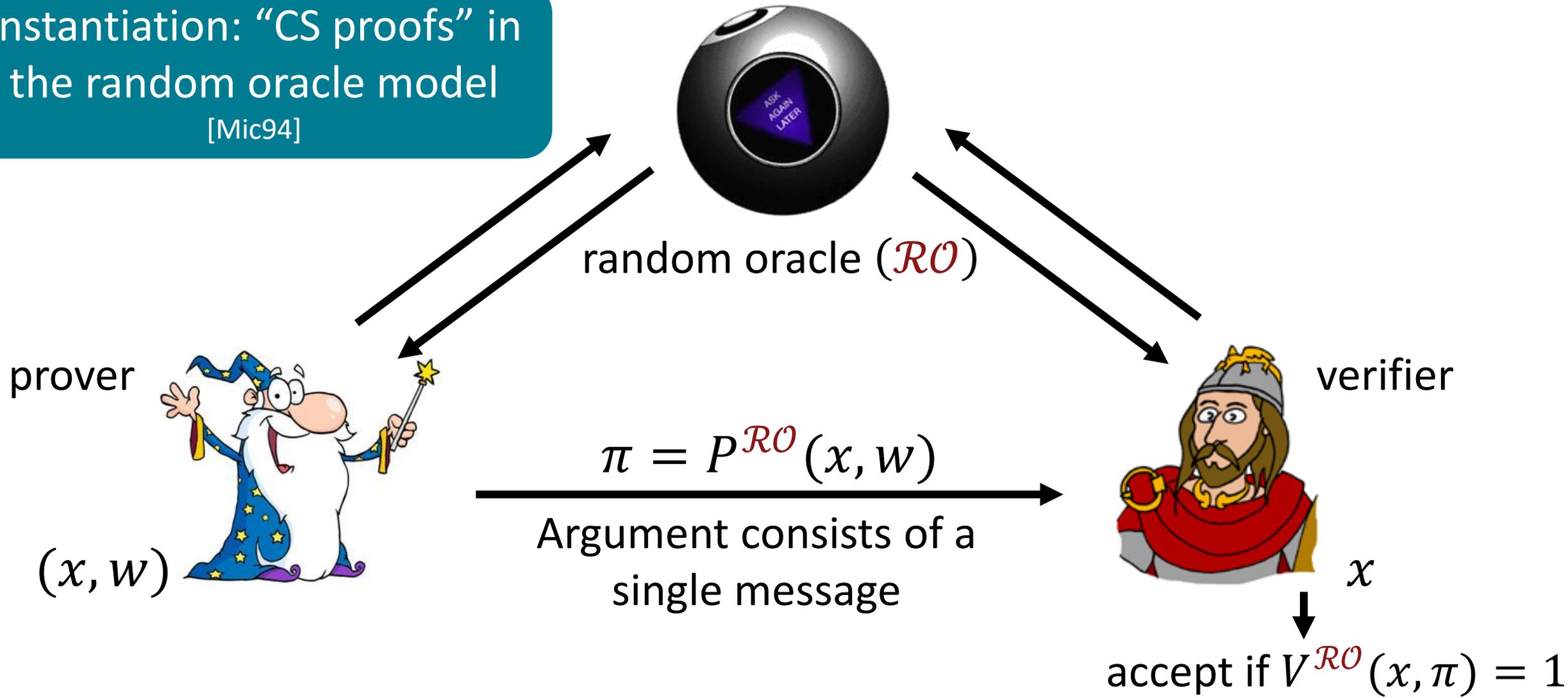
For general NP languages, succinct non-interactive arguments are unlikely to exist in the standard model [BP04, Wee05]

Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

Instantiation: "CS proofs" in
the random oracle model

[Mic94]



Succinct Non-Interactive Arguments (SNARGs)

[Kil92, Mic00, GW11]

Preprocessing SNARGs:
allow “expensive” setup

Setup(1^λ)



common reference
string (CRS)

verification
state



prover



(x, w)

$$\pi = P(\sigma, x, w)$$

Argument consists of a
single message

verifier



x

accept if $V(\tau, x, \pi) = 1$

Can consider publicly-
verifiable and secretly-
verifiable SNARGs

Complexity Metrics for SNARGs

Soundness: for all provers P^* of size 2^λ :

$$x \notin \mathcal{L}_C \implies \Pr[V(x, P^*(x)) = 1] \leq 2^{-\lambda}$$

How short can the proofs be?

$$|\pi| = \Omega(\lambda)$$

Even in the designated-verifier setting

How much work is needed to generate the proof?

$$|P| = \Omega(|C|)$$

Quasi-Optimal SNARGs

Soundness: for all provers P^* of size 2^λ :

$$x \notin \mathcal{L}_C \implies \Pr[V(x, P^*(x)) = 1] \leq 2^{-\lambda}$$

A SNARG (for Boolean circuit satisfiability) is quasi-optimal if it satisfies the following properties:

- Quasi-optimal succinctness:

$$|\pi| = \lambda \cdot \text{polylog}(\lambda, |C|) = \tilde{O}(\lambda)$$

- Quasi-optimal prover complexity:

$$|P| = \tilde{O}(|C|) + \text{poly}(\lambda, \log|C|)$$

Asymptotic Comparisons

Construction	Prover Complexity	Proof Size	Assumption
CS Proofs [Mic94]	$\tilde{O}(C)$	$\tilde{O}(\lambda^2)$	Random Oracle
Groth [Gro16]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Generic Group
Groth [Gro10]	$\tilde{O}(\lambda C ^2 + C \lambda^2)$	$\tilde{O}(\lambda)$	Knowledge of Exponent
GGPR [GGPR12]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Knowledge of Exponent
BCIOP (Pairing) [BCIOP13]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Linear-Only Encryption
This work (over integer lattices)	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Linear-Only Vector Encryption
This work (over ideal lattices)	$\tilde{O}(C)$	$\tilde{O}(\lambda)$	Linear-Only Vector Encryption

For simplicity, we ignore low order terms $\text{poly}(\lambda, \log|C|)$ in the prover complexity

Constructing (Quasi-Optimal) SNARGs

New framework for building preprocessing SNARGs (following [BCIOP13]):

Step 1 (information-theoretic):

- Identify useful information-theoretic building block (linear PCPs and linear MIPs)

Step 2 (cryptographic):

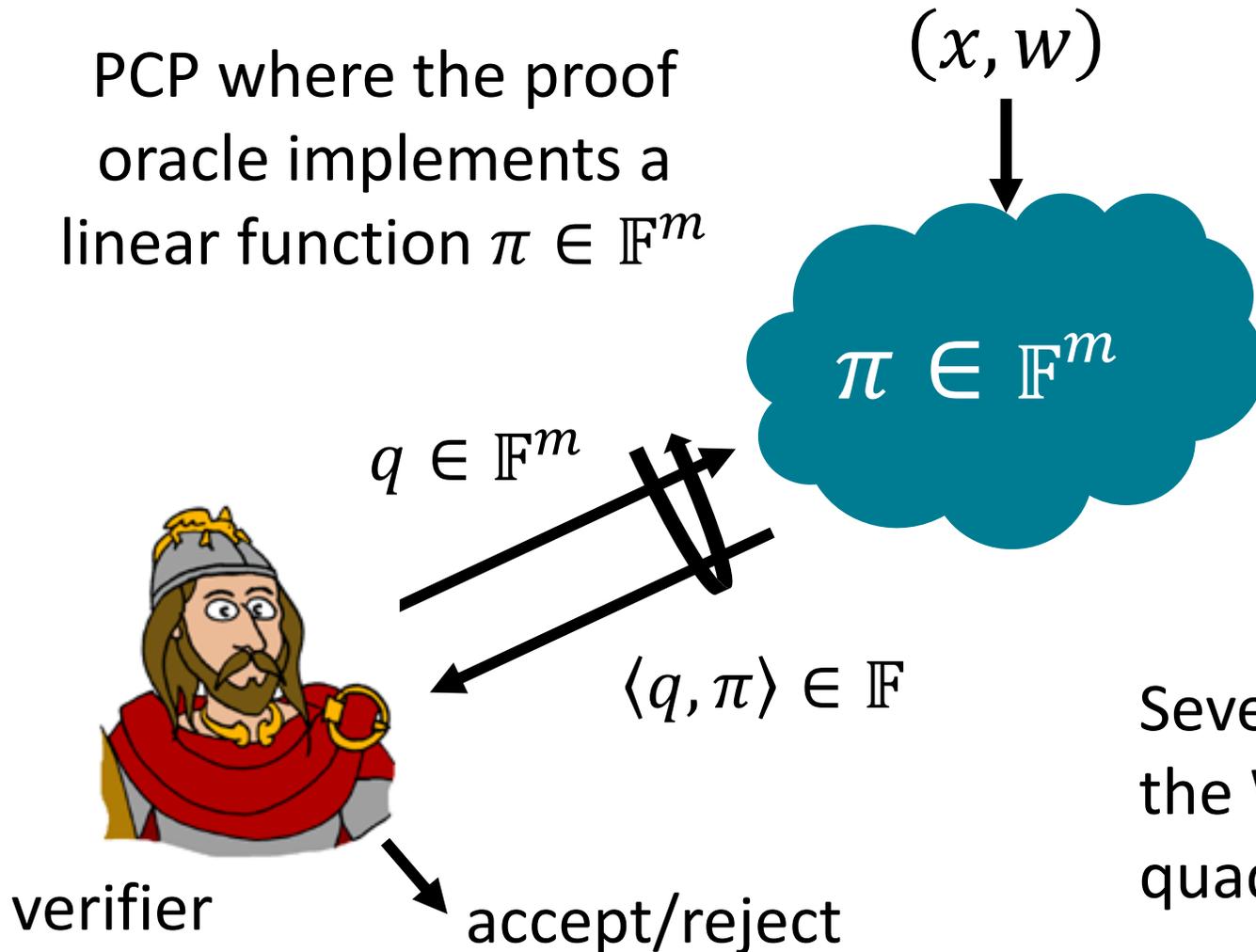
- Use cryptographic primitives to compile information-theoretic building block into a preprocessing SNARG

Instantiating our framework yields new lattice-based SNARG candidates

Linear PCPs

[IKO07]

PCP where the proof oracle implements a linear function $\pi \in \mathbb{F}^m$



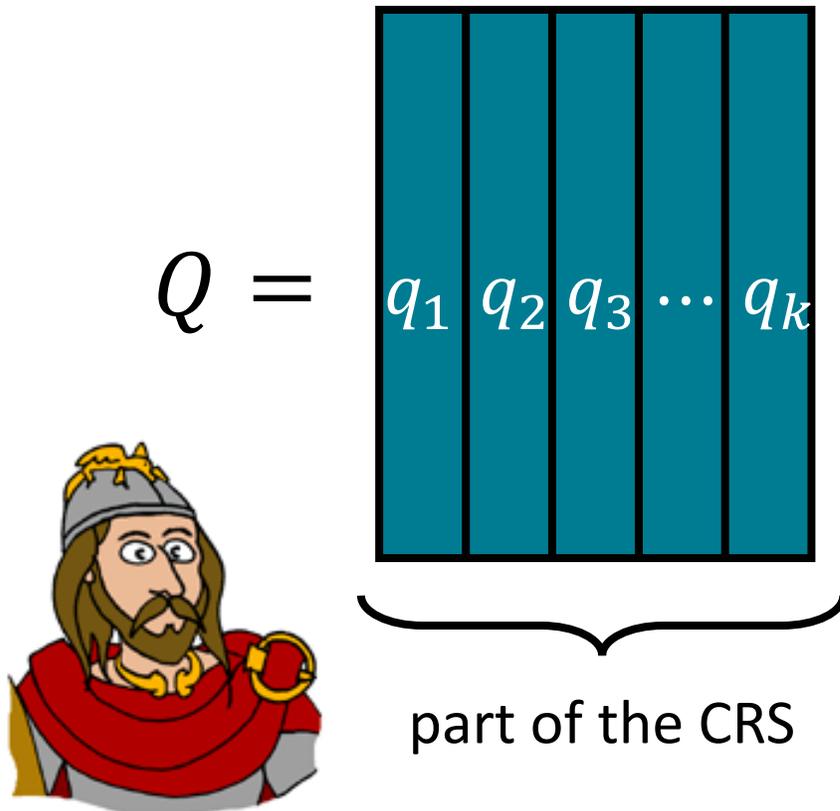
In these instantiations, verifier is oblivious (queries independent of statement)

Several possible instantiations: based on the Walsh-Hadamard code [ALMSS92] or quadratic span programs [GGPR13]

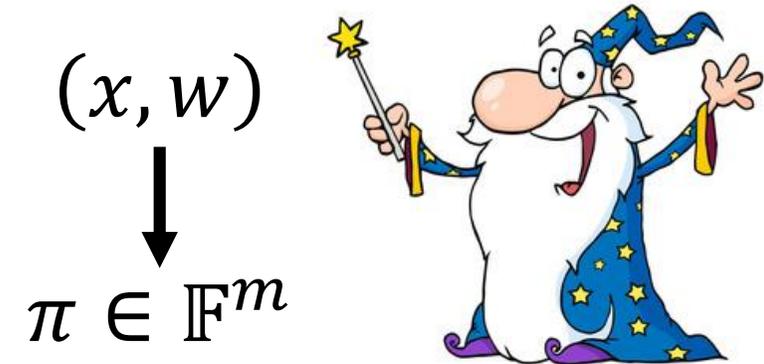
From Linear PCPs to SNARGs

[BCIOP13]

Oblivious verifier can “commit”
to its queries ahead of time



Prover constructs linear
PCP π from (x, w)



Prover computes responses
to linear PCP queries



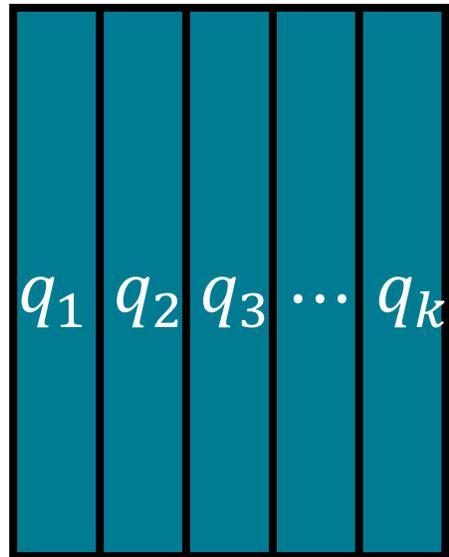
SNARG proof

From Linear PCPs to SNARGs

[BCIOP13]

Oblivious verifier can “commit”
to its queries ahead of time

$$Q =$$



part of the CRS

Two issues:

- Malicious prover can choose π based on the queries
- Malicious prover can apply different π to each query

Prover computes responses
to linear PCP queries



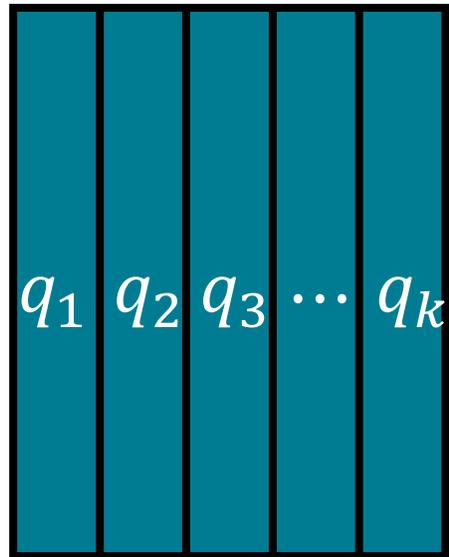
SNARG proof

From Linear PCPs to SNARGs

[BCIOP13]

Oblivious verifier can “commit”
to its queries ahead of time

$$Q =$$



part of the CRS



Two issues:

- Malicious prover can choose π based on the queries
- Malicious prover can apply different π to each query

Prover computes responses
to linear PCP queries

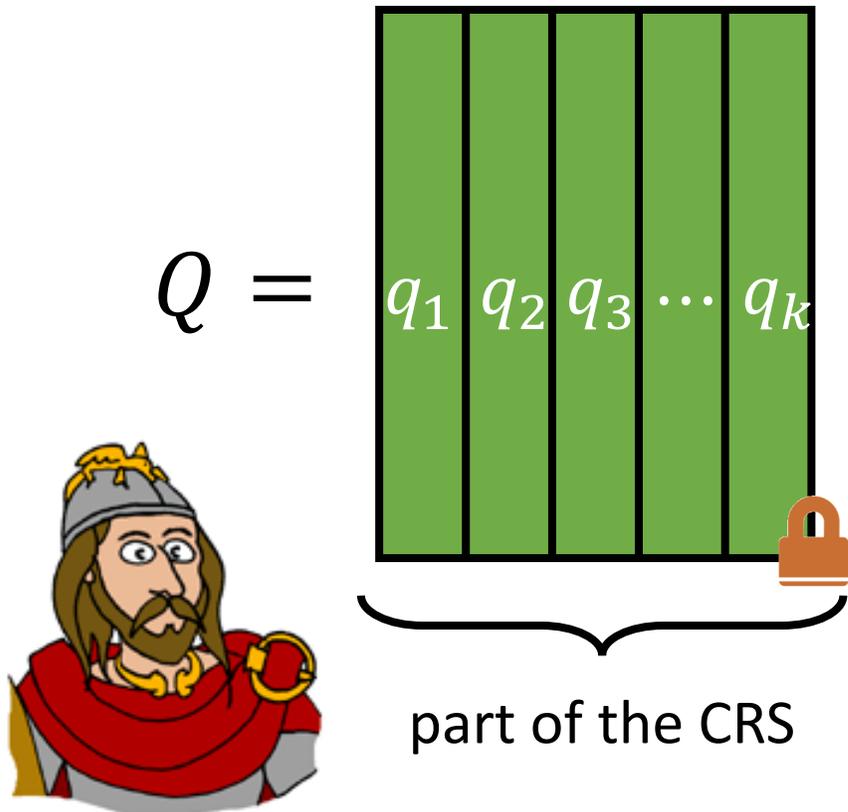


SNARG proof

From Linear PCPs to SNARGs

[BCIOP13]

Oblivious verifier can “commit”
to its queries ahead of time



Two issues:

- Malicious prover can choose π based on the queries
- Malicious prover can apply different π to each query

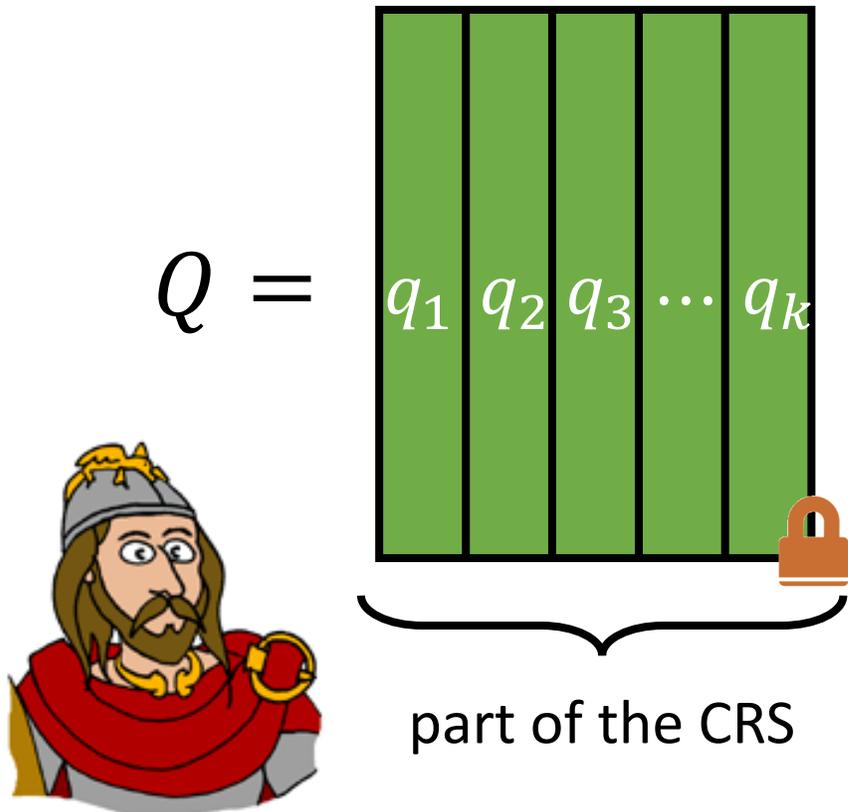
Step 1: Verifier encrypts its queries using an additively homomorphic encryption scheme

- Prover homomorphically computes $Q^T \pi$
- Verifier decrypts encrypted response vector and applies linear PCP verification

From Linear PCPs to SNARGs

[BCIOP13]

Oblivious verifier can “commit”
to its queries ahead of time



Two issues:

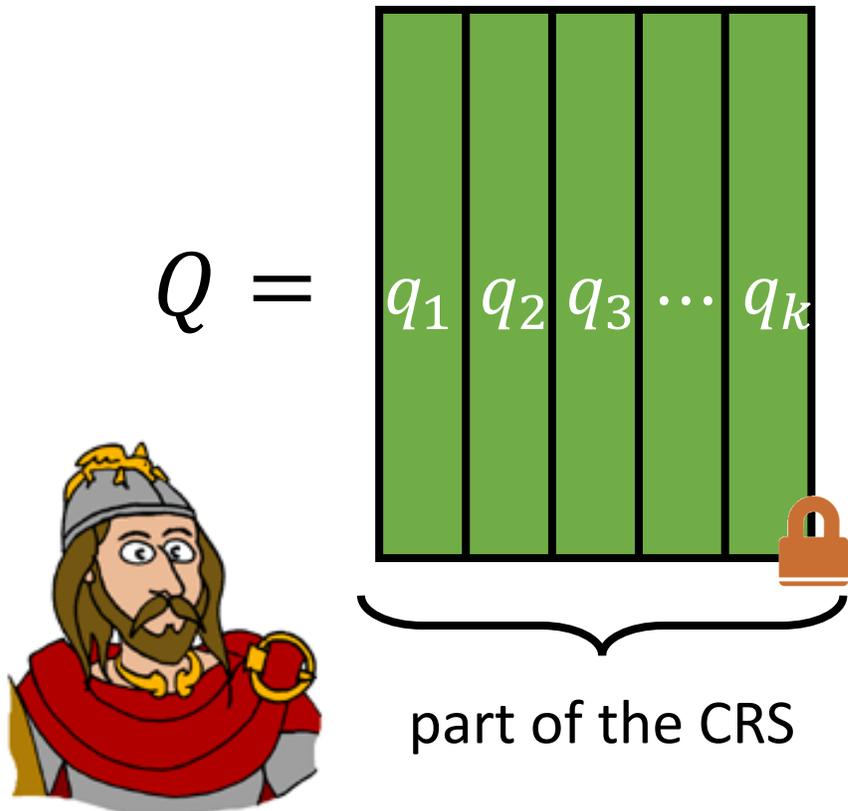
- Malicious prover can choose π based on the queries
- Malicious prover can apply different π to each query

Step 1: Verifier encrypts its queries using an additively homomorphic encryption scheme

- Prover homomorphically computes $Q^T \pi$
- Verifier decrypts encrypted response vector and applies linear PCP verification

From Linear PCPs to SNARGs

Oblivious verifier can “commit”
to its queries ahead of time



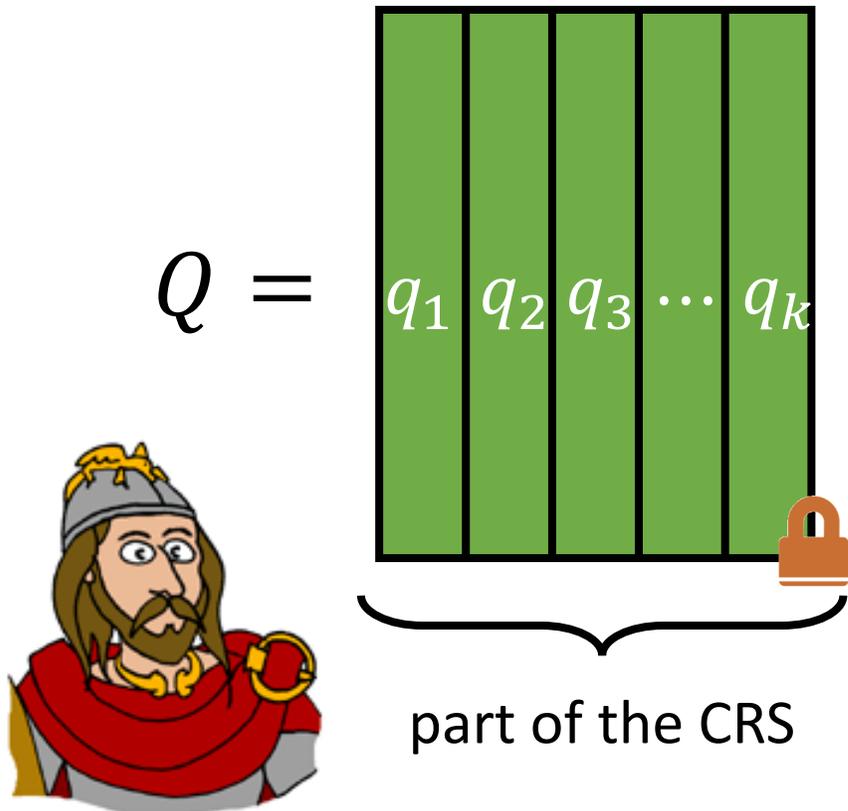
Two issues:

- Malicious prover can choose π based on the queries
- Malicious prover can apply different π to each query

Step 2: Conjecture that the encryption scheme only supports a limited subset of homomorphic operations (linear-only vector encryption)

From Linear PCPs to SNARGs

Oblivious verifier can “commit”
to its queries ahead of time



- Differs from [BCIOP13] compiler which relies on additional consistency checks to build a preprocessing SNARG
- Using linear-only vector encryption allows for efficient instantiation from lattices (resulting SNARG satisfies quasi-optimal succinctness)

Step 2: Conjecture that the encryption scheme only supports a limited subset of homomorphic operations (linear-only vector encryption)

Linear-Only Vector Encryption

$$v_1 \in \mathbb{F}^k$$

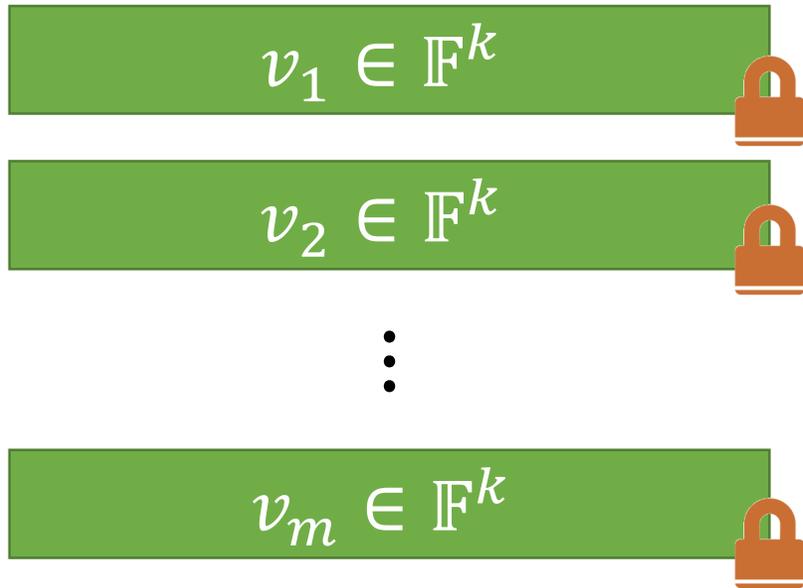
$$v_2 \in \mathbb{F}^k$$

⋮

$$v_m \in \mathbb{F}^k$$

plaintext space is a
vector space

Linear-Only Vector Encryption

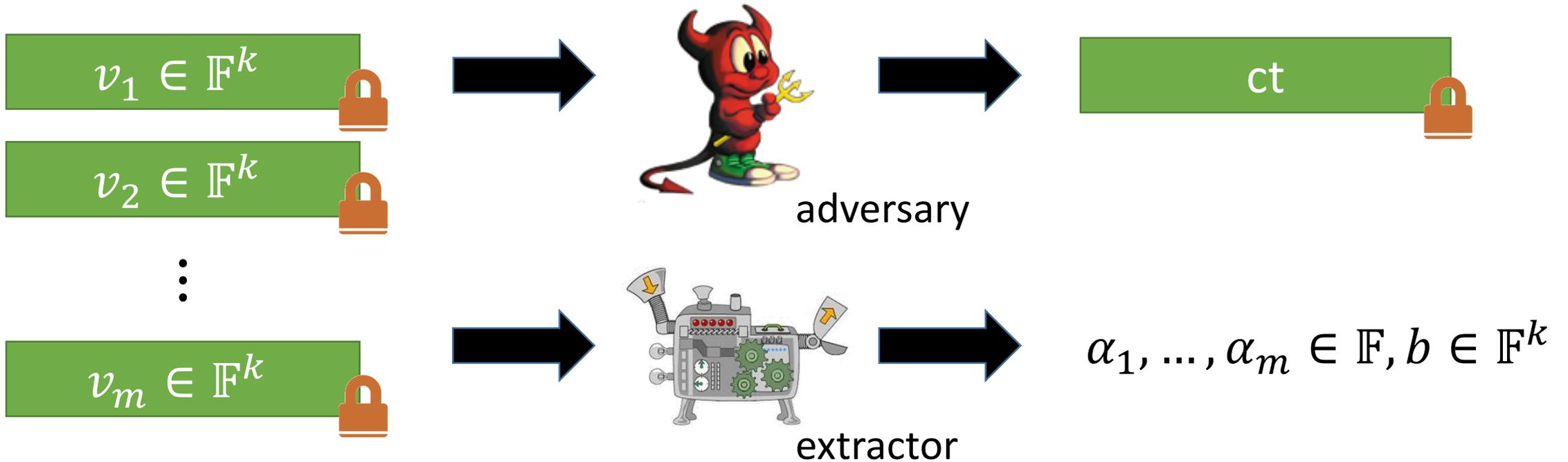


plaintext space is a
vector space



encryption scheme is
semantically-secure and
additively homomorphic

Linear-Only Vector Encryption

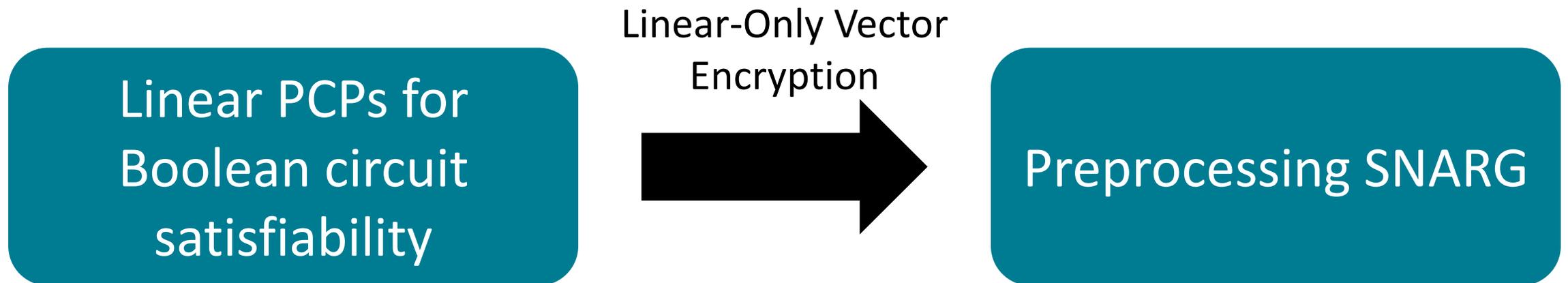


For all adversaries, there is an efficient extractor such that if ct is valid, then the extractor is able to produce a vector of coefficients $(\alpha_1, \dots, \alpha_m) \in \mathbb{F}^m$ and $b \in \mathbb{F}^k$ such that $\text{Decrypt}(\text{sk}, ct) = \sum_{i \in [n]} \alpha_i v_i + b$

[Weaker property also suffices]

Instantiating Linear-Only Vector Encryption

Conjecture: Regev encryption (specifically, variant of the [PVW08] scheme) based on lattices is a linear-only vector encryption scheme.



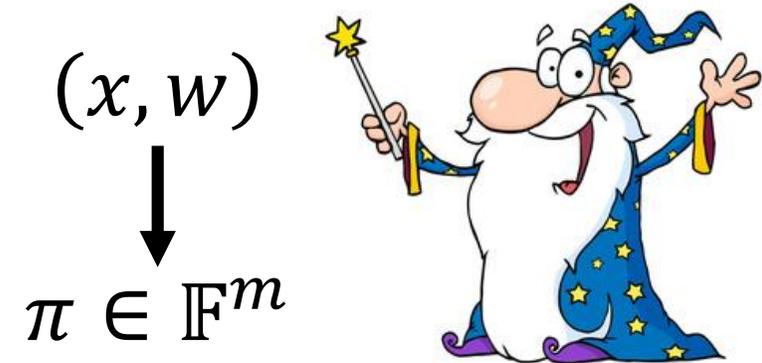
Complexity of the Construction

Evaluating inner product requires $\Omega(|C|)$ homomorphic operations;
prover complexity:
 $\Omega(\lambda) \cdot \Omega(|C|) = \Omega(\lambda|C|)$

$$Q = [q_1 \ q_2 \ q_3 \ \dots \ q_k]$$

Proof consists of a single
ciphertext: total length $O(\lambda)$ bits

Prover constructs linear
PCP π from (x, w)



Prover computes responses
to linear PCP queries



Asymptotic Comparisons

Construction	Prover Complexity	Proof Size	Assumption
CS Proofs [Mic94]	$\tilde{O}(C)$	$\tilde{O}(\lambda^2)$	Random Oracle
Groth [Gro16]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Generic Group
Groth [Gro10]	$\tilde{O}(\lambda C ^2 + C \lambda^2)$	$\tilde{O}(\lambda)$	Knowledge of Exponent
GGPR [GGPR12]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	
BCIOP (Pairing) [BCIOP13]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Linear-Only Encryption
This work (over integer lattices)	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Linear-Only Vector Encryption

For simplicity, we ignore low order terms $\text{poly}(\lambda, \log|C|)$ in the prover complexity

Towards Quasi-Optimality

Evaluating inner product requires $\Omega(|C|)$ homomorphic operations;
prover complexity:
 $\Omega(\lambda) \cdot \Omega(|C|) = \Omega(\lambda|C|)$

$$Q = [q_1 \mid q_2 \mid q_3 \mid \dots \mid q_k]$$

Proof consists of a constant
number of ciphertexts: total length
 $O(\lambda)$ bits

Prover constructs linear
PCP π from (x, w)



We pay $\Omega(\lambda)$ for each
homomorphic
operation. Can we
reduce this?



SNARG proof

Linear-Only Encryption over Rings

Consider encryption scheme over a polynomial ring $R_p = \mathbb{Z}_p[x]/\Phi_\ell(x) \cong \mathbb{F}_p^\ell$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_\ell \end{bmatrix} + \begin{bmatrix} x'_1 \\ x'_2 \\ x'_3 \\ \vdots \\ x'_\ell \end{bmatrix} = \begin{bmatrix} x_1 + x'_1 \\ x_2 + x'_2 \\ x_3 + x'_3 \\ \vdots \\ x_\ell + x'_\ell \end{bmatrix}$$

Homomorphic operations correspond to component-wise additions and scalar multiplications

Plaintext space can be viewed as a vector of field elements

Using RLWE-based encryption schemes, can encrypt $\ell = \tilde{O}(\lambda)$ field elements ($p = \text{poly}(\lambda)$) with ciphertexts of size $\tilde{O}(\lambda)$

Linear-Only Encryption over Rings

Consider encryption scheme over a polynomial ring $R_p = \mathbb{Z}_p[x]/\Phi_\ell(x) \cong \mathbb{F}_p^\ell$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ \vdots \\ x_\ell \end{bmatrix} + \begin{bmatrix} x'_1 \\ x'_2 \\ x'_3 \\ \vdots \\ x'_\ell \end{bmatrix} = \begin{bmatrix} x_1 + x'_1 \\ x_2 + x'_2 \\ x_3 + x'_3 \\ \vdots \\ x_\ell + x'_\ell \end{bmatrix}$$

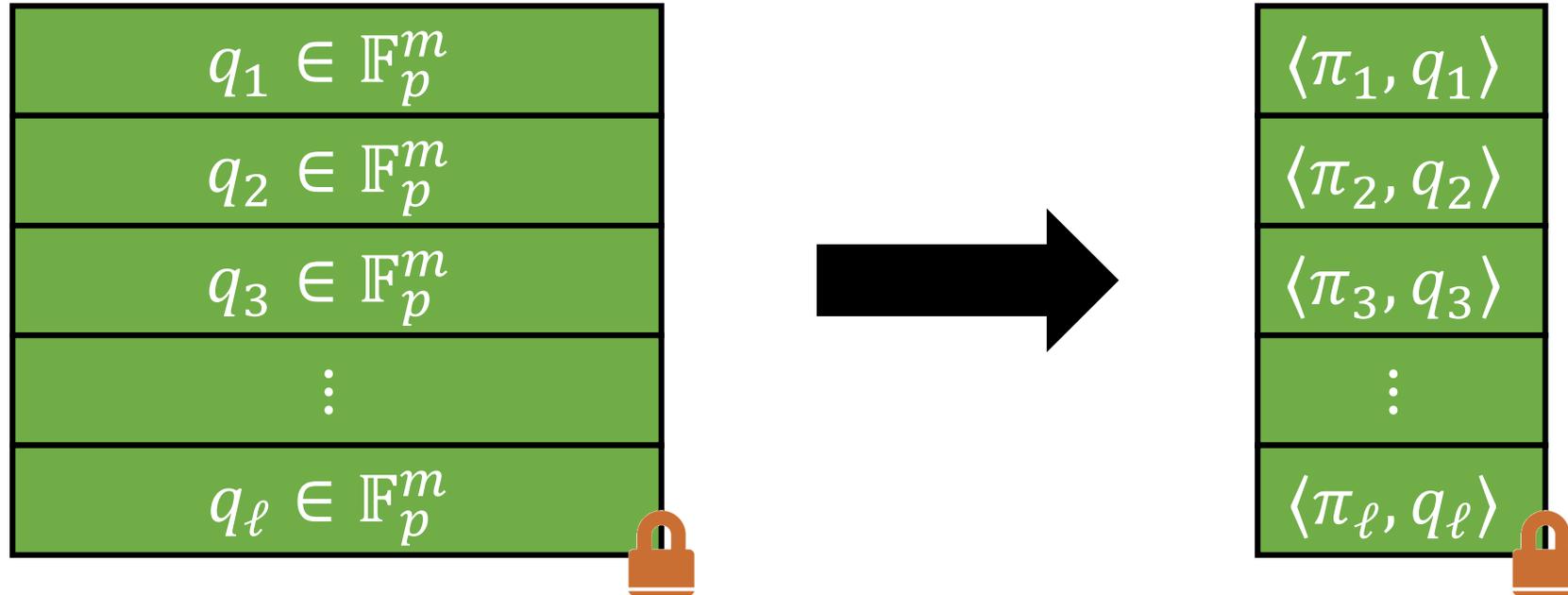
Homomorphic operations

Amortized cost of homomorphic operation on a single field element is $\text{polylog}(\lambda)$

Plaintext space can be viewed as a vector of field elements

Using RLWE-based encryption schemes, can encrypt $\ell = \tilde{O}(\lambda)$ field elements ($p = \text{poly}(\lambda)$) with ciphertexts of size $\tilde{O}(\lambda)$

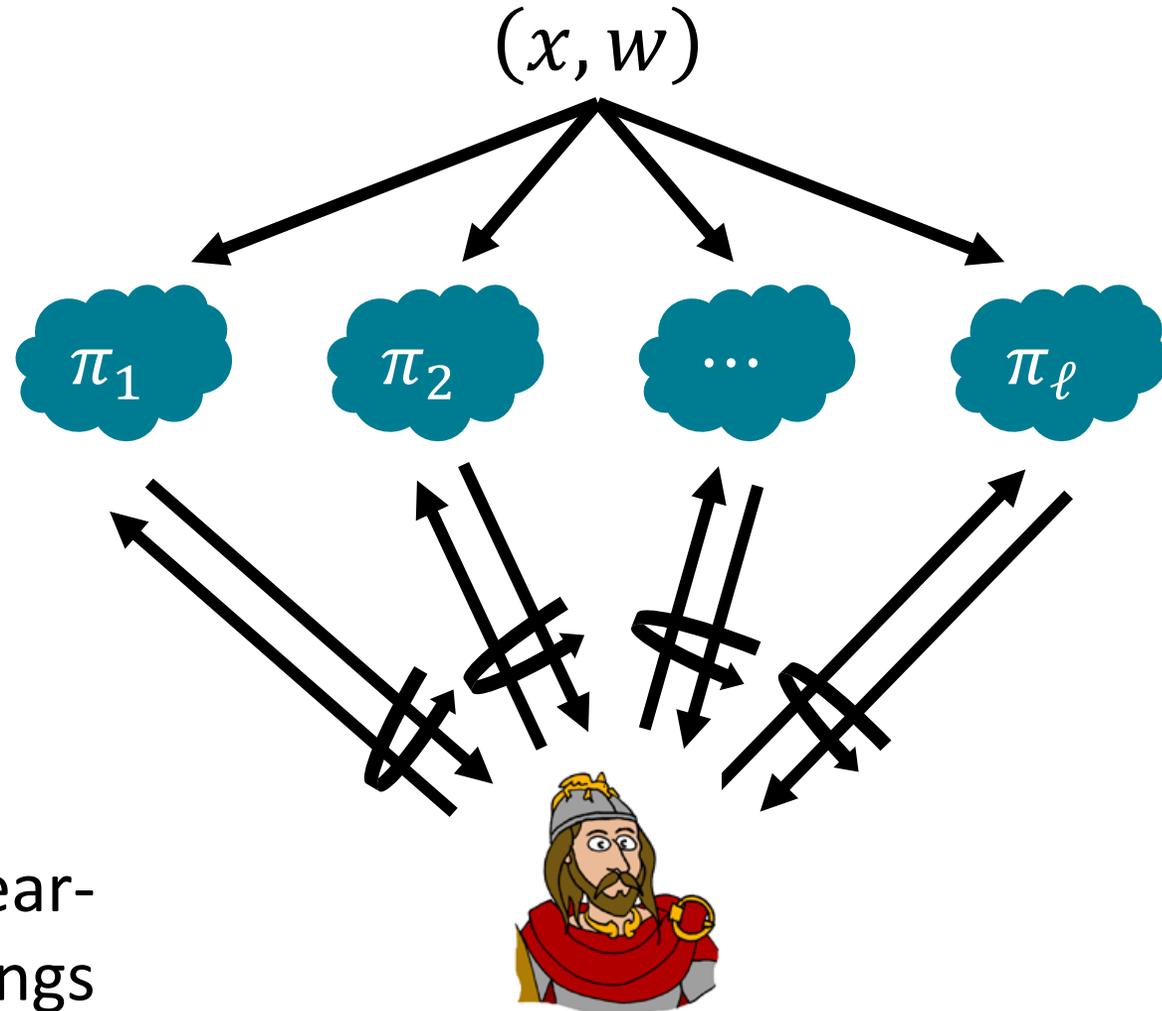
Linear-Only Encryption over Rings



Given encrypted set of query vectors, prover can homomorphically apply independent linear functions to each slot

Key idea: Check multiple independent proofs in parallel

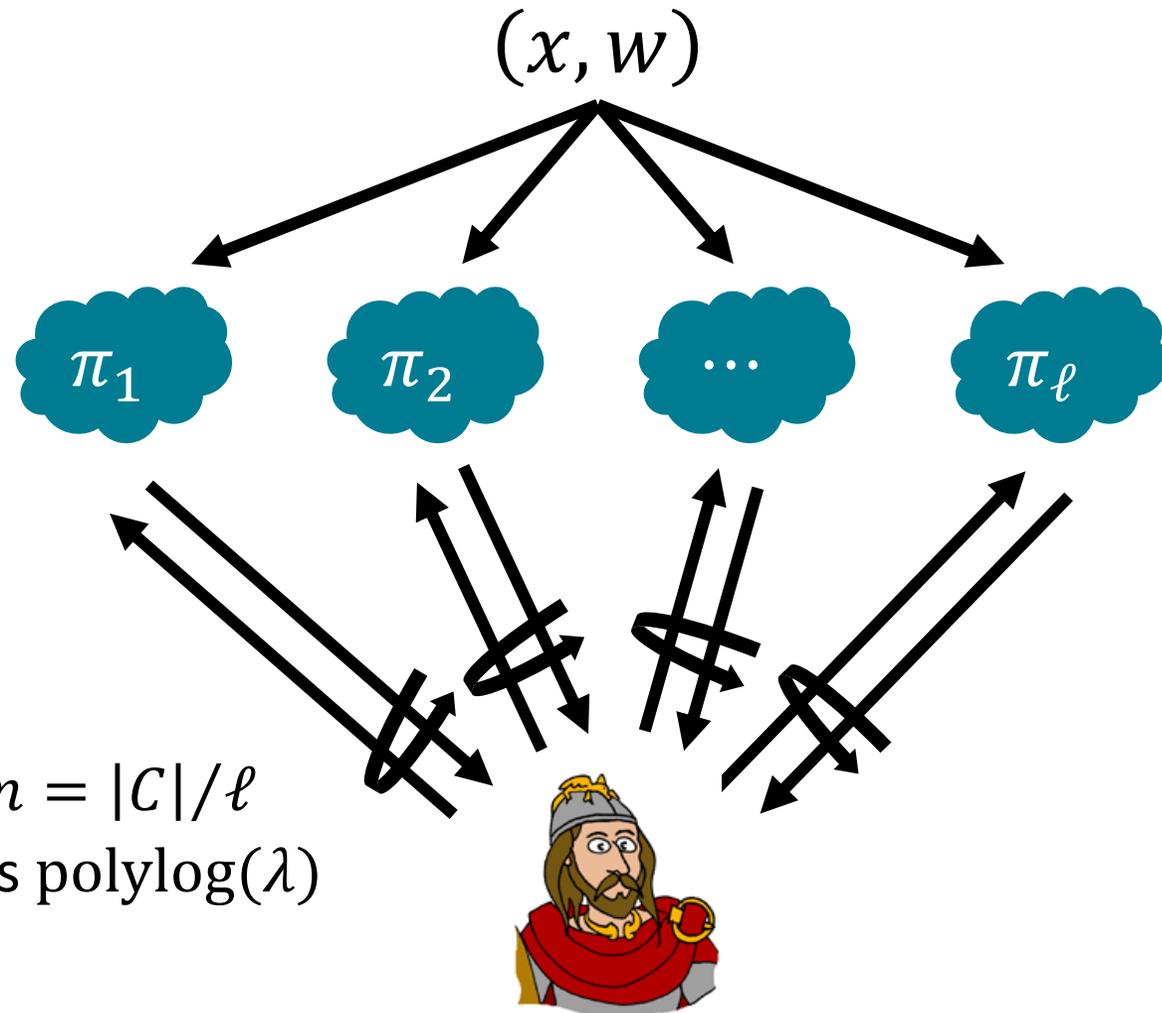
Linear Multi-Prover Interactive Proofs (MIPs)



Verifier has oracle access to multiple linear proof oracles
[Proofs may be correlated]

Can convert linear MIP to preprocessing SNARG using linear-only (vector) encryption over rings

Linear Multi-Prover Interactive Proofs (MIPs)



Suppose

- Number of provers $\ell = \tilde{O}(\lambda)$
- Proofs $\pi_1, \dots, \pi_\ell \in \mathbb{F}_p^m$ where $m = |C|/\ell$
- Number of queries to each π_i is $\text{polylog}(\lambda)$

Then, linear MIP is quasi-optimal

Linear Multi-Prover Interactive Proofs (MIPs)



Prover complexity:

$$\tilde{O}(\ell m) = \tilde{O}(|C|)$$

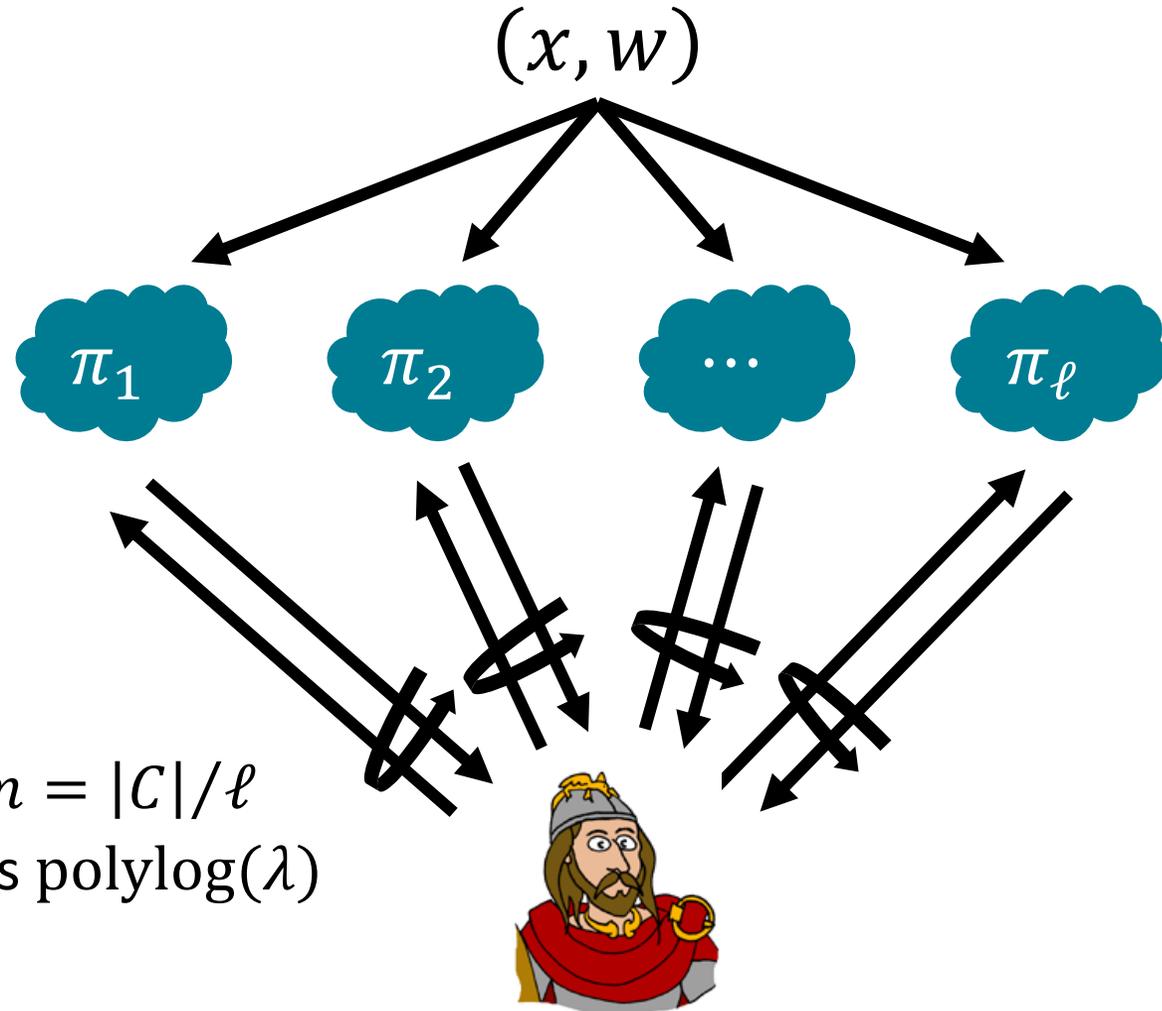
Linear MIP size:

$$O(\ell \cdot \text{polylog}(\lambda)) = \tilde{O}(\lambda)$$

Suppose

- Number of provers $\ell = \tilde{O}(\lambda)$
- Proofs $\pi_1, \dots, \pi_\ell \in \mathbb{F}_p^m$ where $m = |C|/\ell$
- Number of queries to each π_i is $\text{polylog}(\lambda)$

Then, linear MIP is quasi-optimal

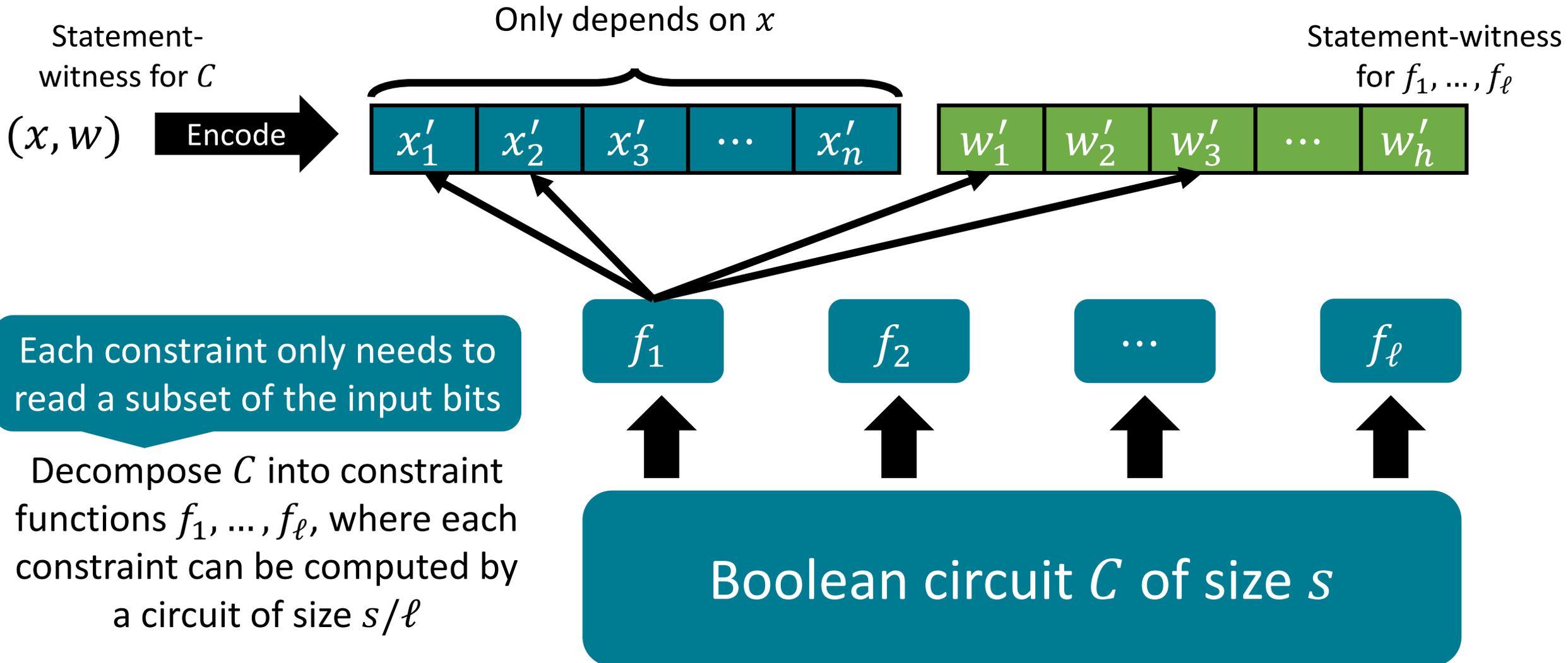


Quasi-Optimal Linear MIPs

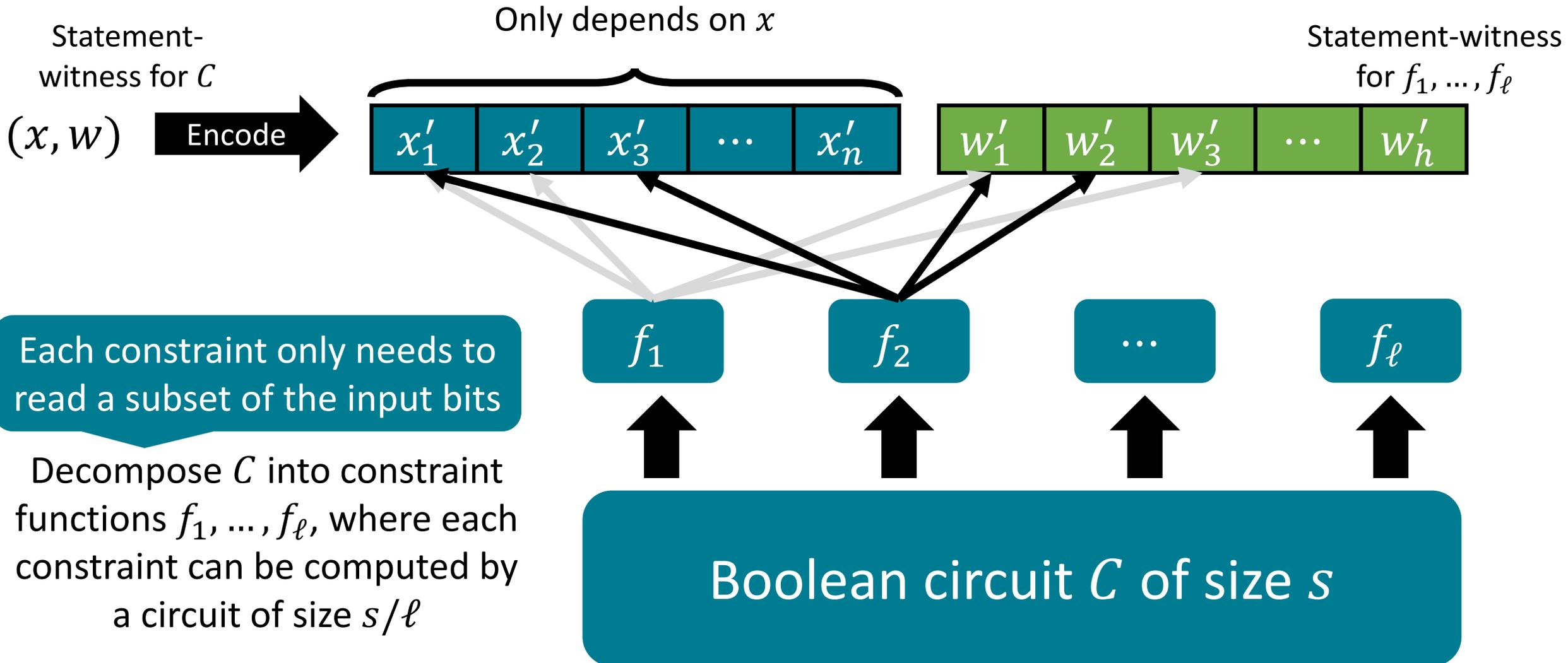
This work: Construction of a quasi-optimal linear MIP for Boolean circuit satisfiability



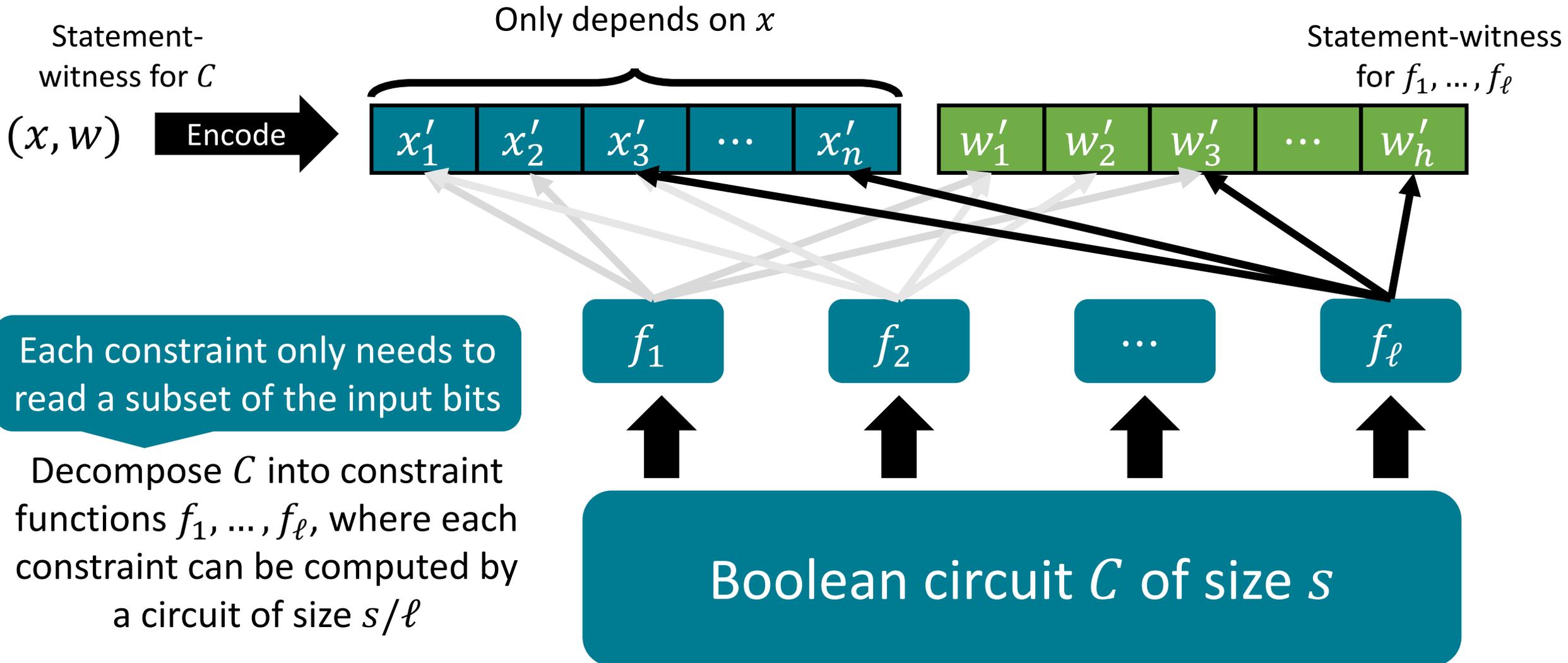
Robust Decomposition



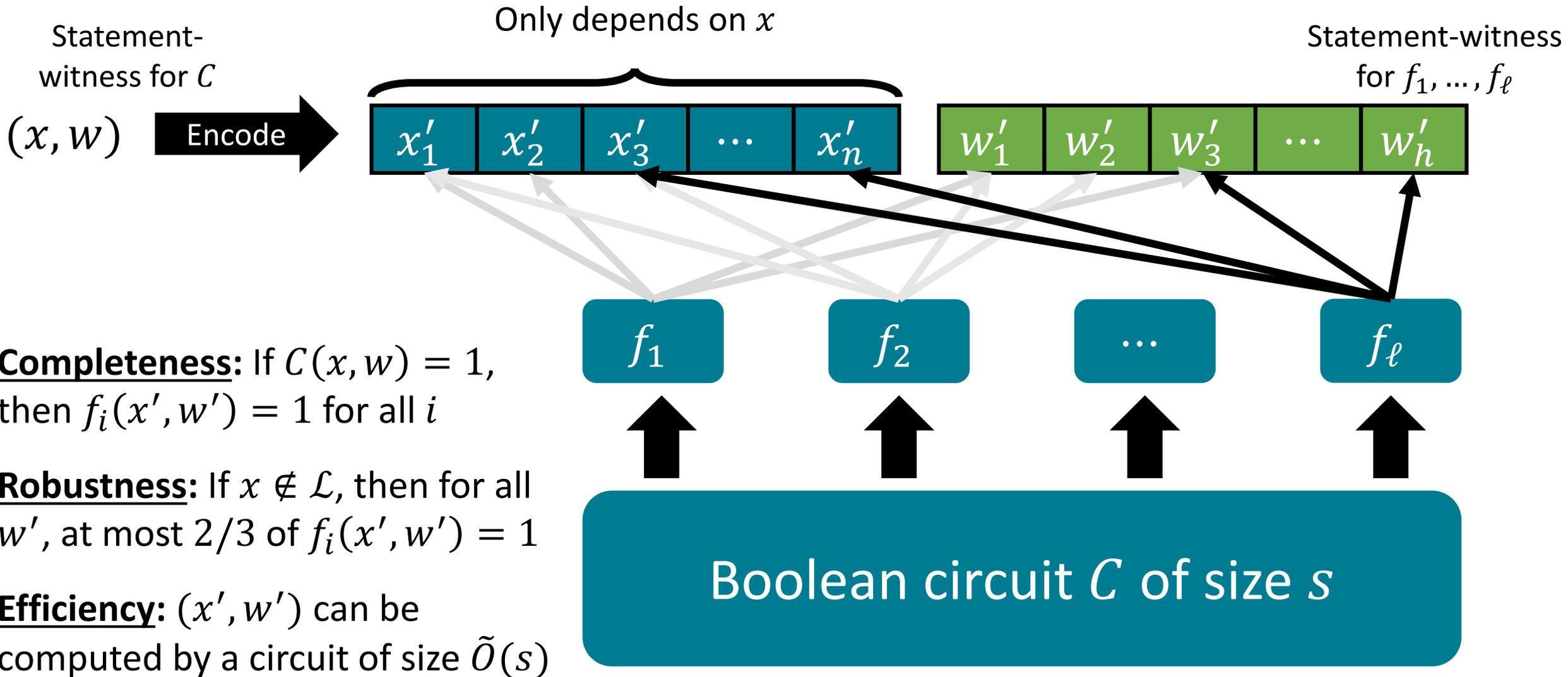
Robust Decomposition



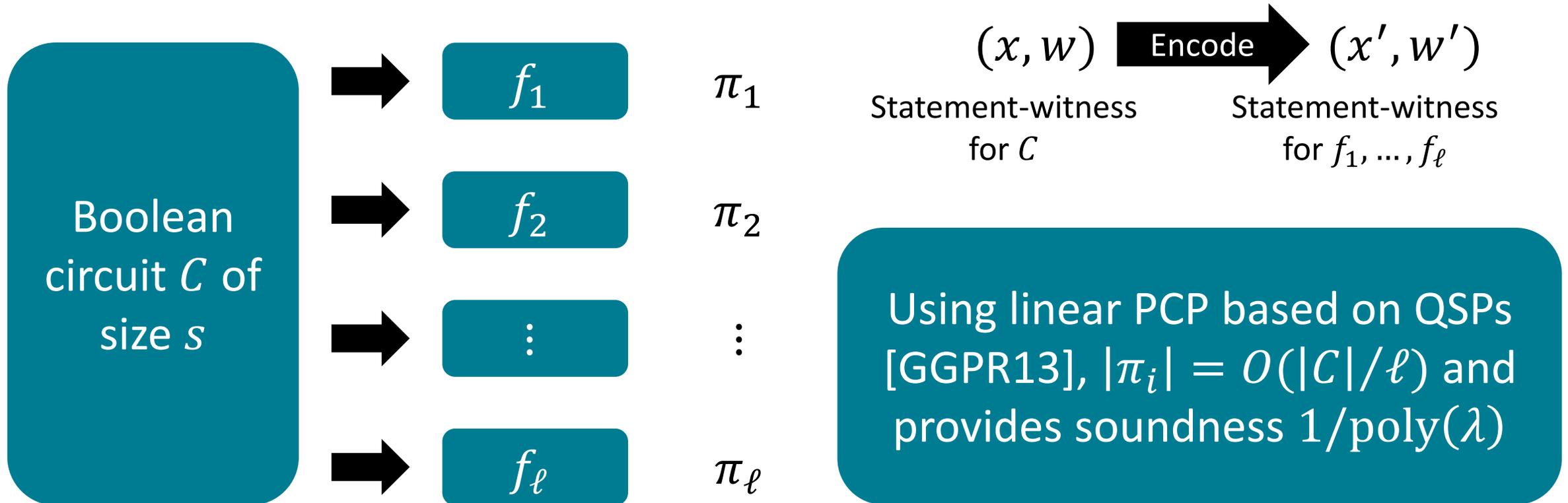
Robust Decomposition



Robust Decomposition

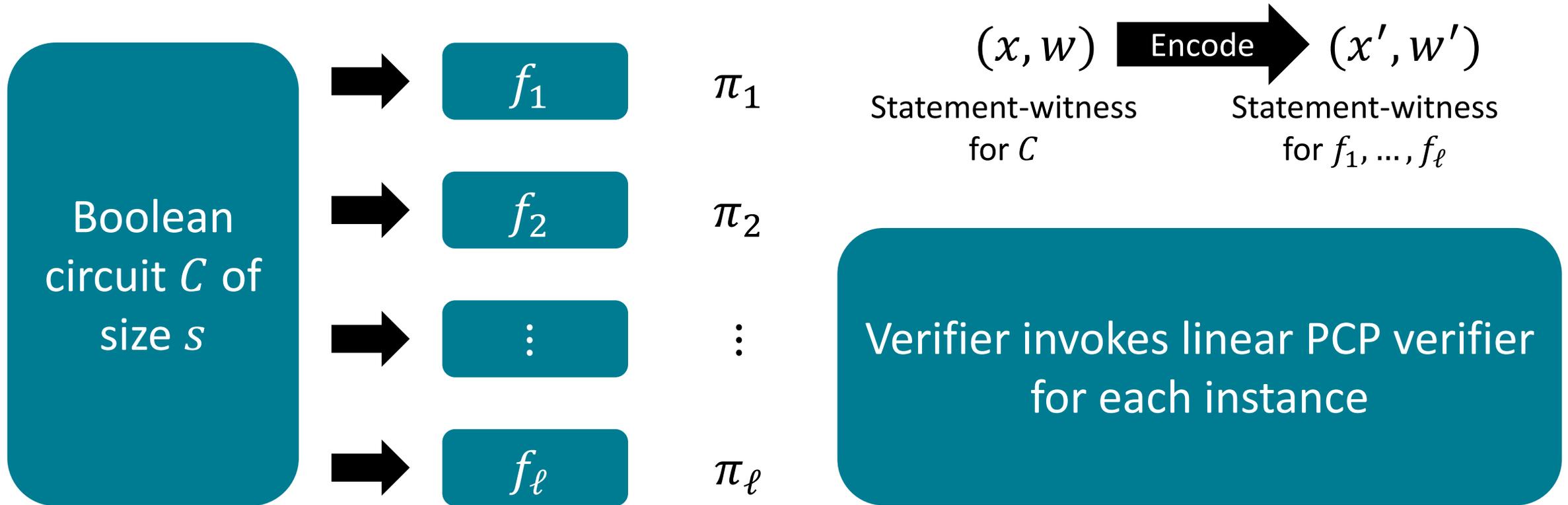


Robust Decomposition



π_i : linear PCP that $f_i(x', \cdot)$ is satisfiable
(instantiated over \mathbb{F}_p where $p = \text{poly}(\lambda)$)

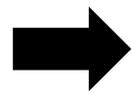
Robust Decomposition



π_i : linear PCP that $f_i(x', \cdot)$ is satisfiable
(instantiated over \mathbb{F}_p where $p = \text{poly}(\lambda)$)

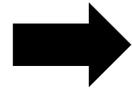
Robust Decomposition

Boolean
circuit C of
size s



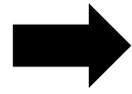
f_1

π_1



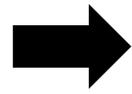
f_2

π_2



\vdots

\vdots



f_ℓ

π_ℓ

Completeness: Follows by completeness of decomposition and linear PCPs

Soundness: Each linear PCP provides $1/\text{poly}(\lambda)$ soundness and for false statement, at least $1/3$ of the statements are false, so if $\ell = \Omega(\lambda)$, verifier accepts with probability $2^{-\Omega(\lambda)}$

π_i : linear PCP that $f_i(x', \cdot)$ is satisfiable
(instantiated over \mathbb{F}_p where $p = \text{poly}(\lambda)$)

Robust Decomposition

Robustness: If $x \notin \mathcal{L}$, then for all w' , at most $2/3$ of $f_i(x', w') = 1$

For false x , no single w' can simultaneously satisfy $f_i(x', \cdot)$; however, all of the $f_i(x', \cdot)$ could individually be satisfiable

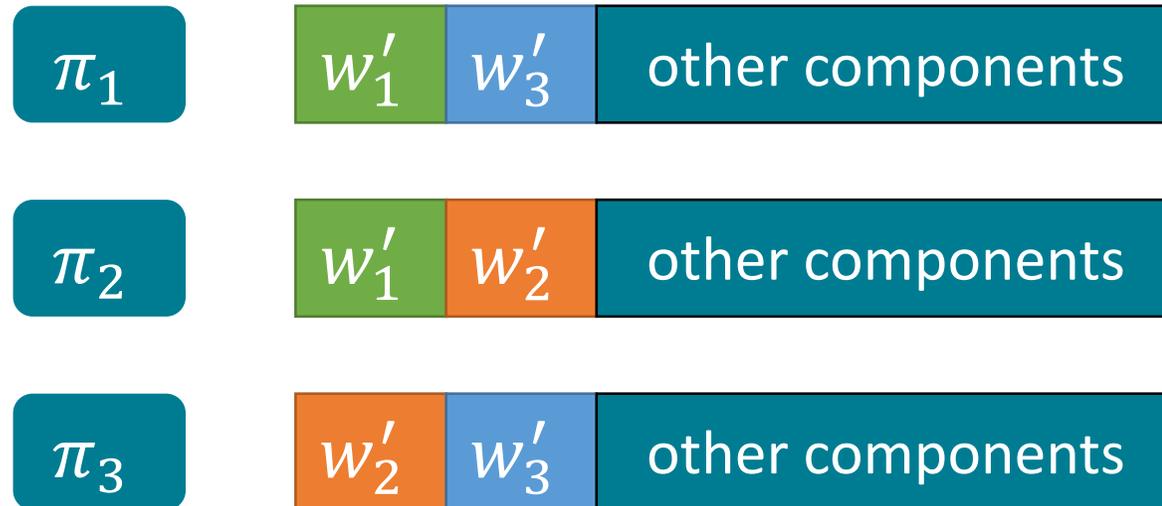
Completeness: Follows by completeness of decomposition and linear PCPs

Soundness: Each linear PCP provides $1/\text{poly}(\lambda)$ soundness and for false statement, at least $1/3$ of the statements are false, so if $\ell = \Omega(\lambda)$, verifier accepts with probability $2^{-\Omega(\lambda)}$

Problematic however if prover uses different (x', w') to construct proofs for different f_i 's

Consistency Checking

Require that linear PCPs are systematic: linear PCP π contains a copy of the witness:



Goal: check that assignments to w' are consistent via linear queries to π_i

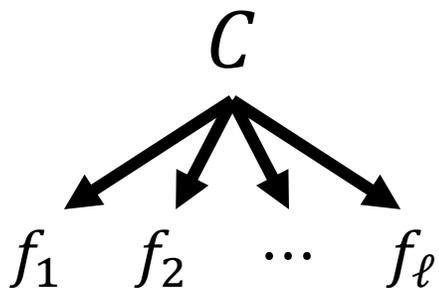
First few components of proof correspond to witness associated with the statement



Each proof induces an assignment to a few bits of the common witness w'

Quasi-Optimal Linear MIP

Robust Decomposition

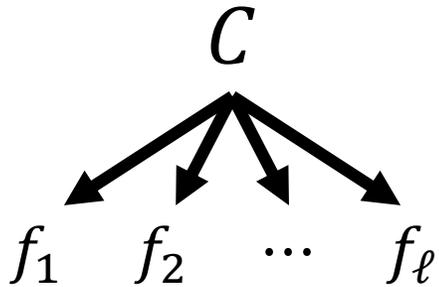


- Checking satisfiability of C corresponds to checking satisfiability of f_1, \dots, f_ℓ (each of which can be checked by a circuit of size $|C|/\ell$)
- For a false statement, no single witness can simultaneously satisfy more than a constant fraction of f_i

Robust decomposition can be instantiated by combining “MPC-in-the-head” paradigm [IKOS07] with a robust MPC protocol with polylogarithmic overhead [DIK10]

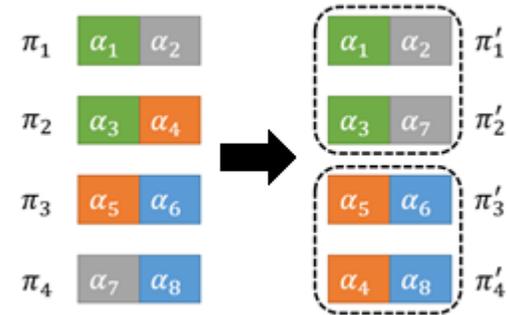
Quasi-Optimal Linear MIP

Robust Decomposition



- Checking satisfiability of C corresponds to checking satisfiability of f_1, \dots, f_ℓ (each of which can be checked by a circuit of size $|C|/\ell$)
- For a false statement, no single witness can simultaneously satisfy more than a constant fraction of f_i

Consistency Check



- Check that consistent witness is used to prove satisfiability of each f_i
- Relies on pairwise consistency checks and permuting the entries to obtain a "nice" replication structure

Asymptotic Comparisons

Construction	Prover Complexity	Proof Size	Assumption
CS Proofs [Mic94]	$\tilde{O}(C)$	$\tilde{O}(\lambda^2)$	Random Oracle
Groth [Gro16]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Generic Group
Groth [Gro10]	$\tilde{O}(\lambda C ^2 + C \lambda^2)$	$\tilde{O}(\lambda)$	Knowledge of Exponent
GGPR [GGPR12]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Knowledge of Exponent
BCIOP (Pairing) [BCIOP13]	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Linear-Only Encryption
This work (over integer lattices)	$\tilde{O}(\lambda C)$	$\tilde{O}(\lambda)$	Linear-Only Vector Encryption
This work (over ideal lattices)	$\tilde{O}(C)$	$\tilde{O}(\lambda)$	Linear-Only Vector Encryption

For simplicity, we ignore low order terms $\text{poly}(\lambda, \log|C|)$ in the prover complexity

Conclusions

A SNARG is quasi-optimal if it satisfies the following properties:

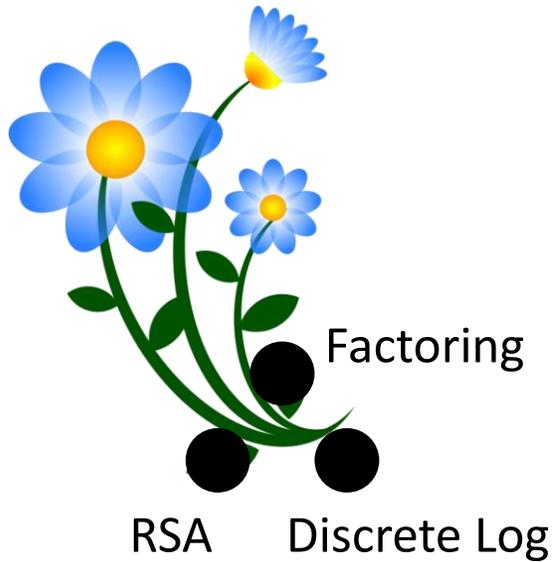
- Quasi-optimal succinctness: $|\pi| = \tilde{O}(\lambda)$
- Quasi-optimal prover complexity: $|P| = \tilde{O}(|C|) + \text{poly}(\lambda, \log|C|)$

New framework for building SNARGs by combining linear PCPs (and linear MIPs) with linear-only vector encryption

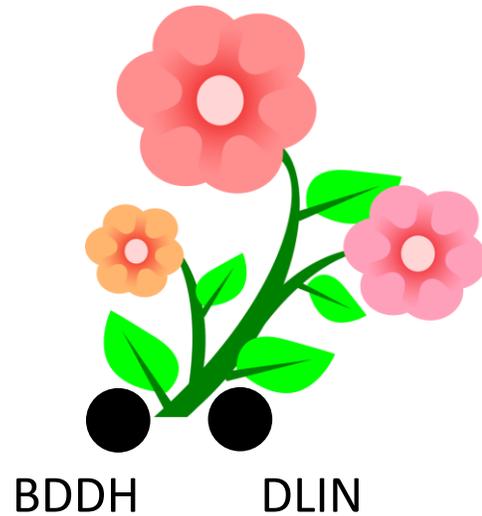
Framework yields first quasi-optimal SNARG by combining quasi-optimal linear MIP with linear-only vector encryption

- Construction of a quasi-optimal linear MIP possible by combining robust decomposition and consistency check

Summary



Number Theory



Bilinear Maps



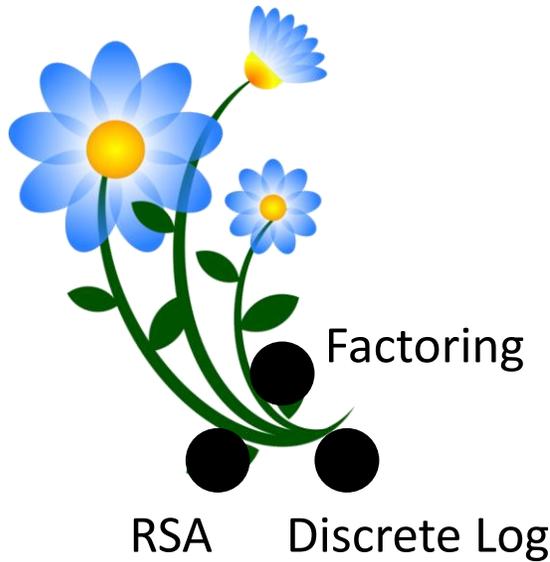
Lattices



Which assumptions imply non-interactive zero-knowledge?

Which assumptions imply succinct non-interactive arguments?

Summary



Number Theory



Bilinear Maps



Lattices



Which assumptions imply non-interactive zero-knowledge?

* In a weaker preprocessing model

Which assumptions imply succinct non-interactive arguments?

Acknowledgments

Special thanks to
all of my amazing collaborators!