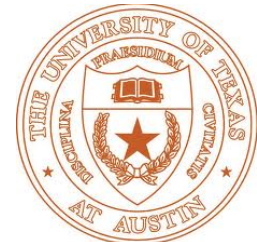


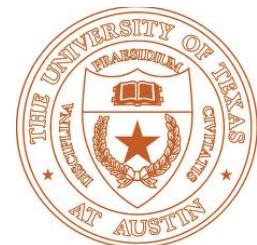
Practical Anonymous Subscriptions

**Alan Dunn, Jonathan Katz, Sangman Kim,
Michael Lee, Lara Schmidt, Brent Waters,
Emmett Witchel**



Practical Anonymous Subscriptions

**Alan Dunn, Jonathan Katz, Sangman Kim,
Michael Lee, Lara Schmidt, Brent Waters,
Emmett Witchel**





Anonymous subscriptions

Provide registered/paid users with the ability to *log in* and *access* services such as:

- Music/video streaming
- reading news articles
- transit pass

...while remaining **anonymous**...

...yet still allowing the server to enforce **admission control**

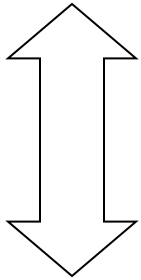
I.e., users cannot share their login with friends



System model

Time broken into a series of well-defined *epochs*

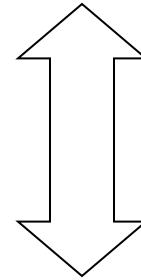
Google™



Google™



Google™

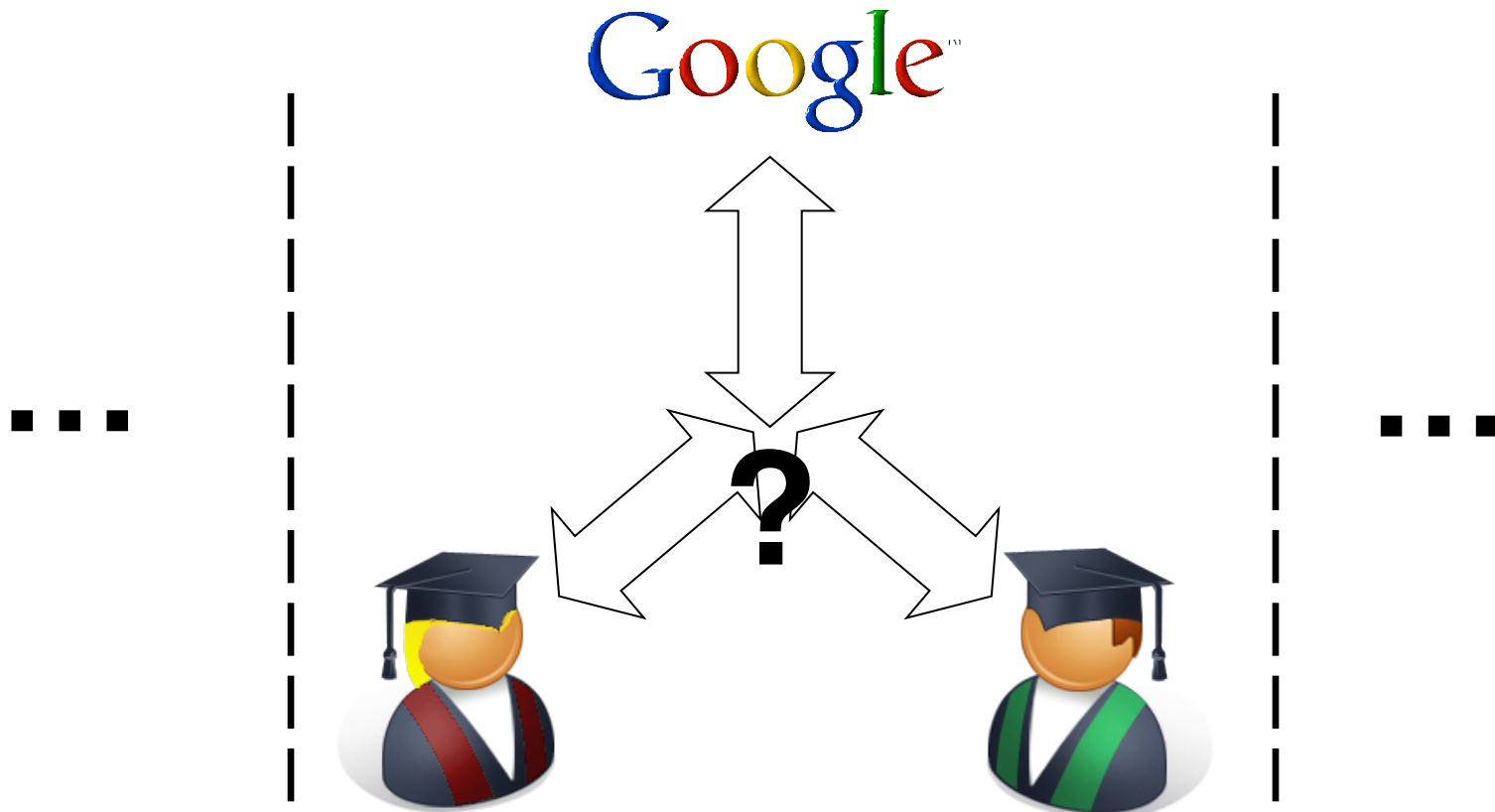




Anonymity/unlinkability

- Cannot link a **user login** to a **user registration**
- Cannot link **logins by the same user** (in different epochs) to each other

Anonymity/unlinkability



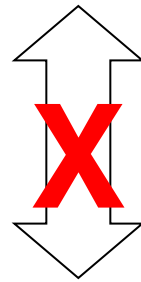
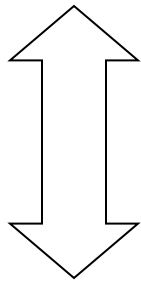


Admission ctr' I (“soundness”)

- Each registered user can only have **one** active login per epoch
 - I.e., a user cannot freely share their login information with their friends
 - (Formal definition later)

Soundness

Google™



sk_1

sk_1

...

...



How long is an epoch?

Shorter epochs \Rightarrow better anonymity

Longer epochs \Rightarrow less computation



How long is an epoch?

- Here: **conditional linkability**
 - Logged in user can choose to “re-up” his login for the next epoch
 - Re-up is cheaper than a login
 - Allows server to link user across epochs
 - User decides when this is acceptable
 - User can do a full login if unlinkability is desired



Related (but different)

- Anonymous credentials, DAA, group signatures
 - Anonymity, but no admission control
- Anonymous blacklisting systems
 - Anonymity, revocation, but no notion of per-epoch admission control
- E-cash
 - Anonymity, double spending detected, but no notion of unlimited re-use



Related work

- Unclonable authentication
[Damgård, Dupont, Østergaard]
- n-time anonymous authentication
[Camenisch et al.]
 - Uses prior ideas from e-cash [Camenisch, Hohenberger, Lysyanskaya]
 - Different model – multiple verifiers, traceability after the fact



Our contributions

- **More efficient, simpler** construction
 - “Weaker” cryptographic assumptions
 - Cleaner definitions
- **Conditional linkability** for improved efficiency
- **Implementation** and system evaluation



What we do *not* prevent

- Users sharing login information to use at **different** times

- **Other ways** of breaking anonymity
 - Traffic analysis, IP addresses
 - User behavior
 - History of accessed content

- Address using complementary techniques



Functional definition I

- **Setup** – server generates public/private keys; initializes state including **cur/next**
- **Registration** – user/server interact; user obtains secret key sk (or error)



Functional definition II

- **Login** – Using sk and the current epoch number, user logs in to server
 - Server increments **cur**
- **Link** (“re-up”) – User currently logged in during epoch t can log in for epoch $t + 1$
 - Server increments **next**



Functional definition III

- **EndEpoch** – server refreshes state; updates **cur/next**
 - **cur = next; next = 0**



Security definitions

- (Honest) user is **logged in** at some point in time if (1) that user previously ran Login in that epoch, or (2) at some point in previous epoch, user was logged in and ran Link
- (Honest) user i is **linked** at some point in time if at some previous point during that epoch, user was logged and ran Link



Soundness (informal)

- Attacker registers any number N of users; honest users also register
- Attacker interacts with server arbitrarily
- Honest users login/link (so affect server state), but attacker cannot observe
- Attacker controls when epochs end

Attacker **succeeds** if, at any point in time,
 $\mathbf{cur} > N + \# \text{honest users logged in}$



Anonymity (informal)

- Phase 0
 - Attacker outputs arbitrary public key
 - Two honest users register (and get secret keys)
- Phase I
 - Attacker induces honest users to Login/Link
- Phase II – neither user logged in
 - Users either permuted or not
 - Attacker induces honest users to Login/Link

Attacker **succeeds** if it can guess whether users were permuted in Phase II (with significantly better than $\frac{1}{2}$ probability)



Construction (intuition)

- **Registration**: user gets “anonymous credential” C (i.e., a re-randomizable blind signature) on PRF key k
- **Login** in epoch t : user sends $C' + F_k(t) +$ ZK proof of correctness
 - Server verifies signature and proof; checks that $F_k(t)$ not in table; stores $F_k(t)$ in table
- **Link** in epoch t : user sends $F_k(t) + F_k(t+1) +$ ZK proof of correctness
 - Look up $F_k(t)$ in table; verify proof; add $F_k(t+1)$



Construction (further detail)

- Anonymous credential is based on variant of **Camenisch-Lysyanskaya signatures**
 - Public key = (g^x, g^y, g^z)
 - Signature on (d, r) is $(g^a, g^{ay}, g^{ayz}, g^{ax}(g^d Z^r)^{axy})$
 - Re-randomizable, blindable, efficient ZK proofs
- **Dodis-Yampolskiy PRF**
 - $F_k(t) = g^{1/(k+t)}$
 - Compatible with various efficient ZK proofs

Construction (further detail)

■ Registration

User

$$d, r \leftarrow Z_q$$

$$M = g^d Z^r$$

PoK (d, r)

Server

$$a \leftarrow Z_q$$

$$g^a, g^{ay}, g^{ayz}, g^{ax} M^{axy}$$

Verify...



Construction (further detail)

■ Login (epoch t)

User

$sk = (A, B, Z_B, C, d, r)$

$r, s \leftarrow Z_q$

A^r, B^r, Z_B^r, C^{rs}

Server

$Y = g^{1/(d+t)}$

Verify...

Y not in table

PoK

(d in signature matches d in Y)





Construction (further detail)

- **Link** (epoch t)

User

$sk = (A, B, Z_B, C, d, r)$

Server

$$Y = g^{1/(d+t)}, Y' = g^{1/(d+t+1)}$$

Y in table?

PoK

(Y and Y' have correct form,
and d in Y matches d in Y')



Construction (further detail)

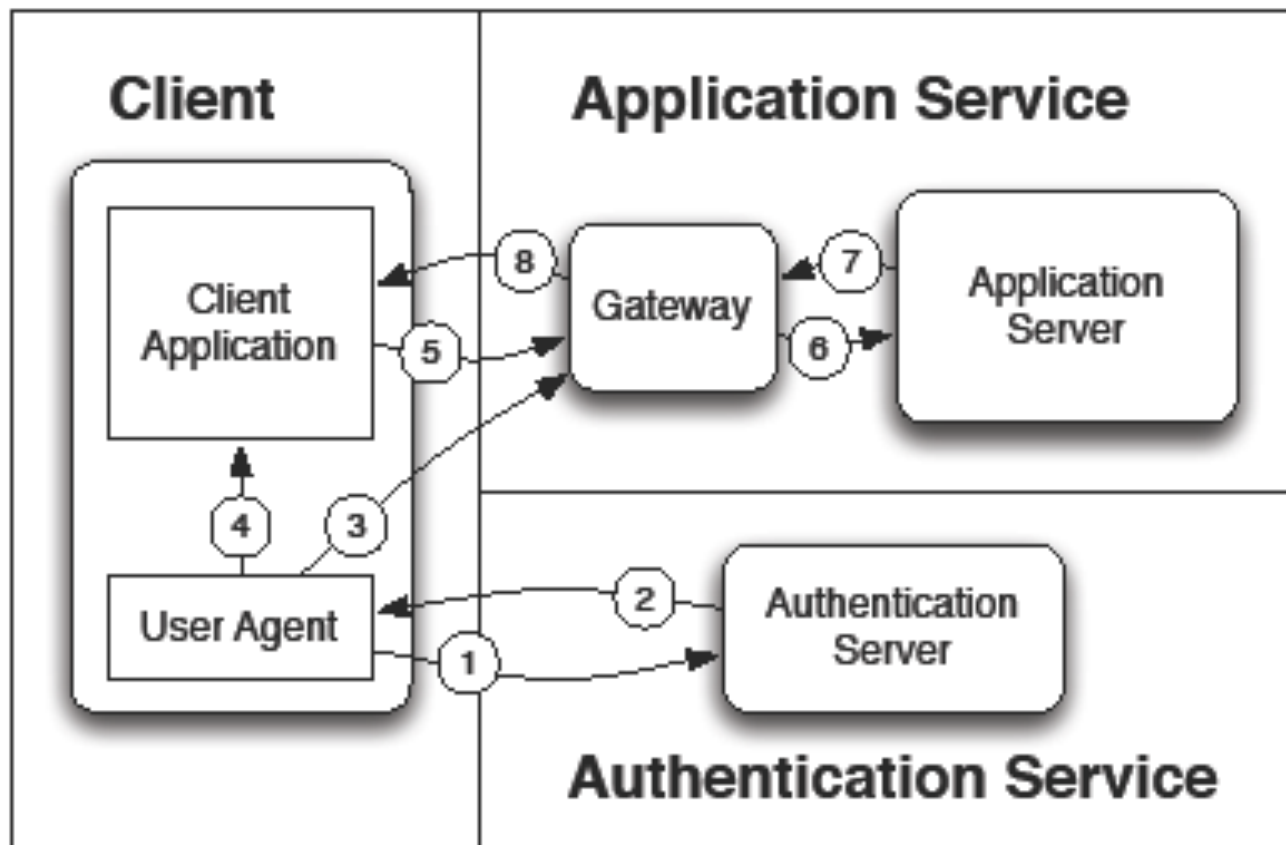
- ZK proofs (of knowledge) fairly standard
 - Made non-interactive using Fiat-Shamir



Security guarantees

- Soundness holds under **LRSW assumption** (essentially, unforgeability of CL signatures)
- Anonymity holds under **DDHI assumption**
 - $g^{1/x}$ “looks random” even given g^x, \dots, g^{x^n}
- Note: in our security proofs, we assume extraction from all ZKPoKs is possible
 - Can be enforced if interactive proofs are used and sequentiality is enforced
 - Heuristic security if Fiat-Shamir proofs are used

System architecture





Notes

- Only loose synchronization needed
 - Server sends timestamp when connection is established
 - User caches previous timestamp to prevent rollback attacks on anonymity
- Login + (multiple) link(s) are done more efficiently than running Login, Link, ...



Implementation

- Using PBC library [Lynn] and PolarSSL
 - Symmetric pairing; 160-bit elliptic-curve group over 512-bit field
- 1400 loc
- Pre-processing used when possible



Raw performance

	User	Server
Login	13.5 ms	7.9 ms
Link	1.3 ms	0.72 ms

(quad-core 2.66 GHz Intel Core 2 CPU, 8GB RAM)



Evaluation I

- Integrated our system into a streaming-music service
 - 7500 users
 - Epoch length = 15 seconds
 - Acceptable performance in terms of playback delay/latency; details in paper



Evaluation II

- Anonymous public-transit passes
 - Epoch length = 5 minutes
 - Estimate <10 servers could handle BART peak-traffic volumes
- Implemented user agent as Android app
 - Login message displayed as QR code for physical scanner to read
 - No network connectivity required
 - Login time: 220 ms (HTC Evo 3D)



Conclusions

- Design, implementation, and evaluation of a system providing **anonymous subscriptions**
- Formal definitions, cryptographic proofs
- Performance acceptable for practical applications