Lecture 4: Knowledge

Henry Corrigan - Gibbs CS355 - Spring 2019

April 10, 2019 Plan - Reap: Interactive proofs - Zero Krowledge * What it is * Why it's useful * How we define it - Example: ZK Proof for HAMCYCLE Keminders > HL 1 due Friday at Spm vin Gradescope Late day policy Today - We will be discussing the most beautiful idea in all of CS. Maybe of all time?

Controversial but still true: - Zero Knowledge - How to prove to you
that I know Something (e.g. of is SAT)
without leaking anything else to you (SAT assignment)
- Amazinely clever, also useful in many cripto
protocols. protocols. -> Lesson: Importance of definitions.

Original Zk perper is important b/c of defin of Zk,

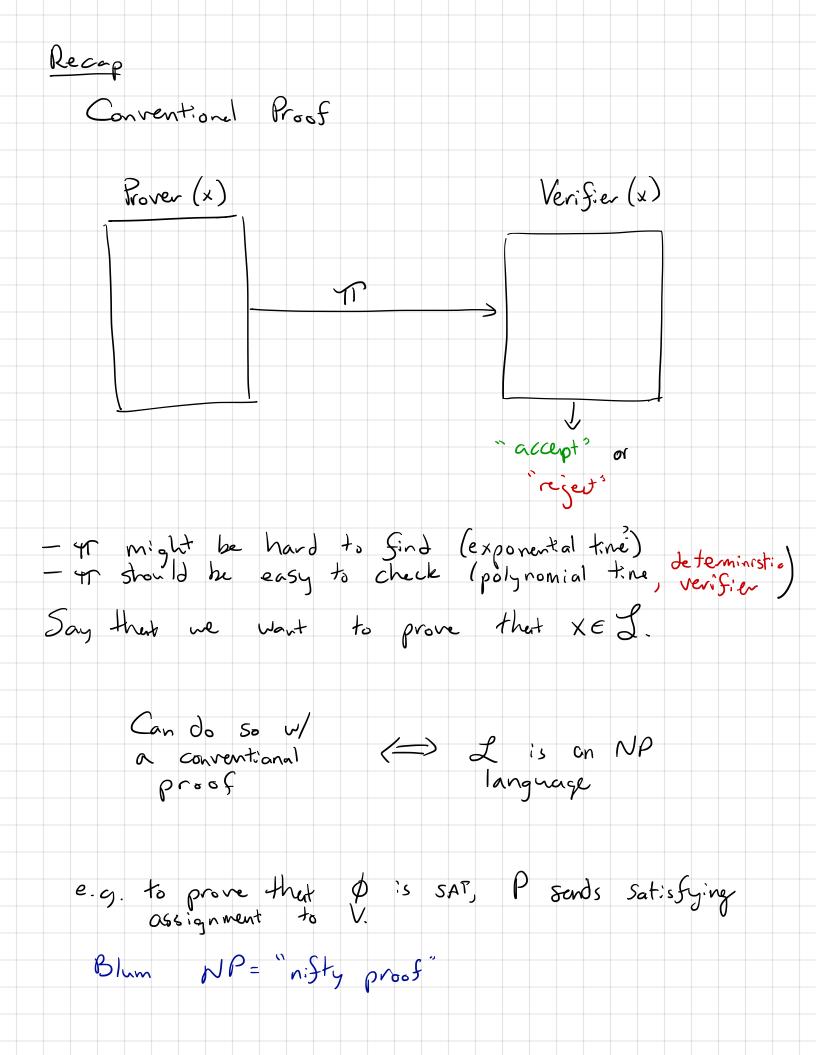
Not because of the specific constructions.

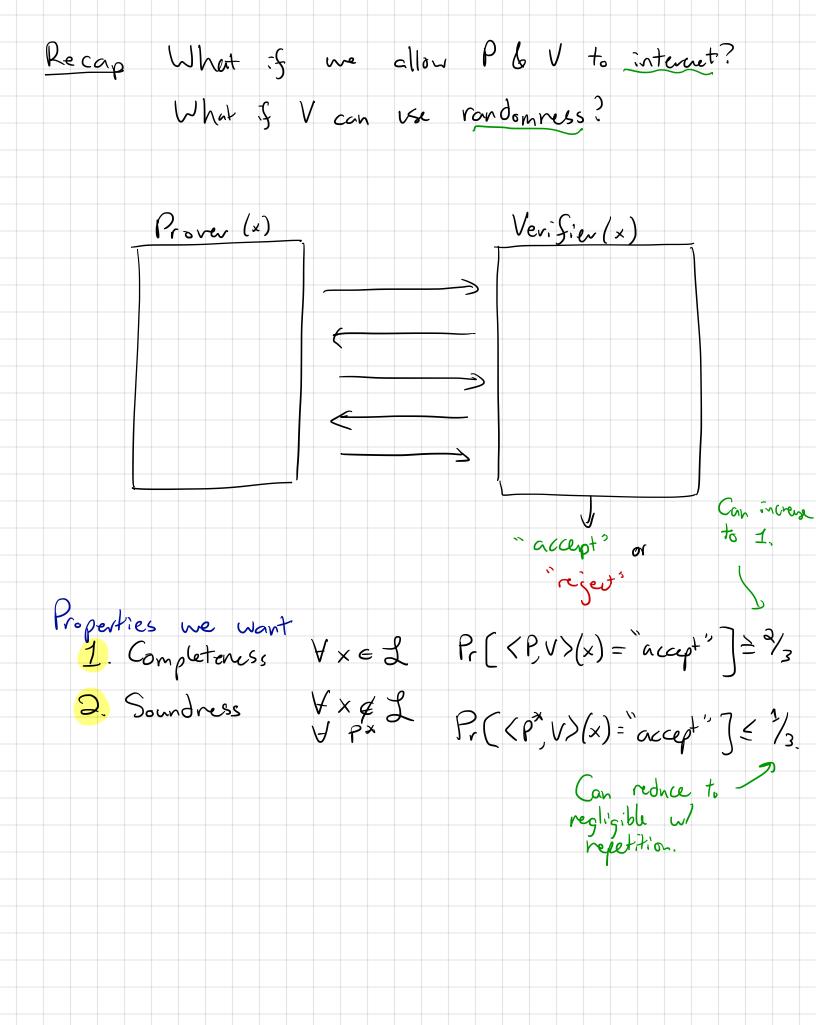
Defin is > 1/2 the bottle

Specific constructions.

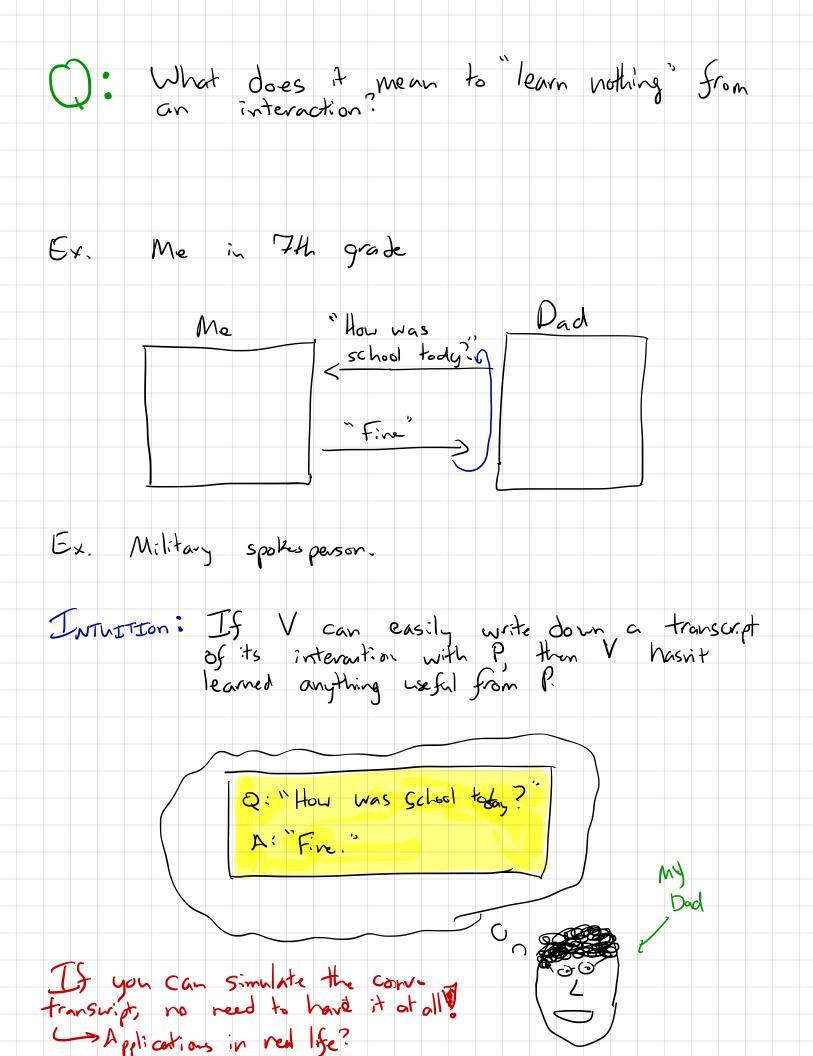
And I of Constructions. Goldwasser, Micali, Rackoff (STOC, 85)

Recap: Interactive proofs
On Monday, Florian introduced interactive proofs
Goal of a proof: Convince someone of something "the verifier" "statement"
In complexity theory, we consider statements of the formi
$x \in \mathcal{I}''$
instance language
Examples: " N is the product of exactly two prines
NE {pq prines p,q}
"The Pythagorean Thm is true."
"The Pythagoreun Thm is true." PYTHME { true statements in system }
" Ø is on unsatissiable SAT formla"
$\phi \in \S$ set of unseristiable SAT instances"

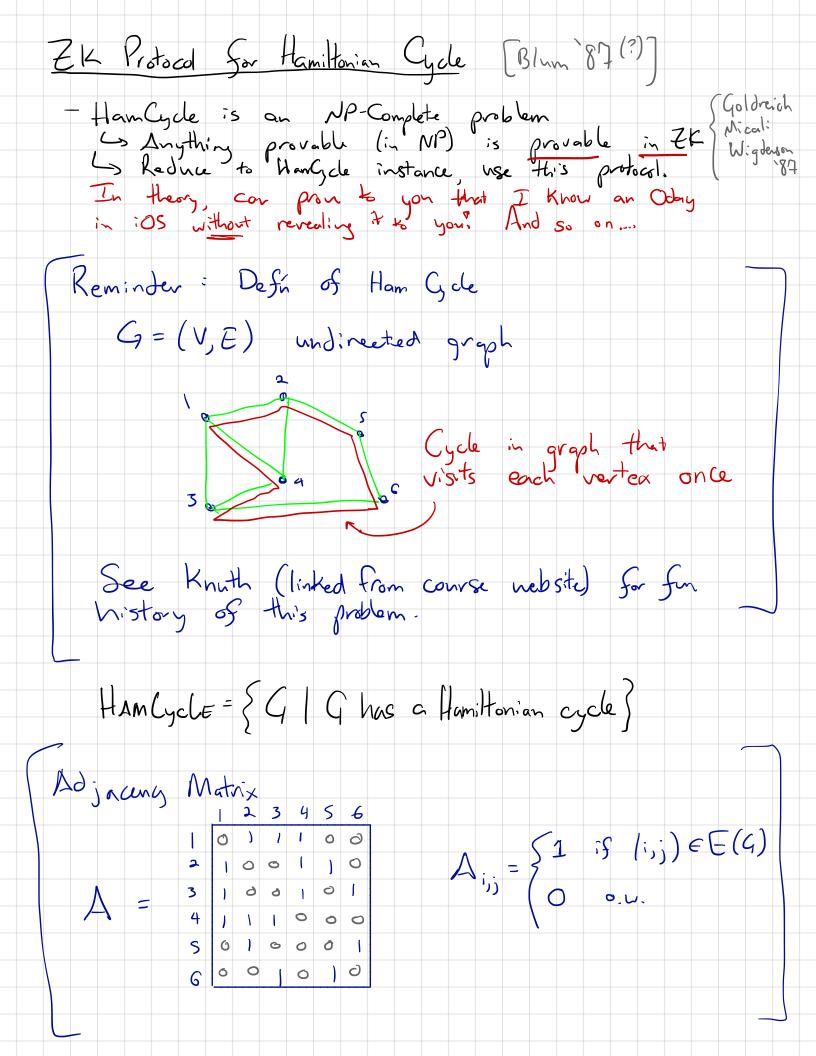


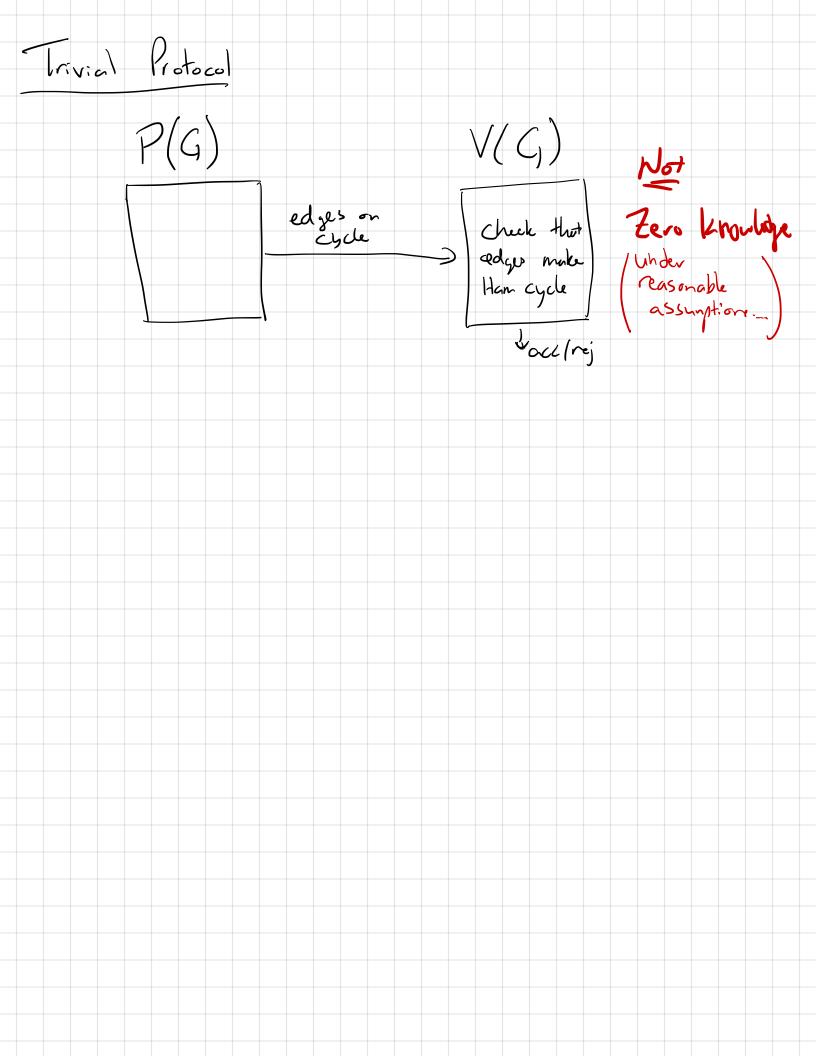


	Q <u>:</u>	Why	j is	intere	action	useful:)	
<i>A</i>	1:	(Or IP	mond Captur PSPACE	ay) es a 5prov	large, ne to you	r class in that a sle!	of pro	blems. Not
Δ	, 2 :	(Too Inte surpri	day) rautive sing	proofs	, ean	have	a H	nî ro
			Want			earns no- interaction		
					2	Huh? Who	t does	this
	Applic	ention:	Can protocol	correl Secret	yon the	at I exthat reve	ecuted s	Sonje
						security is leaks'		



The s clean	surprising t	thing is	that this:	there i	5 c, V	ery
3.	Zero Kno	uledge: V	esticient t. V x	. √*, ∃ ∈ L	efficient	Sin
		{Vieu	* [P(x)<→ V	1		
				5	perfect statistical	S\$ flavors = ≈ s ~ 1 ≈ c
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	ntuition: - Whatever 1 can learn	/ can lear s.ttg at	by into	exulting the	N/ P :	t
	Holds even is malicions	7		alions over No	w York."	
_	Key to new	rember: In	put to	/	3	capthes
						when
	nere is an a on want to -> "Auxilian	,-inpt ZK' See	Goldrei al	x 84.3	. 3	





24	Protocol (Blum)			
	Blum, well imagine ne implement w/ c	that P can ryptographic co.	send V mm,tments.	l'ilocked boxes,
	(G)		Ver:5:	er (G)
* Put each	of the n vertices v, boxes B, , , Bn in ran	dom order.		
* Into box	Bij, put § 1 if vertice are as	s in B, and B;		
Bis = relab	eling of vertices matrix under relabeling			
	Send the n-	+ (n) boxes		
		-	Flip a	coin be {0,1}
	If b=0: "Show			
	IS b=1: "Show	ne the cycle"		
	<			
If b=0:	Unlock all boxes.		Chec	le :
IS b= 1:	Unlock all boxes. Unlock only boxes corresponding to Ham Cyc Keys	·او نہ کہ .	b=0	le: Got a perm of adj, motrix
	Keys			Cot a capele
				C

Sone Comments

Box contrins ms 9 Some particular type of hash fin. Inagine: = H(m,r)(m,v) Properties 1. Complete. V 2. Sound. If G ∉ Ham Cycle, then no matter what Pt puits in bosses, V will reject w.p = 1/2. 3. Zero knowledge. L'e construct eff Sim. Sim (G & HAM Cycle) - Cruss b = (0,1).

- If b=0, put random perm of Adj not in Boxes.

- Bun b = V*(C, Boxes)

- If b = b Abort.

- Else, open boxes per V*; regrest

- Output (C, Boxes, b, Keys to boxes)

ac transcript. as transcript. N.B. When we replace it al box w/ a real commitment, we get a protocol that is only computational ZK.

Life lessons to remember

** If you can simulate as interaction,

you havan't learned anything useful from it.

** Ideally doesn't apply to this lecture.

** Input to simulator = what leaks.

** Anything that has a traditional (NP) proof also has a zero knowledge proof system.