Day 7: UTXOs
(and payments via ledgers)
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Today
(1) History of Money
(2) Public Leelger
(3) Goofy Coin
(4) Transaction for SPCS-Coin

1 A history of money

- Before computers:
- Money is a scarce object
- naturally scarce gold, seashells,
- artificially scarce: government -issued notes
- Payments are physical transfers of the object
- Properties:
- Paymaris ar irrevocable
- Scarcity is natural or foo unforgeability
- Very private
- After computers
- Money is data in a bank's computer
- Redundantly stand
- Backed by real money
- Highly regulated
- Payments are data updates
- Properties
- Fast \& convenient
- relies on integrity of banks (and laws)
- some what private: bank sees all

Key Question Does a financial system require trust? $\rightarrow$ trusting banks to follow rules trusting regulators to enforce laws trusting Th Fed/ I trams to have 'good' monetary policy

Well see that the answer is NO!
(2) The Public Ledger

Key tool: a distributed public ledger

- Rules

- Angora can post
- Entries cant be removed ("append-only")
- Everyone can see
- Everyone always sees the same ledger (consencus)

Example:
Initially: ["A"]
After Ales posts " $B$ ": [" $A$ ", "B"]
After Bob posts "C": $\left[A^{\prime \prime}, " B^{\prime}, C^{\prime \prime}\right]$
Today: How to build a financial system from ledger
Tommorow: How to build the ledger \& secure it!
3 Goofy Coin

- Ledger has two kinds of entries:
- "CreateCoin ID NAME": mints a coats from nothing 50 to NAME
- "Pay ID FROM TO": gives a coin ID from FROM to TO
- Rules: in order to "Pay", you must have the can

Examples:

| Create $O A$ | Crate $O A$ | Create $O A$ |
| :---: | :---: | :---: |
| Pay $O A B$ | Crate 1 B | Pay $O A B$ |
| Pay $O B C$ | Pay $O B C X$ | Pay $O A C X$ |
|  |  | an authorized <br> not ow owned |

Problems:
Ideas:

- Anyone can spend anyone's money !! signatures
- Anyone can mint money!!
- Cant make change!
(4) SPCS transactions?
- Ore type of ledge entry a transaction (tx)
- Aft has lists of inputs and outputs
- An output creates a coin and has
- id: a unique name for this coin
- ply: public key of who owns it
- amt: how much it is worth

An input spends a coin an has

- id: which coin is spent
- sig: a signature on id by sk for pe.
- Validation
- Transactions are validated from first to last
- As tui are validated, we maintain a set of unspent $t_{x}$ outputs (uTXOs).
- Tx rules $t$ in python: \{id:oufput $\}$
- All input ids must be in UTXO set
- All output ids must not be in UTXO set
- All input signatures must be valid
- Sum of input amounts must $\geq$ sum of of output amounts.
- Q how to get inapt amounts: from UT $X O$ set!

Examples:
Start with $\{0$ : Out (id $=0$, ph $=A$, ant $=3)\}$

$$
\begin{aligned}
& \operatorname{T}_{x}\left([ \operatorname { I n } ( \text { id } = 0 , \text { sig } = \cdots ) ] \left[O_{u}(L d=1, p k=B, \text { ant }=2\right.\right. \\
& \left.\left.O_{u} t(i d=2, p k=A, \text { ant }=1)\right]\right) \\
& \vee V \text { ald } .
\end{aligned}
$$

If the $2^{\text {nd }}$ output has amount 2? $x$ If the $1^{\text {st }}$ output has amount 1? If the signature is invalid? $x$ If the $2^{\text {nd }}$ output has id $=0$ ? $x$ If the $1^{\text {st }}$ output has $p k=A$ ? $V$

Small Example:
Alice has coins

| id: | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a m+:$ | 7 | 3 | 4 | 7 | 5 | 1 |

Alice wants to build a to pay
Bob $\$ 7$.
One way to do this: Use $\$ 7$ coin, get $\$ 10$ in change:

$$
\begin{array}{r}
\text { Ins } \\
\frac{\text { Outs }}{\text { id }=3} \\
i d=6, p k=p k_{\text {Bub, amt }}=7 \\
i d=7, p h=p k_{\text {Alice, }, \text { ant }}=10
\end{array}
$$

- How many ways can Alice get $\$ 0$ in change? Two $\$ 7$ or $\$ 3+\$ 4$
- What if Alice wants $\$ 2$ in change? $\$ 4 \pm \$ 5$
- Many ways to build teas...
- Revisiting Problems'
- Anyone can spend anyone's money
$\rightarrow$ Signatures prevent this!
- Anyone can mint money
$\rightarrow$ Undear: we havens discussed how $\$$ is created
- Cant make change
$\rightarrow$ Multiple inputs \& outputs!

Problems: Implementing Tx validation!

