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Overarching goal of cryptography: securing communication over untrusted networks

Alice Bob

third party should not be able to 1) eavesdrop of communication (confidentiality) 2) tamper with the communication (integrity)

<u>Today</u>: secure communication on web (https://...) TLS protocol (transport layer security) two components : handshake (key exchange) record layer (confidentiality + integrity)

protecting data at rest: disk encryption

<u>Most of this course</u>: study mechanics for protecting confidentiality + data Encryption schemes for confidentiality

- Signature schemes for message integrity

- Key exchange for setting up shared secrets

End of this course: protecting communication => protecting computation

Two users want to learn a joint function of their private inputs

is training modules on private (hiddun) data

is comparing two DNA sequences privately

is private auction to determine vinner without revealing bids

La private voting mechanisms (can identify winner of election without revealing individual votes)

- We will show the following remarkable theorem:

"Anything that can be computed with a trusted party can be computed without !"

- Will study concepts like zero-knowledge:

- Can you prove to someone a theorem is true without telling them any information?

- What does it mean to know something?

Logistics and administrivia:

- Course website: https://www.cs.virginia.edu/dwut/courses/Sp20

- See Piazza for announce ments

- Homework submission via Gradescope + Collab (written assignments -> Gradescope, programming -> Collab)

Course consists of 5 homework assignments (worth 75%) and one take-home midterm (worth 25%)

- Course TA: Rohit Musti

- Some lectures will be recorded (due to travel) - details will be provided later must be independent (see website)

L> Collaboration encouraged but work

L> or held live via videoconference

- Three late days for the semester (see website for info)

K K, M, C are sets (e.g., $K = M = C = \{0, 1\}^{128}$) Definition. A cipher is defined over (K, M, C) where K is a key-space, M is a message space and C is a ciphertext space, and consists of two algorithms (Encrypt, Decrypt): Encrypt: $K \times M \rightarrow C$ } functions should be "efficiently-computable" Decrypt: $K \times C \rightarrow M$ } theory: runs in probabilistic <u>polynomial</u> time [algorithm can be <u>randomized</u>] practice: fast on an actual computer (e.g., < 10ms on my laptop) <u>Correctness</u>: Ykek, YmeM: Decrypt (k, Encrypt(k, m)) = m "decrypting a ciphertext recovers the original message" A brief history of cryptography: Original goal was to protect communication (in times of war) Basic idea: Alice and Bob have a shared key k Alice computes C = Encr.pt (k, m) ciphertext key message (plaintext) Bob computes $M \leftarrow Decrypt(k, c)$ to recover the message This tuple (Encrypt, Decrypt) is called a <u>cipher</u> Early ciphers: - Caesar cipher: "shift by 3" AHD Not a cipher! There is no key! Anyone can decrypt! L> Algorithm to encrypt is assumed to be public. <u>NEVER RELY ON SECURITY BY OBSCURITY!</u> - Harder to change system than a key BH⇒E CH>F ; Xμλ YHOB - Less scrutiny for secret algorithms $Z \mapsto C$ - Caesar cipher ++ : "shift by k" (k=13: ROT-13) k is the key - Substitution cipher: the key defines a permutation of the alphabet (i.e., substitution) $\begin{array}{c|c} A \mapsto C \\ B \mapsto X \\ C \mapsto Z \\ C \mapsto J \end{array}$

 $Z \mapsto T \leftarrow$ substitution table is the key How many keys? For English alphabet, 26! $\approx 2^{88}$ possible keys

very large value, <u>cannot</u> brate force the key

- Still broken by frequency analysis e is the most frequent character (~12%) g is the least frequent character (~0.10%)
- Can also look at digram, trigram frequencies
- Vigener apper (late 1500s) "polyalphabetic substitution" key is short phrase (used to determine substitution table): m = HELLO
 - k = CAT
 - k = un, Encrypt (k, m): HELLO + <u>CATCA</u> < repeat the key "EEPP

L'interpret letters as number between 1 and 26 addition is module 26

if we know the key length, can break using frequency analysis otherwise, can try all possible key lengths l=1,2,...

L> general assumption: keys will be much shorter than the message lotherwise if we have a good mechanism to deliver long keys securely, then can use that mechanis to share messages directly

Francier substitution ciphers: Enigma (based on rator machines) but ... still breakable by frequency analysis

Today: encryption done using computers, lots of different ciphers - AES (advanced encryption standard; 2000) "block cipher" "stream cipher"

not ideal property	
One-time pad [Vigenene cipher where key is as long as the message!]	
$K = \{0, 1\}^n$ Encrypt (k, m) : output $c = k \oplus m$	
M= {o,1}" Decrypt(k,c): output m= k @ C	
C = {0,1}	n mod 2)
Correctness: Take any k E 10,11° m E 30,12°:	
Descript $(k \in Euccent(k m)) = k \oplus (k \oplus m) = (k \oplus k) \oplus m = m$	$(since \mathbf{k} \mathbf{A} \mathbf{k} = 0^{n})$
Ta this secure? How do we define security?	
- Given a citatestart second the key?	
Not Good' Sur nothing about hiden as more Fare of (k m) = m until be cause unde	a the definition but this otherway
is totally increase intribute for	
Given a ciphertect, cannot recover the message.	
NOT GOOD: Can leak part of the missage. Encrypt (K, (Mo, Mi)) - (Mo, Mi) W/. This e	norryption might be considered secure
but leaks halt the message. I imagise it message was username. alice [Passward : 123456
Given a ciphertext, cannot recover any bit of the message.	this might be the
NOT GOOD! Can still learn parity of the bits (or every poir of bits), etc. Information still	leabed
- Given a ciphertest, learn nothing about the message.	
GOOD! But how to define this.	
Coming up with good definitions is difficult! Definitions have to rule out all adversarial behavior	r li.e., capture broad enough class
of attacks)	
> Big part of crypto is getting the definitions right. Pre-1970s: cryptography has relied o	a intuition, but intuition is eiten
wrong! Just because I	connot break it does not mean
How do we capture " karning nothing about the message"?	someone else cannot
If the key is random, then ciphertext should not give information about the message.	
Definition. A cipher (Encrypt, Decrypt) satisfies perfect secrecy if for all messages mo, m, E	M, and all ciphertexts CEC:
Pr[k & K : Encrypt(k, mo) = C] = Pr[k & K : Encrypt(k, m,) =	- C]
is c, where the publicity is	
taken over the remain choice of	
the key k	

Perfect secrecy says that given a ciphertext, any two messages are equally likely.

=> Cannot infer anything about underlying message given only the ciphertext (i.e., "ciphertext - only" attack)

<u>Theorem</u>. The one-time pad sortisfies perfect secrecy: <u>Proof</u>. Take any message $M \in \{0,1\}^n$ and ciphertext $C \in \{0,1\}^n$. Then, $D_{D} \left[k \in \{0,1\}^n : Forevet(k,m) = C_1^n = P_{C} \left[k \in \{0,1\}^n : k \oplus \{0,1\}^n \right] \right]$

$$\Pr\left[k \stackrel{R}{\leftarrow} i_{0,13}^{n} : E_{ncrypt}(k,m) = C\right] = \Pr\left[k \stackrel{R}{\leftarrow} i_{0,13}^{n} : k \bigoplus m = C\right]$$
$$= \Pr\left[k \stackrel{R}{\leftarrow} i_{0,13}^{m} : k = m \bigoplus C\right]$$
$$= \frac{1}{2^{n}}$$

This holds for all messages in and ciphertexts c, so one-time put satisfies perfect secrecy.

Are we done? We now have a perfectly-secure cipher!

No! Keys are very long! In fact, as long as the message... [if we can share keys of this length, can use same mechanism to] "One-time" restriction [will revisit this later] Malleable [will revisit this later]

Issues with the one-time pad:

- One-time: Very important. Never reuse the one-time pad to encrypt two messages. Completely broken!

Suppose $c_1 = k \oplus m$, and $c_2 = k \oplus m_2$ Then, $c_1 \oplus c_2 = (k \oplus m_1) \oplus (k \oplus m_2)$ $= m_1 \oplus m_2$ Can kereage this to recover massages (HW1) $= m_1 \oplus m_2$ Can kereage this to recover massages (HW1)

One-time pad reuse:

- Project Verona (U.S. counter-intelligence operation against U.S.S.R during Cold War)

- → Soviets reused some pages in codebook ~ led to decryption of ~ 3000 messages sent by Soviet intelligence over 37-year period [notably exposed espionage by Julius and Ethul Rosenberg] - Microsoft Point-to-Point Tunneling (MS-EPTP) in Windows 98/NT (used for VPN)
 - ightarrow Same key (in stream cipher) used for both server ightarrow client communication AND for client ightarrow server ightarrow communication ightarrow (RC4)

- 802.11 WEP: both client and server use same key to encrypt traffic

many problems just beyond one-time pad reuse (can even recover key after observing small number of frames!)

- Malleable: one-time pad provides no integrity; anyone can modify the ciphertext:

^C replace c with c⊕m'

⇒ k ⊕ (c ⊕ m') = m ⊕ m' ← adversary's change now xored into original message