Sufficient now to construct a compression function.

Typical approach is to use a block cipher.

Davies-Meyer: Let $F: \mathbb{K} \times X \longrightarrow X$ be a block cipher. The Davies-Meyer compression function h: K×X→X is then $h(k, x) := F(k, x) \oplus x$ tinex F Many other variants also possible : $h(k, x) = F(k, x) \oplus k \oplus x$ [used in Whirlpool hash family] Need to be careful with design! $Th(k,x) = F(k,x) \text{ is } \underline{not} \text{ collision-resistant} : h(k,x) = h(k', F'(k', F(k,x)))$ $-h(k,x) = F(k,x) \oplus k \quad \text{is not collision-resistant}: h(k,x) = h(k',F'(k',F(k,x) \oplus k \oplus k'))$ Theorem. If we model F as an ideal block cipher (i.e., a traly random permutation for every choice of key), then Davies-Meyer is > birthday attack ran-time: ~280 attack ran in time ~264 (100,000× faster) collision - resistant. January, 2020: chosen-prefix
Collision in ~2644 fine!
no longer secure [first collision found in 2017!] Conclusion: Block cipher + Davies-Meyer + Merkle-Damyard => CRHFs Ecomples: SHA-1: SHACAL-1 block cipher with Dowies-Meyer + Merkle-Damg&rd SHA-256: SHACAL-2 block cipher with Davies-Meyer + Merkle-Dangerd -SHA-1 extensively used (e.g., git, srn, software uplates, PGP/GPG eignornes, certificances) -> attacks show need -Block size too small! AES outputs are 128-bits, not 256 sits (so birthday attack finds collision in 2^{G4} fine) to transition to SHA-2 or SHA-3 Why not use AES? - Short keys means small number of message bits processed per iteration. Typically, block cipher designed to be fast when using same key to encrypt many messages L> In Merkle-Dangard, <u>different</u> keys are used, so alternate design preferred (AES key schedule is expensive) <u>Recently</u>: SHA-3 family of hash functions standardized (2015) L> Relies on different underlying structure ("sponge" function) 1-> Both SHA-2 and SHA-3 are believed to be secure (most systems we SHA-2 - typically much faster) V or even better, a large-domain PRF Back to building a secure MAC from a CRHF - can we do it more directly than using CRHF + small-domain MAC? hain difficulty seems to be that CRHFs are keyless but MACs are keyed Idea: include the key as part of the hashed input By "itself, collision-resistance does not provide any "randomness" guasantees on the output → For instance, if H is collision-resistant, then H'(m) = moll... ||m10 || H(m) is also collision-resistant even though H' also leaks the first 10 bits/blocks of m L> Constructing a PRF/MAC from a hash function will require more than just collision resistance - Option 1: Model hash function as an "ideal hash function" that behaves like a fixed truly random function (modeling <u>leuristic</u> called the random oracle model - will encounter later in this course) - Option 2: Start with a concrete construction of a CRHF (e.g., Merkle-Damgård or the sponge construction) and reason about its properties L> we will take this approach

Suppose H is a Merkle-Damgerd Lash function built from a secure compression function