

if 
$$T = g^2$$
, then  $(g^3, g^2, m)$  is uniform over  $G^2$  (since y, 2 are sampled independently of each other an   
of m) — this is exactly the distribution where A sees  $(c_0, c_i) \stackrel{a}{\leftarrow} G^2$ 

What if we want to encrypt longer necessages? [or messages that is not a group element] - Hybrid encryption (key encapsulation [KEM]):

Use PKE scheme to encrypt a secret key [PKE Encrypt (pk, k) "header" [slows] Encrypt payload using secret key + authenticated encryption ]AE. Encrypt (k, M) "payload" [fast]

orade,

Vanilla ElGamal described above is not CCA-secure!

Ciphertexts are malleable: given ct = (g<sup>3</sup>, h<sup>3</sup>·m), can construct ciphertext (g<sup>3</sup>, h<sup>3</sup>·m·g) which decrypts to message m·g L> directly implies a CCA attack

Several approaches to get CCA security from DH assumptions:

- Cramer-Shoup (CCA-security from DDH) based on hash-proof systems We do not know of any groups where CDH - Fujisaki-Okamoto transformation (using an ideal hash function + CDH) believed to be hard, but interactive CDH - Make stronger assumption (interactive CDH + use ideal hash function): (CDH is hard even
- Make stronger assumption (interactive CDH + use ideal hash function):
  Setup: x & Zp pk:h
  Labo called strong DH assumption
  Symmetric authenticated
  A DDH oracle a DDH oracle
  Encrypt (pk, m): y & Zp k ← H(g, g<sup>x</sup>, g<sup>y</sup>, h<sup>y</sup>) ct' ← EncAE (k, m)
  C ← (g<sup>y</sup>, ct')
  Decrypt (sk, c): k ← H(g, g<sup>x</sup>, co, c<sup>x</sup>)

Essentially ElGanal where key derived from bosh function

 $m \leftarrow Dec_{AE}(k, c,)$