Now, we will see how to use LWE to obtain a key agreement protoco)

We start with an anortized version of Reger's PKE scheme where each ciphertext encrypts a <u>vector</u> of bits <u>Vanilla Reger</u>: encryption of single bit  $\mu \in \{0,1\}$  is a vector  $c = Ar + \mu \cdot \lfloor \frac{4}{2} \rceil \cdot \lfloor \frac{0}{1} \rceil$ Encrypting multiple bits: May seen wasteful to use a vector to encrypt a <u>single</u> bit. We can consider a simple variant of Reger encryption where we rever A to encrypt multiple bits: <u>Setup(1<sup>n</sup>, 1<sup>k</sup>)</u>: sample  $A \stackrel{a}{=} \mathbb{Z}_{1}^{non}$   $S \stackrel{a}{=} \mathbb{Z}_{1}^{nvL}$   $B^{T} \in S^{T}A + E^{T} \in \mathbb{Z}_{1}^{kon}$  sk: S <u>Setup(1<sup>n</sup>, 1<sup>k</sup>)</u>: sample  $r \stackrel{a}{=} 1_{0}r_{1}^{N}$   $B = compt(pk, \mu \in 10r_{1}^{N})$ : sample  $r \stackrel{a}{=} 1_{0}r_{1}^{N}$  unitable concentrated together $<u>Encrypt(pk, \mu \in 10r_{1}^{N})</u>: sample <math>r \stackrel{a}{=} 1_{0}r_{1}^{N}$  unitable concentrated together $<u>Encrypt(sk, ct)</u>: output <math>Lct_{2} \cdot S^{T}ct_{1}|_{2}$ <u>Convectores</u>: As before:  $ct_{2} - S^{T}ct_{1} = B^{T}r + \mu \cdot \lfloor \frac{1}{2} \rfloor$ <u>Security</u>: As before: by Live,  $(A, S^{T}A + E^{T}) \stackrel{a}{\sim} (A, R)$  where  $A \stackrel{a}{=} \mathbb{Z}_{1}^{non}$ ,  $S \stackrel{a}{=} \mathbb{Z}_{1}^{nk}$ ,  $E \in \chi^{nvA}$ ,  $R \stackrel{a}{=} \mathbb{Z}_{1}^{kn}$ <u>Convectores</u>: how the convertice of a compared and and again for each row of S (and conversionly row of S^{T}A + E^{T}). Plite b and the tild of the tild of the tild of the compared of a compared by conversion of  $S^{T}A + E^{T}$ .

Public keys are large ; if m = n log g, then public key has size n²log g - for instance : n ~ 600, g ~ 2<sup>12</sup> (~ 550 KB) L> Can shrink public keys to n² (Will kave as exercise; hint: sample secret key from error distribution) L> Can shrink further using ring LWE (O(n) public key size)

Lattice-based key exchange. Recall Diffie-Hellman:

